A Story of Units®

Succeed

Eureka Math helps students truly understand mathematics and connect it to the real world, preparing them to solve problems they have not encountered. Great Minds teachers and mathematicians believe that it is not enough for students to know the process for solving a problem; they need to understand why that process works.

Eureka Math presents mathematics as a story, one that develops from grades PK through 12. In A Story of Units, our elementary curriculum, this sequencing has been joined with methods of instruction that have been proven to work, in this nation and abroad.

Great Minds is here to make sure you succeed with an ever-growing library of resources, including free tip sheets, resource sheets, and full grade-level modules at eureka-math.org.

Sequence of Grade 5 Modules

Module 1: Place Value and Decimal Fractions

Module 3: Addition and Subtraction of Fractions

Module 4: Multiplication and Division of Fractions and Decimal Fractions

Module 5: Addition and Multiplication with Volume and Area

Module 6: Problem Solving with the Coordinate Plane



What does this painting have to do with math? Turn this book over to find out.

Vincent van Gogh (1853-1890), The Bedroom at Arles, 1889. Oil on canvas, 57.5 x 74.0 cm. Inv. RF1959-2. Photo: Hervé Lewandowski Location: Musée d'Orsay, Paris, France Photo Credit: © RMN-Grand Palais / Art Resource, NY

What does this painting have to do with math?

In an effort to take advantage of every opportunity to build students' cultural literacy, Great Minds features an important work of art or architecture on the cover of each book we publish. We select images that we know students and teachers will love to look at again and again. These works also relate, in visual terms, to ideas taken up in the book. In his painting The Bedroom at Arles, Vincent van Gogh evidenced thoughtful care in his arrangement of objects, not unlike the sort of intentionality we hope A Story of Units will cultivate in students' manipulation of units.





Eureka Math Grade 5 Modules 1 & 2

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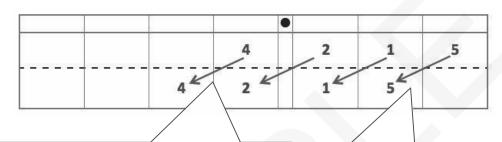
Student Name:

Published by Great Minds®

Note: It is common to encourage students to simply "move the decimal point" a number of places when multiplying or dividing by powers of 10. Instead, encourage students to understand that the decimal point lives between the ones place and the tenths place. The decimal point does not move. Rather, the digits shift along the place value chart when multiplying and dividing by powers of ten.

Use the place value chart and arrows to show how the value of the each digit changes.

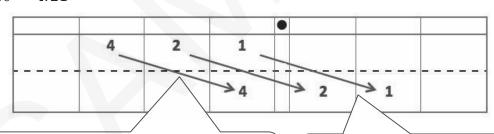
1. $4.215 \times 10 = 42.15$



4 ones times 10 is 4 tens. Since I'm multiplying by 10, the value of each digit becomes 10 times greater.

When multiplying by 10, each digit shifts 1 place to the left on the place value chart.

2. $421 \div 100 = 4.21$



4 hundreds divided by 100 is 4 ones. Since I'm dividing by 100, the value of each digit becomes 100 times smaller.

When dividing by 100, each digit shifts 2 places to the right on the place value chart.

Lesson 1:

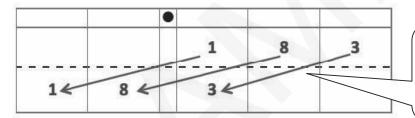
3. A student used his place value chart to show a number. After the teacher instructed him to multiply his number by 10, the chart showed 3,200.4. Draw a picture of what the place value chart looked like at first.

 $3\ \mbox{hundreds}$ times $10\ \mbox{is}\ 3$ thousands. The original number must have had a $3\ \mbox{in}$ the hundreds place.

thousands	hundreds	tens	ones	•	tenths	hundredths	thousandths
	3	2	0		0	4	
	2			3 1	7,000		

I used the place value chart to help me visualize what the original number was. When multiplying by 10, each digit must have shifted 1 place to the left, so I shifted each digit 1 place back to the right to show the original number.

4. A microscope has a setting that magnifies an object so that it appears 100 times as large when viewed through the eyepiece. If a small bug is 0.183 cm long, how long will the insect appear in centimeters through the microscope? Explain how you know.



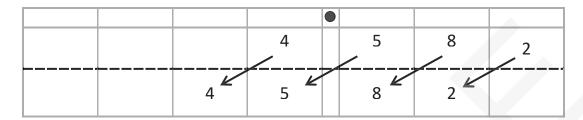
When multiplying by 100, each digit shifts 2 places to the *left* on the place value chart.

The bug will appear to be 18.3 cm long through the microscope.

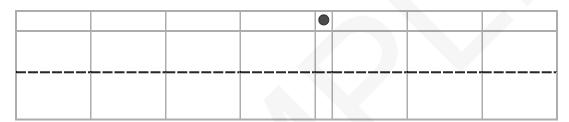
Since the microscope magnifies objects 100 times, the bug will appear to be 100 times larger. I used a place value chart to show what happens to the value of each digit when it is multiplied by 100. Each digit shifts 2 places to the left.

Nama	Data
Name	Date

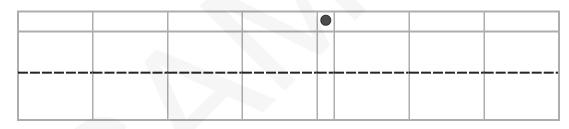
- 1. Use the place value chart and arrows to show how the value of each digit changes. The first one has been done for you.
 - a. 4.582 × 10 = <u>45.82</u>



b. 7.281 × 100 = ____



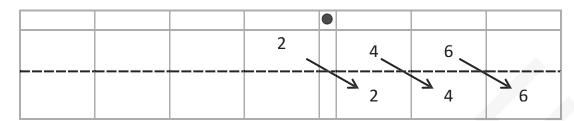
c. 9.254 × 1,000 = __



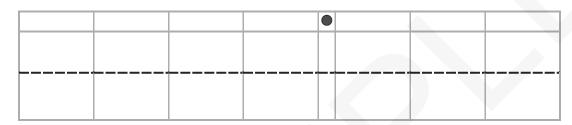
d. Explain how and why the value of the 2 changed in (a), (b), and (c).

2. Use the place value chart and arrows to show how the value of each digit changes. The first one has been done for you.

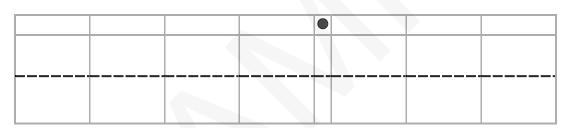
a. $2.46 \div 10 = 0.246$



b. 678 ÷ 100 = ____



c. 67 ÷ 1,000 = ____



d. Explain how and why the value of the 6 changed in the quotients in (a), (b), and (c).

- 3. Researchers counted 8,912 monarch butterflies on one branch of a tree at a site in Mexico. They estimated that the total number of butterflies at the site was 1,000 times as large. About how many butterflies were at the site in all? Explain your thinking, and include a statement of the solution.
- 4. A student used his place value chart to show a number. After the teacher instructed him to divide his number by 100, the chart showed 28.003. Draw a picture of what the place value chart looked like at first.



Explain how you decided what to draw on your place value chart. Be sure to include reasoning about how the value of each digit was affected by the division.

5. On a map, the perimeter of a park is 0.251 meters. The actual perimeter of the park is 1,000 times as large. What is the actual perimeter of the park? Explain how you know using a place value chart.





1. Solve.

a.
$$4,258 \times 10 = 42,580$$

I visualized a place value chart. 8 ones times 10 is 8 tens. When multiplying by 10, each digit shifts 1 place to the *left*.

b.
$$4,258 \div 10 = 425.8$$

When dividing by 10, each digit shifts 1 place to the \emph{right} .

c.
$$3.9 \times 100 = 390$$

The factor 100, has 2 zeros, so I can visualize each digit shifting 2 places to the *left*.

d.
$$3.9 \div 100 = 0.039$$

The divisor, 100, has 2 zeros, so each digit shifts 2 places to the *right*.

$$7 \times 1 \text{ hundred} = 7 \text{ hundreds} = 700$$

2. Solve.

a.
$$9,647 \times 100 =$$
964, **700**

b.
$$9,647 \div 1,000 = ______9.647$$

$$7 \div 1 \text{ thousand} = 7 \text{ thousandths} = 0.007$$

I visualized a place value chart. Multiplying by 100 shifts each digit in the factor 9,647 two places to the left, so there were 2 additional zeros in the product.

d. Explain how you decided where to place the decimal in the quotient for part (b).

Explain how you decided on the number of zeros in the product for part (a).

The divisor, 1,000, has 3 zeros, so each digit in 9,647 shifts 3 places to the right. When the digit 9 shifts 3 places to the right, it moves to the ones places, so I knew the decimal point needed to go between the ones place and the tenths place. I put the decimal between the 9 and the 6.

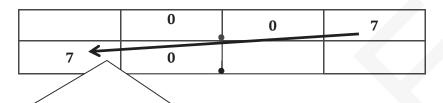


9

3. Jasmine says that 7 hundredths multiplied by 1,000 equals 7 thousands. Is she correct? Use a place value chart to explain your answer.

Jasmine is not correct. 7 ones \times 1,000 would be 7 thousands.

But $0.07 \times 1,000 = 70$. Look at my place value chart.

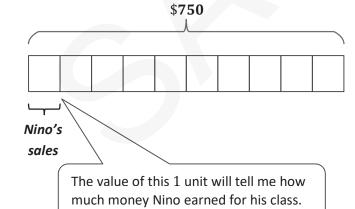


The factor 1,000 has 3 zeros, so the digit 7 shifts 3 places to the left on the place value chart.

4. Nino's class earned \$750 selling candy bars for a fundraiser. $\frac{1}{10}$ of all the money collected was from sales made by Nino. How much money did Nino raise?

The whole tape represents all of the money earned by Nino's class.

Nino collected $\frac{1}{10}$ of all the money, so I partition the tape diagram into 10 equal units.



$$10 \text{ units} = \$750$$

$$1\,\text{unit} = \$750 \div 10$$

$$1 \text{ unit} = $75$$

Nino raised \$75.

1. Solve.

2. Find the products.

Explain how you decided on the number of zeros in the products for (a), (b), and (c).

3. Find the quotients.

a. 16.5 ÷ 10 = _____

b. 16.5 ÷ 100 = _____

c. Explain how you decided where to place the decimal in the quotients for (a) and (b).

4. Ted says that 3 tenths multiplied by 100 equals 300 thousandths. Is he correct? Use a place value chart to explain your answer.

5. Alaska has a land area of about 1,700,000 square kilometers. Florida has a land area $\frac{1}{10}$ the size of Alaska. What is the land area of Florida? Explain how you found your answer.



1. Write the following in exponential form.

a.
$$10 \times 10 \times 10 = _{\underline{}}$$

b. $1,000 \times 10 = _{0}$

10 is a factor 3 times, so the exponent is 3. I can read this as, "ten to the third power."

- c. $100,000 = 10^5$
- d. $100 = 10^2$

 $1,000 = 10 \times 10 \times 10$, so this expression uses 10 as a factor 4 times. The exponent is 4.

I recognize a pattern. 100 has 2 zeros. Therefore, the exponent is 2. One hundred equals 10 to the 2^{nd} power.

2. Write the following in standard form.

a.
$$6 \times 10^3 =$$
 6,000

 10^3 is equal to 1,000. 6 times 1 thousand is 6 thousand.

c.
$$643 \div 10^3 = \mathbf{0.643}$$

b.
$$60.43 \times 10^4 = 604,300$$

The exponent 4 tells me how many places each digit will shift to the left. d. $6.4 \div 10^2 = 0.064$

The exponent 2 tells me how many places each digit will shift to the right.

3. Complete the patterns.

a. 0.06

0.6

600

6,000

6 tenths is larger than 6 hundredths. Each number in the pattern is 10 times larger than the previous number.

60

b. **92**, **100**

9,210

921

9.21 92.1

0.921

The numbers are getting smaller in this pattern.

The digits have each shifted 1 place to the right. The pattern in this sequence is "divide by 10^1 ."



Date _____

1. Write the following in exponential form (e.g., $100 = 10^2$).

2. Write the following in standard form (e.g., $4 \times 10^2 = 400$).

a.
$$4 \times 10^3 =$$

e.
$$6.072 \times 10^3 =$$

c.
$$5,300 \div 10^2 =$$

g.
$$948 \div 10^3 =$$

d.
$$5,300,000 \div 10^3 =$$

h.
$$9.4 \div 10^2 =$$

3. Complete the patterns.

34,000

3.4

8,570

85.7

d. 444 4440 44,400

e. _____ 9.5 950

95,000

4. After a lesson on exponents, Tia went home and said to her mom, "I learned that 10⁴ is the same as 40,000." She has made a mistake in her thinking. Use words, numbers, or a place value chart to help Tia correct her mistake.

- 5. Solve $247 \div 10^2$ and 247×10^2 .
 - a. What is different about the two answers? Use words, numbers, or pictures to explain how the digits shift.

b. Based on the answers from the pair of expressions above, solve $247 \div 10^3$ and 247×10^3 .



In the first 2 problems, I am converting a

In these 2 problems, I am converting a smaller unit to a larger unit. Therefore, I need to divide to find the equivalent

larger unit to a smaller unit. Therefore, I need to multiply to find the equivalent 1. Convert and write an equation with an exponent. length.

1 meter is equal to 100 centimeters.

a. 4 meters to centimeters

4 m = 400 cm

 $4 \times 10^2 = 400$

1 meter is equal to 1,000 millimeters.

b. 2.8 meters to millimeters

2.8 m = 2,800 mm

 $2.8 \times 10^3 = 2,800$

2. Convert using an equation with an exponent.

There are 100 centimeters in 1 meter.

a. 87 centimeters to meters

cm = 0.87

length.

 $87 \div 10^2 = 0.87$

There are 1,000 millimeters in 1 meter.

b. 9 millimeters to meters

9 mm = 0.009 m

 $9 \div 10^3 = 0.009$

3. The height of a cellphone is 13 cm. Express this measurement in meters. Explain your thinking. Include an equation with an exponent in your explanation.

$$13 \text{ cm} = 0.13 \text{ m}$$

In order to rename smaller units as larger units, I'll need to divide.

Since 1 meter is equal to 100 centimeters, I divided the number of centimeters by 100.

$$13 \div 10^2 = 0.13$$

I need to include an equation with an exponent, so I'll express 100 as 10^2 .



Use exponents to denote powers of 10 with application to metric



Na	me _			Date
1.	Con	overt and write an equation with	n an exponent. Use your meter	strip when it helps you.
	a.	2 meters to centimeters	2m = 200 cm	$2 \times 10^2 = 200$
	b.	108 centimeters to meters	108 cm = m	
	c.	2.49 meters to centimeters	m = cm	
	d.	50 centimeters to meters	cm = m	
	e.	6.3 meters to centimeters	m = cm	
	f.	7 centimeters to meters	cm = m	
	g.	In the space below, list the let	ters of the problems where sma	aller units are converted to larger units.
2.	Con	overt using an equation with an	exponent. Use your meter strip	when it helps you.
	a.	4 meters to millimeters	m = mm	
	b.	1.7 meters to millimeters	m = mm	
	c.	1,050 millimeters to meters	mm = m	
	d.	65 millimeters to meters	mm = m	
	e.	4.92 meters to millimeters	m = mm	
	f.	3 millimeters to meters	mm = m	

g. In the space below, list the letters of the problems where larger units are converted to smaller units.

3. Read each aloud as you write the equivalent measures. Write an equation with an exponent you might use to convert.

a. 2.638 m

= mm

 $2.638 \times 10^3 = 2,638$

b. 7 cm

= m

c. 39 mm

= m

d. 0.08 m

= _____ mm

e. 0.005 m

= _____ cm

4. Yi Ting's height is 1.49 m. Express this measurement in millimeters. Explain your thinking. Include an equation with an exponent in your explanation.

5. A ladybug's length measures 2 cm. Express this measurement in meters. Explain your thinking. Include an equation with an exponent in your explanation.

6. The length of a sticky note measures 77 millimeters. Express this length in meters. Explain your thinking. Include an equation with an exponent in your explanation.

- 1. Express as decimal numerals.
 - a. Eight and three hundred fifty-two thousandths

8.352

b. $\frac{6}{100}$

The word *and* separates the whole numbers from the decimal numbers.

I can rewrite this fraction as a decimal. There are zero ones and zero tenths

0.06

- c. $5\frac{132}{1000}$
 - 5.132
- 2. Express in words.

a. 0.034

Thirty-four thousandths

The word *and* separates the whole numbers from the decimal numbers.

b. 73.29

Seventy-three and twenty-nine hundredths

3. Write the number in expanded form using decimals and fractions.

in the fraction 6 hundredths.

303.084

$$3 \times 100 + 3 \times 1 + 8 \times 0.01 + 4 \times 0.001$$

$$3 \times 100 + 3 \times 1 + 8 \times \frac{1}{100} + 4 \times \frac{1}{1000}$$

This expanded form uses decimals. 8 hundredths is the same as 8 units of 1 hundredth or (8×0.01) .

This expanded form uses fractions.

$$\frac{1}{1000} = 0.001$$

Both are read as one thousandths.



9.936

- 4. Write a decimal for each of the following.
 - a. $4 \times 100 + 5 \times 1 + 2 \times \frac{1}{10} + 8 \times \frac{1}{1000}$ 405.208
 - b. $9 \times 1 + 9 \times 0.1 + 3 \times 0.01 + 6 \times 0.001$

There are 0 tens and 0 hundredths in expanded form, so I wrote 0 tens and 0 hundredths in standard form too.

 $3\,\times\,0.01$ is 3 units of 1 hundredth, which I can write as a 3 in the hundredths place.

Name	Date
Name	Date

1. Express as decimal numerals. The first one is done for you.

a.	Five thousandths	0.005
b.	Thirty-five thousandths	
c.	Nine and two hundred thirty-five thousandths	
d.	Eight hundred and five thousandths	
e.	8 1000	
f.	28 1000	
g.	$7\frac{528}{1000}$	
h.	$300\frac{502}{1000}$	

2. Express each of the following values in words.

a 0 (800						
-------	-----	--	--	--	--	--	--

3. Write the number on a place value chart. Then, write it in expanded form using fractions or decimals to express the decimal place value units. The first one is done for you.

a. 27.346

Tens	Ones	Tenths	Hundredths	Thousandths
2	7	3	4	6

$$27.346 = 2 \times 10 + 7 \times 1 + 3 \times \left(\frac{1}{10}\right) + 4 \times \left(\frac{1}{100}\right) + 6 \times \left(\frac{1}{1000}\right) \text{ or}$$

$$27.346 = 2 \times 10 + 7 \times 1 + 3 \times 0.1 + 4 \times 0.01 + 6 \times 0.001$$

b. 0.362

c. 49.564

4. Write a decimal for each of the following. Use a place value chart to help, if necessary.

a.
$$3 \times 10 + 5 \times 1 + 2 \times \left(\frac{1}{10}\right) + 7 \times \left(\frac{1}{100}\right) + 6 \times \left(\frac{1}{1000}\right)$$

b.
$$9 \times 100 + 2 \times 10 + 3 \times 0.1 + 7 \times 0.001$$

c.
$$5 \times 1000 + 4 \times 100 + 8 \times 1 + 6 \times \left(\frac{1}{100}\right) + 5 \times \left(\frac{1}{1000}\right)$$

- 5. At the beginning of a lesson, a piece of chalk is 4.875 inches long. At the end of the lesson, it is 3.125 inches long. Write the two amounts in expanded form using fractions.
 - a. At the beginning of the lesson:
 - b. At the end of the lesson:
- 6. Mrs. Herman asked the class to write an expanded form for 412.638. Nancy wrote the expanded form using fractions, and Charles wrote the expanded form using decimals. Write their responses.

Thousandths	
Hundredths	
Tenths	
Ones	
Tens	
Hundreds	
Thousands	

thousands through thousandths place value chart





1. Show the numbers on the place value chart using digits. Use >, <, or = to compare.

43.554 > 43.545

	4	3	5	5	4
	4	3	5	4	5

5 hundredths is greater than 4 hundredths. Therefore, 43.554 > 43.545.

I put each digit of both numbers in the place value chart. Now I can easily compare the values.

- 2. Use the >, <, or = to compare the following.
 - a. 7.4 = 74 tenths

20 tenths = 2 ones70 tenths = 7 ones10 tenths = 1 oneTherefore, 74 tenths = 7 ones and 4 tenths.

b. 2.7 \geq Twenty-seven hundredths

1 one = 10 tenths2 ones = 20 tenths2.7 = 27 tenthsTenths are a larger unit that hundredths, therefore 27 tenths is greater than 27 hundredths.

c. $3.12 \leq 312$ tenths

I can think of both numbers in unit form: 312 hundredths < 312 tenths. Hundredths are a smaller unit than tenths.

I can also think of both numbers in decimal notation: 3.12 < 31.2.

d. 1.17 > 1.165

Both of these numbers have 1 one and 1 tenth. But 7 hundredths is *greater* than 6 hundredths. I know that 1.17 is greater than 1.165.

I need to be careful! Although 1.165 has more digits than 1.17, it doesn't always mean it has a greater value.

I also know that 1.17 = 1.170. When both numbers have the same number of digits, I can clearly see that 1.170 > 1.165.

3. Arrange the numbers in *increasing* order.

8.719 8.79 8.7 8.179

8.179, 8.7, 8.719, 8.79

Increasing order means I need to list the numbers from *least* to *greatest*.

8	7	1	9
8	7	9	
8	7		
8	1	7	9
	$\overline{}$		

All of the numbers have 8 ones. 1 tenth is less than 7 tenths, so 8.179 is the smallest number.

To make comparing easier, I'm going to use a place value chart.

The 9 hundredths is greater than all of the other digits in the hundredths place. 8.79 is the largest number.

Decreasing order means I need to list the numbers from greatest to least.

4. Arrange the numbers in decreasing order.

56.128 56.12 56.19 56.182

This time I'll just visualize the place value chart in my head.

56.19, 56.182, 56.128, 56.12

I'll begin by comparing the largest units, tens, first. All of the numbers have 5 tens, 6 ones, and 1 tenth. I'll look to the hundredths place next to compare.

Even though this number has only 4 digits, it's actually the largest number. The 9 in the hundredths place is the largest of all the digits in the hundredths places.

When I compare 56.12 and 56.128 to the other numbers, I see that they both have the fewest number of hundredths. However, I know that 56.128 is larger because it has 8 thousandths more than 56.12.



a. 16.45		16.454
b. 0.83	0	83 100
C. $\frac{205}{1000}$	0	0.205
d. 95.045		95.545
e. 419.10		419.099
f. Five ones and eight tenths	0	Fifty-eight tenths
g. Thirty-six and nine thousandths	0	Four tens
h. One hundred four and twelve hundredths	0	One hundred four and two thousandths
i. One hundred fifty-eight thousandths	0	0.58
j. 703.005		Seven hundred three and five hundredths
rrange the numbers in increasing order		
8.08 8.081 8.09 8.008		

- 3. Arrange the numbers in decreasing order.
 - a. 8.508 8.58 7.5 7.058

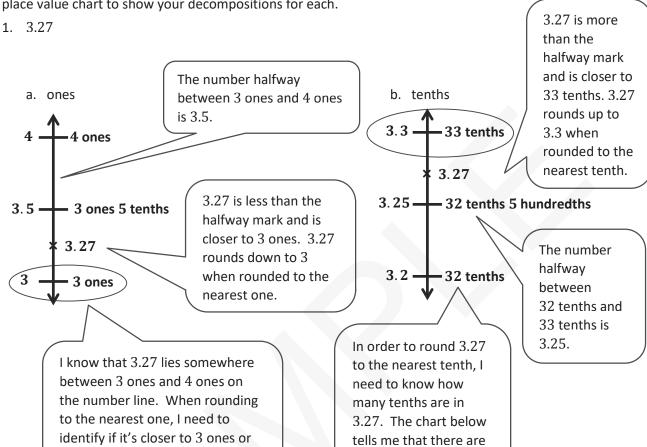
b. 439.216 439.126 439.612 439.261

4. James measured his hand. It was 0.17 meter. Jennifer measured her hand. It was 0.165 meter. Whose hand is bigger? How do you know?

5. In a paper airplane contest, Marcel's plane travels 3.345 meters. Salvador's plane travels 3.35 meters. Jennifer's plane travels 3.3 meters. Based on the measurements, whose plane traveled the farthest distance? Whose plane traveled the shortest distance? Explain your reasoning using a place value chart.



Round to the given place value. Label the number lines to show your work. Circle the rounded number. Use a place value chart to show your decompositions for each.



ones	tenths	hundredths
3	2	7
	32	7
		327

I can think of 3.27 in several ways. I can say it is 3 ones +2 tenths +7 hundredths. I can also think of it as 32 tenths +7 hundredths or 327 hundredths.

32 tenths in 3.27.

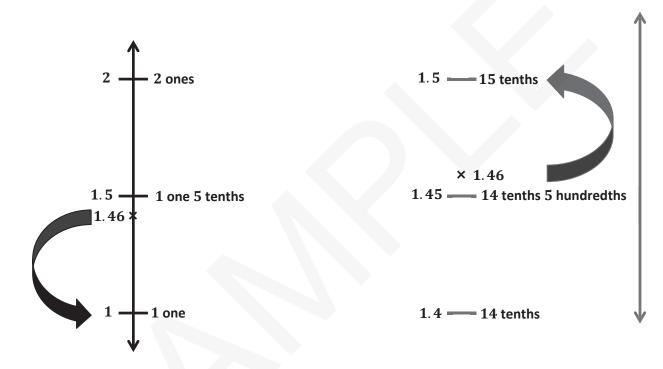


4 ones.

2. Rosie's pedometer said she walked 1.46 miles. She rounded her distance to 1 mile, and her brother, Isaac, rounded her distance to 1.5 miles. They are both right. Why?

Rosie rounded the distance to the nearest mile, and Isaac rounded the distance to the nearest tenth of a mile.

- 1.46 rounded to the nearest one is 1.
- 1.46 rounded to the nearest tenth is 15 tenths or 1.5.



Name	Date
Name	Date

Fill in the table, and then round to the given place. Label the number lines to show your work. Circle the rounded number.

- 1. 4.3
 - a. Hundredths
- b. Tenths
- c. Ones







Tens	Ones	Tenths	Hundredths	Thousandths
	`			

- 2. 225.286
 - a. Hundredths



b. Ones



Tens	Ones	Tenths	Hundredths	Thousandths

3. 8.984

Tens	Ones	Tenths	Hundredths	Thousandths

a. Hundredths

b. Tenths

c. Ones

d. Tens







- 4. On a Major League Baseball diamond, the distance from the pitcher's mound to home plate is 18.386 meters.
 - a. Round this number to the nearest hundredth of a meter. Use a number line to show your work.
 - b. How many centimeters is it from the pitcher's mound to home plate?
- 5. Jules reads that 1 pint is equivalent to 0.473 liters. He asks his teacher how many liters there are in a pint. His teacher responds that there are about 0.47 liters in a pint. He asks his parents, and they say there are about 0.5 liters in a pint. Jules says they are both correct. How can that be true? Explain your answer.

1. Round the quantity to the given place value. Draw number lines to explain your thinking. Circle the rounded value on the number line.

Round 23.245 to the nearest tenth and hundredth.

2 tens = 200 tenths

3 ones = 30 tenths

There are 232 tenths

4 hundredths 5 thousandths in

the number 23.245.

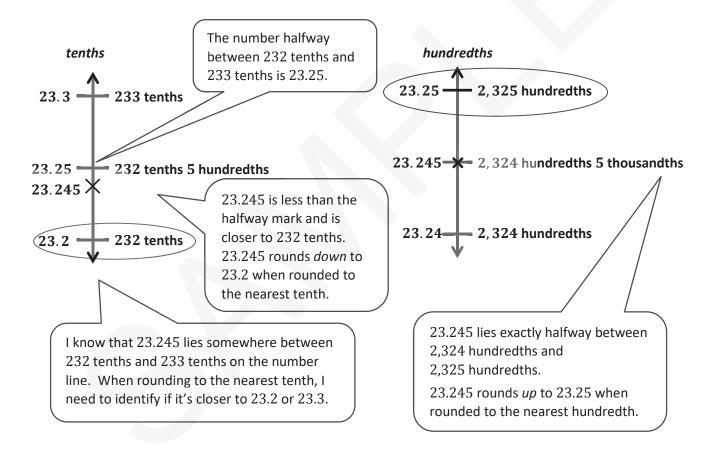
2 tens = 2,000 hundredths

3 ones = 300 hundredths

2 tenths = 20 hundredths

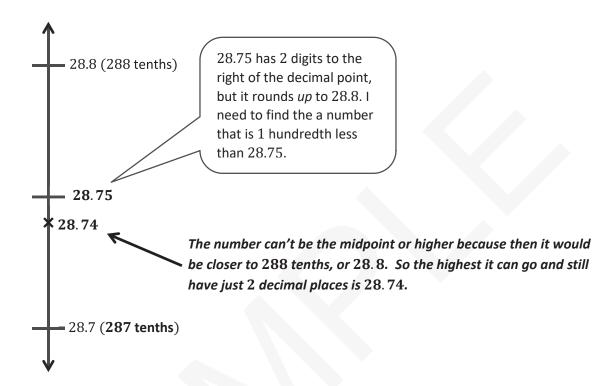
There are 2,324 hundredths

5 thousandths in the number 23.245.





2. A decimal number has two digits to the right of its decimal point. If we round it to the nearest tenth, the result is 28.7. What is the maximum possible value of this decimal? Use words and the number line to explain your reasoning.



Nar	ame Date	
	Write the decomposition that helps you, and then round to the given place value explain your thinking. Circle the rounded value on each number line.	. Draw number lines to

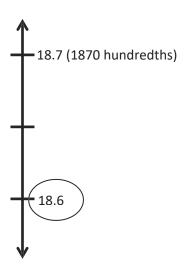
a. 43.586 to the nearest tenth, hundredth, and one.

b. 243.875 to nearest tenth, hundredth, ten, and hundred.

2. A trip from New York City to Seattle is 2,852.1 miles. A family wants to make the drive in 10 days, driving the same number of miles each day. About how many miles will they drive each day? Round your answer to the nearest tenth of a mile.



- 3. A decimal number has two digits to the right of its decimal point. If we round it to the nearest tenth, the result is 18.6.
 - a. What is the maximum possible value of this number? Use words and the number line to explain your reasoning. Include the midpoint on your number line.



b. What is the minimum possible value of this decimal? Use words, pictures, or numbers to explain your reasoning.



Note: Adding decimals is just like adding whole numbers—combine like units. Study the examples below:

- 2 apples + 3 apples = 5 apples
- 2 ones + 3 ones = 5 ones
- 2 tens + 3 tens = 5 tens = 50
- 2 hundredths + 3 hundredths = 5 hundredths = 0.05

1. Solve.

I'll combine the like units, tenths, to get 5 tenths.

a. $2 \text{ tenths} + 3 \text{ tenths} = \underline{} \text{ tenths}$

The standard form is 0.2 + 0.3 = 0.5.

I'll combine the like units, hundredths, and get 31 hundredths.

b. 26 hundredths + 5 hundredths = 31 hundredths = 3 tenths 1 hundredths

The standard form is 0.26 + 0.05 = 0.31.

- 10 hundredths = 1 tenth
- 20 hundredths = 2 tenths
- 30 hundredths = 3 tenths

I'll combine the like units and get 5 ones 6 tenths, which is the same as 56 tenths.

c. 5 ones 2 tenths + 4 tenths = tenths

1 one = 10 tenths

5 ones = 50 tenths

The standard form is 5.2 + 0.4 = 5.6.



- 2. Solve using the standard algorithm.
 - a. 0.3 + 0.91 = 1.21

3 tenths + 9 tenths is 12 tenths. I'll record 12 tenths as 1 one and

2 tenths.

b. 75.604 + 12.087 = 87.691

75.604

+ 12.087

87.691

When setting up the algorithm, I need to be sure to add like units. Therefore I'll line up the tens with the tens, the ones with the ones et cetera.

4 thousandths + 7 thousandths is

11 thousandths. I'll record

11 thousandths as 1 hundredth

1 thousandth.

3. Anthony spends \$6.49 on a book. He also buys a pencil for \$2.87 and an eraser for \$1.15. How much money does he spend altogether?

\$6.49 + \$2.87 + \$1.15 = \$10.51

I'll add all three items together to find the total price.

6.49

2.87

9 hundredths + 7 hundredths + 5 hundredths is 21 hundredths. I'll record 21 hundredths as 2 tenths 1 hundredth.

+1.15

10.51

 $4\ tenths+8\ tenths+1\ tenth+2\ tenths$ is $15\ tenths$. I'll record $15\ tenths$ as $1\ one$ and $5\ tenths$.

Anthony spends \$10.51.

Name				Date			
	Sol						
	a.	3 tenths + 4 tenths =	_ tenths				
	b.	12 tenths + 9 tenths =	tenths =	one(s)	tenth(s)		
	c.	3 hundredths + 4 hundredths =	hundredths				
	d.	27 hundredths + 7 hundredths =	hundredths =	tenths	hundredths		
	e.	4 thousandths + 3 thousandths = _	thousandt	hs			
	f.	39 thousandths + 5 thousandths =	thousandths =	_ hundredths	_ thousandths		
	g.	5 tenths + 7 thousandths =	thousandths				

thousandths

2. Solve using the standard algorithm.

h. 4 ones 4 tenths + 4 tenths = _____ tenths

i. 8 thousandths + 6 ones 8 thousandths = _

a. 0.4 + 0.7 =	b. 2.04 + 0.07 =
c. 6.4 + 3.7 =	d. 56.04 + 3.07 =

Lesson 9:

e. 72.564 + 5.137 =	f. 75.604 + 22.296 =

- 3. Walkway Over the Hudson, a bridge that crosses the Hudson River in Poughkeepsie, is 2.063 kilometers long. Anping Bridge, which was built in China 850 years ago, is 2.07 kilometers long.
 - a. What is the total span of both bridges? Show your thinking.

b. Leah likes to walk her dog on the Walkway Over the Hudson. If she walks across and back, how far will she and her dog walk?

4. For his parents' anniversary, Danny spends \$5.87 on a photo. He also buys a balloon for \$2.49 and a box of strawberries for \$4.50. How much money does he spend all together?



Note: Subtracting decimals is just like subtracting whole numbers—subtract like units. Study the examples below.

5 apples -1 apple = 4 apples

5 ones -1 one = 4 ones

5 tens - 1 ten = 4 tens

5 hundredths -1 hundredth = 4 hundredths

1. Subtract.

a. $7 \text{ tenths} - 4 \text{ tenths} = \frac{1}{2}$ tenths I'll subtract the like units, tenths, to get 3 tenths.

The standard form is 0.7 - 0.4 = 0.3.

I'll look at the units carefully.

A hundred is different than a hundredth.

I'll subtract 3 hundredths from 8 hundredths, and get 5 hundredths.

b. 4 hundreds 8 hundredths -3 hundredths =

hundreds

hundredths

The standard form is 400.08 - 0.03 = 400.05.

1.7 is the same as 1.70.

2. Solve 1.7 - 0.09 using the standard algorithm.

When setting up the algorithm, I need to be sure to subtract like units. Therefore, I'll line up the ones with the ones, the tenths with the tenths, etc.

6 10

1. 7

0. 0

There are 0 hundredths, so I can't subtract 9 hundredths. I'll rename 7 tenths as 6 tenths 10 hundredths.

10 hundredths minus 9 hundredths is equal to 1 hundredth.

6 ones 3 tenths = 6.3 = 6.3058 hundredths = 0.58

3. Solve 6 ones 3 tenths -58 hundredths.

There are 0 hundredths, so I can't subtract 8 hundredths. I'll rename 3 tenths as 2 tenths 10 hundredths.

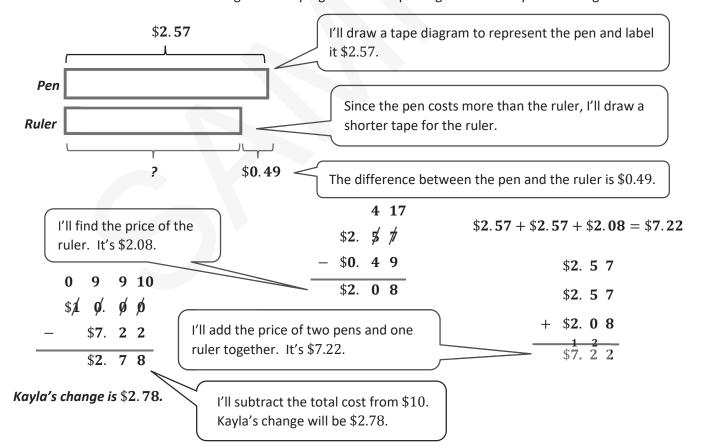
I'll rename 6 ones as 5 ones 10 tenths. 10 tenths, plus the 2 tenths already there, makes 12 tenths.

5 12 10 **6**. **3** 0. 5 8 5. 7

10 hundredths minus 8 hundredths is equal to 2 hundredths.

Students can solve using a variety of methods. This problem may not require the standard algorithm as some students can compute mentally.

4. A pen costs \$2.57. It costs \$0.49 more than a ruler. Kayla bought two pens and one ruler. She paid with a ten-dollar bill. How much change does Kayla get? Use a tape diagram to show your thinking.



44

Lesson 10: Subtract decimals using place value strategies, and relate those strategies to a written method.



Note: Encourage your child to use a variety of strategies when solving. The standard algorithm may not always be necessary for some students. Ask them about different ways to solve the problem. Below you'll find some alternate solution strategies that could be applied.

2.57 + 2.57 + 2.08 = 7.22

When finding the total cost of the 3 items, I can think of adding \$2.50 + \$2.50 + \$2, which is equal to \$7. Then I'll add the remaining 7¢ + 7¢ + 8¢, which is 22¢. The total then, is \$7 + \$0.22 = \$7.22. I can do all of this mentally!

Then when finding the amount of change Kayla gets, I can use another strategy to solve.

Instead of finding the difference of \$10 and \$7.22 using the subtraction algorithm, I can count up from \$7.22.

$$\$7.22 \xrightarrow{+3¢} \$7.25 \xrightarrow{+75¢} \$8.00 \xrightarrow{+\$2} \$10.00$$

3¢ more makes \$7.25.

3 quarters, or 75 cents, more makes \$8.

\$2 more makes \$10.

2 dollars, 3 quarters, and 3 pennies is \$2.78. That's what Kayla gets back.

Kayla gets \$2.78 back in change.





Name	Date	
_	<u>-</u>	

- 1. Subtract. You may use a place value chart.
 - a. 9 tenths 3 tenths = _____ tenths
 - b. 9 ones 2 thousandths 3 ones = _____ones _____thousandths
 - c. 4 hundreds 6 hundredths 3 hundredths = _____ hundreds ____ hundredths
 - d. 56 thousandths 23 thousandths = _____ thousandths = ____ hundredths ____ thousandths
- 2. Solve using the standard algorithm.

a. 1.8 – 0.9 =	b. 41.84 – 0.9 =	c. 341.84 – 21.92 =
d. 5.182 – 0.09 =	e. 50.416 – 4.25 =	f. 741 – 3.91 =

	lve

a.	30 tens – 3 tens 3 tenths	b.	5 – 16 tenths	c.	24 tenths – 1 one 3 tenths
d.	6 ones 7 hundredths – 2.3	e.	8.246 – 5 hundredths	f.	5 ones 3 tenths – 0.53

4. Mr. House wrote 8 tenths minus 5 hundredths on the board. Maggie said the answer is 3 hundredths because 8 minus 5 is 3. Is she correct? Explain.

5. A clipboard costs \$2.23. It costs \$0.58 more than a notebook. Lisa bought two clipboards and one notebook. She paid with a ten-dollar bill. How much change does Lisa get? Use a tape diagram to show your thinking.

hundreds to thousandths place value chart (from Lesson 7)





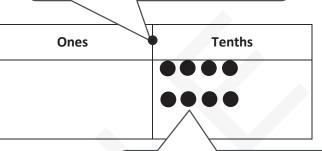
- 1. Solve by drawing disks on a place value chart. Write an equation, and express the product in standard form.
 - a. 2 copies of 4 tenths $= 2 \times 0.4$

= 0.8

multiply 2 times 4 tenths. The answer is 8 tenths, or 0.8.

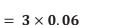
2 copies means 2 groups. So, I'll

I'll draw a place value chart to help me solve, and this dot is the decimal point.



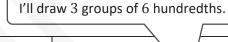
Each dot represents 1 tenth, so I'll draw 2 groups of 4 tenths.

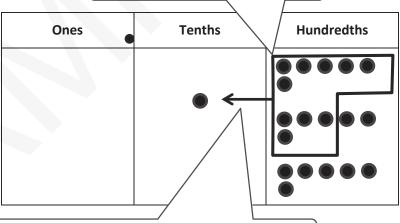
b. 3 times as much as 6 hundredths



= 0.18

I'll multiply 3 times 6 hundredths. The answer is 18 hundredths, or 0.18.



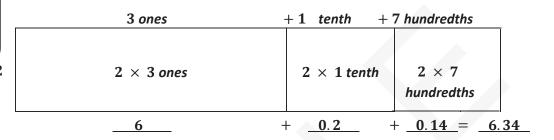


I'll bundle 10 hundredths and exchange them for 1 tenth.

- 2. Draw an area model, and find the sum of the partial products to evaluate each expression.
 - 3.17 is the same as 3 ones 1 tenth 7 hundredths. a. 2×3.17

The factor 2 represents the width of the area model.

The factor 3.17 represents the length of the area model.



I'll multiply 2 times each place value unit.

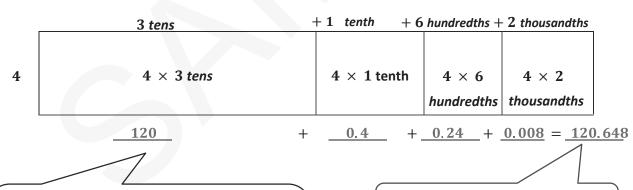
$$2 \times 3$$
 ones = 6 ones = 6

$$2 \times 1$$
 tenth = 2 tenths = 0.2

$$2 \times 7$$
 hundredths = 14 hundredths = 0.14

The product of 2 and 3.17 is 6.34.

There are 0 ones in 30.162, so my area model does not b. 4 times as much as 30.162 include the ones.



I'll multiply 4 times each place value unit.

$$4 \times 3 \text{ tens} = 12 \text{ tens} = 120$$

$$4 \times 1$$
 tenth = 4 tenths = 0.4

$$4 \times 2$$
 thousandths = 8 thousandths = 0.008

The product of 4 and 30.162 is 120.648.



Na	me						Date	
1.	Sol for	ve by drawing disks om.	on a place val	lue chart.	Write an	equation	n, and express the pr	roduct in standard
	a.	2 copies of 4 tenths			b.	4 groups	s of 5 hundredths	
	C.	4 times 7 tenths			d.	3 times !	5 hundredths	
	e.	9 times as much as	7 tenths		f.	6 thousa	ndths times 8	
2.	Dra	aw a model similar to	the one nict	ured held	w Find t	he sum o	f the partial product	rs to evaluate each
		pression.	and one piec			54111 0	partial product	e is craidate caell
	a.	4 × 6.79	6 ones	+	7 tenths	+	9 hundredths	1

 4×7 tenths

4 × 9 hundredths

 4×6 ones

- b. 6×7.49
- c. 9 copies of 3.65

d. 3 times 20.175

3. Leanne multiplied 8×4.3 and got 32.24. Is Leanne correct? Use an area model to explain your answer.

4. Anna buys groceries for her family. Hamburger meat is \$3.38 per pound, sweet potatoes are \$0.79 each, and hamburger rolls are \$2.30 a bag. If Anna buys 3 pounds of meat, 5 sweet potatoes, and 1 bag of hamburger rolls, what will she pay in all for the groceries?



1. Choose the reasonable product for each expression. Explain your thinking in the spaces below using words, pictures, or numbers.

a. 3.1×3 930 93 0.93

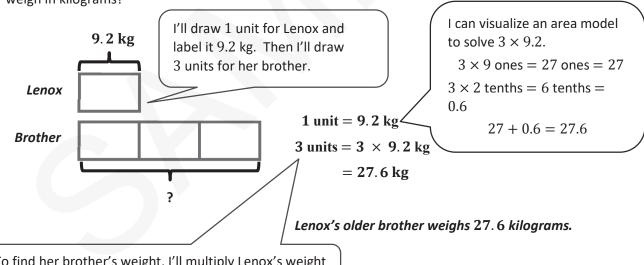
3.1 is just a little more than 3. A reasonable product would be just a little more than 9.

 $3 \times 3 = 9$. I looked for a product that was close to 9.



 $8 \times 7 = 56$. I looked for a product that was close to 56.

2. Lenox weighs 9.2 kg. Her older brother is 3 times as heavy as Lenox. How much does her older brother weigh in kilograms?



To find her brother's weight, I'll multiply Lenox's weight by 3. The answer is 27.6 kilograms.



Date _____

Name _____

1.	. Choose the reasonable product for each expression. Explain your thinking in the spaces below words, pictures, or numbers.					es below using
	a.	2.1 × 3	0.63	6.3	63	630
	b.	4.27 × 6	2562	256.2	25.62	2.562
	C.	7 × 6.053	4237.1	423.71	42.371	4.2371

4.338



d.

 9×4.82

43.38

433.8

4338

Lesson 12:

2.	Yi Ting weighs 8.3 kg.	Her older brother	is 4 times as he	avy as Yi Ting.	How much does her	older brother
	weigh in kilograms?					

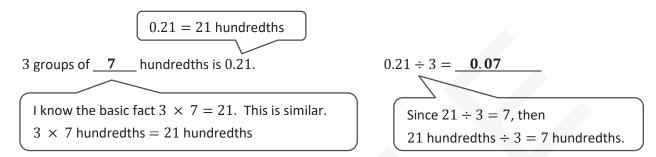
3. Tim is painting his storage shed. He buys 4 gallons of white paint and 3 gallons of blue paint. Each gallon of white paint costs \$15.72, and each gallon of blue paint is \$21.87. How much will Tim spend in all on paint?

4. Ribbon is sold at 3 yards for \$6.33. Jackie bought 24 yards of ribbon for a project. How much did she pay?

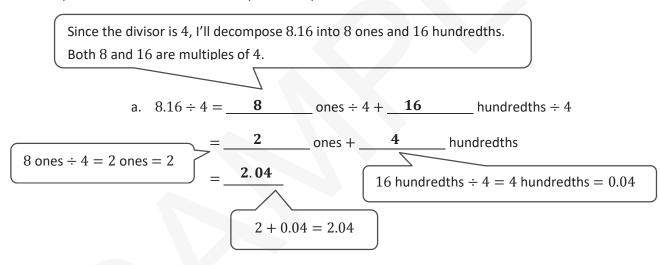


Note: The use of unit language (e.g., 21 hundredths rather than 0.21) allows students to use knowledge of basic facts to compute easily with decimals.

1. Complete the sentence with the correct number of units, and then complete the equation.



2. Complete the number sentence. Express the quotient in units and then in standard form.



Since the divisor is 6, I'll decompose 1.242 into 12 tenths and 42 thousandths. Both 12 and 42 are multiples of 6.

b.
$$1.242 \div 6 = \underbrace{ (12 \text{ tenths} \div 6) + (42 \text{ thousandths} \div 6)}_{= \underbrace{ 2 \text{ tenths} + 7 \text{ thousandths}}_{= \underbrace{ 0.207}_{= \underbrace{ 42 \text{ thousandths} \div 6 = 7 \text{ thousandths} = 0.007}_{= \underbrace{ 0.207}_{= \underbrace{ 42 \text{ thousandths} \div 6 = 7 \text{ thousandths} = 0.007}_{= \underbrace{ 0.207}_{= \underbrace{ 42 \text{ thousandths} \div 6 = 7 \text{ thousandths} = 0.007}_{= \underbrace{ 0.207}_{= \underbrace{ 0.2$$



Lesson 13: Divide decimals by single-digit whole numbers involving easily identifiable multiples using place value understanding and relate to a written method

3. Find the quotients. Then, use words, numbers, or pictures to describe any relationships you notice between the pair of problems and their quotients.

a.
$$35 \div 5 = 7$$

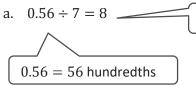
I know this basic fact!

b. $3.5 \div 5 =$ I can use that basic fact to help me solve this one.

 $35 \text{ tenths} \div 5 = 7 \text{ tenths} = 0.7$

Both problems are dividing by 5, but the quotient for part (a) is 10 times larger than the quotient for (b). That makes sense because the number we started with in part (a) is also 10 times larger than the number we started with in part (b).

4. Is the quotient below reasonable? Explain your answer.



56 hundredths \div 7 = 8 hundredths

No, the quotient is not reasonable.

 $56 \div 7 = 8$, so 56 hundredths $\div 7$ must be 8 hundredths.

5. A toy airplane weighs 3.69 kg. It weighs 3 times as much as a toy car. What is the weight of the toy car?

I draw 1 tape diagram to show the weight of the airplane. 3.69 kgThe airplane airplane weighs 3 times as much as the car car, so I partition the tape diagram, into 3 equal The car is equal units. to the weight of 1 unit.

I can use unit language and basic facts to solve.

$$3 \text{ ones} \div 3 = 1 \text{ one}$$

$$6 \text{ tenths} \div 3 = 2 \text{ tenths} = 0.2$$

9 hundredths
$$\div$$
 3 = 3 hundredths = 0.03

3 units = 3.69

$$1\,\text{unit} = 3.69 \div 3$$

1 unit = 1.23

The toy car weighs 1.23 kg.

60

Name	Date
Name	Date

- 1. Complete the sentences with the correct number of units, and then complete the equation.
 - a. 3 groups of _____ tenths is 1.5.

- 1.5 ÷ 3 =
- b. 6 groups of _____ hundredths is 0.24.
- $0.24 \div 6 = _{--}$
- c. 5 groups of _____ thousandths is 0.045.
- 2. Complete the number sentence. Express the quotient in units and then in standard form.
 - a. $9.36 \div 3 =$ _____ ones $\div 3 +$ _____ hundredths $\div 3$

= _____ ones + _____ hundredths

b. 36.012 ÷ 3 = _____ ones ÷ 3 + ____ thousandths ÷ 3

= _____ ones + _____ thousandths

c. $3.55 \div 5 =$ _____ tenths $\div 5 +$ _____ hundredths $\div 5$

d. 3.545 ÷ 5 = _____



3. Find the quotients. Then, use words, numbers, or pictures to describe any relationships you notice between each pair of problems and quotients.

a. 21 ÷ 7 = _____

2.1 ÷ 7 = _____

b. 48 ÷ 8 = _____

 $0.048 \div 8 =$

4. Are the quotients below reasonable? Explain your answers.

a. $0.54 \div 6 = 9$

b. $5.4 \div 6 = 0.9$

c. $54 \div 6 = 0.09$

5.	A toy airplane costs \$4.84.	It costs 4 times as much as a toy car.	What is the cost of the tov car?

6. Julian bought 3.9 liters of cranberry juice, and Jay bought 8.74 liters of apple juice. They mixed the two juices together and then poured them equally into 2 bottles. How many liters of juice are in each bottle?

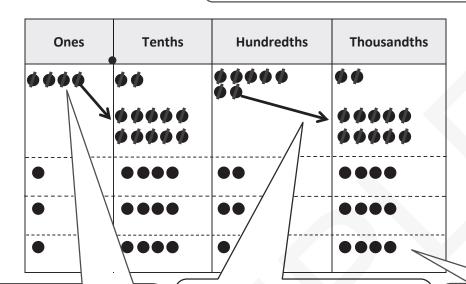




1. Draw place value disks on the place value chart to solve. Show each step using the standard algorithm.

$$4.272 \div 3 = 1.424$$

4.272 is divided into 3 equal groups. There is 1.424 in each group.



2 2

When I share 4 ones equally with 3 groups, there is 1 one in each group and 1 one remaining.

In order to continue sharing, or dividing, I'll exchange the 1 remaining hundredth for 10 thousandths.

In each group, there is 1 one 4 tenths 2 hundredths 4 thousandths, or 1.424.

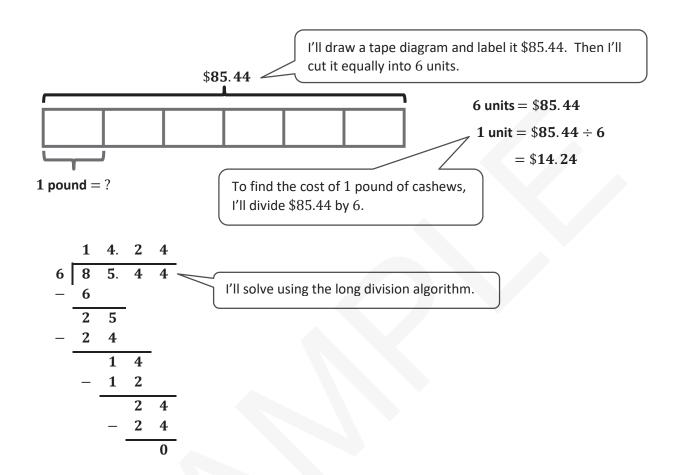
2. Solve $15.704 \div 4$ using the standard algorithm.

15.704 is divided into 4 equal groups. There is 3.926 in each group.

As I work, I'm visualizing the place value chart and thinking out loud. "We had 15 ones and shared 12 of them. 3 ones remain. I can change those 3 ones for 30 tenths, which combined with the 7 tenths in the whole, makes 37 tenths. Now I need to share 37 tenths equally with 4 groups. Each group gets 9 tenths."

When completing the division, I need to be sure to line up the place value units carefully—the tens with the tens, the ones with the ones, etc.

3. Mr. Huynh paid \$85.44 for 6 pounds of cashews. What's the cost of 1 pound of cashews?



The cost of 1 pound of cashews is \$14.24.

Name	Date
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- 1. Draw place value disks on the place value chart to solve. Show each step using the standard algorithm.
 - a. 5.241 ÷ 3 = _____

Ones	Tenths	Hundredths	Thousandths

b. 5.372 ÷ 4 = _____

Ones	Tenths	Hundredths	Thousandths

4 5. 3 7 2

2. Solve using the standard algorithm.

a. 0.64 ÷ 4 = _____

b. 6.45 ÷ 5 = _____

c. 16.404 ÷ 6 = _____

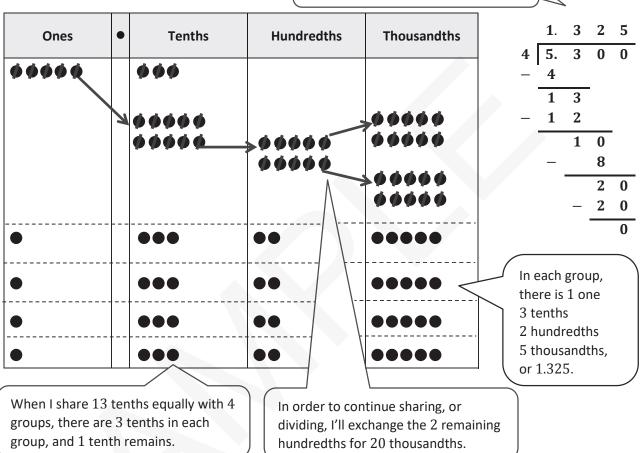
3. Mrs. Mayuko paid \$40.68 for 3 kg of shrimp. What's the cost of 1 kilogram of shrimp?

4. The total weight of 6 pieces of butter and a bag of sugar is 3.8 lb. If the weight of the bag of sugar is 1.4 lb, what is the weight of each piece of butter?

1. Draw place value disks on the place value chart to solve. Show each step in the standard algorithm.

$$5.3 \div 4 = 1.325$$

5.3 is divided into 4 equal groups There is 1.325 in each group.



2. Solve using the standard algorithm.

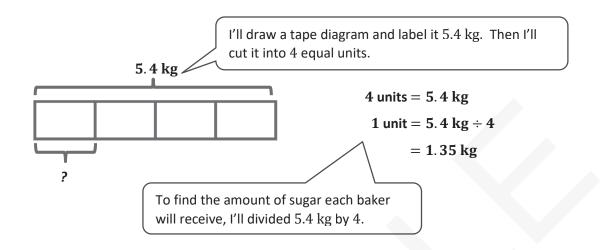
$$9 \div 5 = 1.8$$
0 is divided into 5 equal

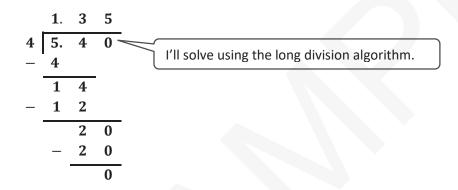
$$9\ \mbox{is divided into}\ 5\ \mbox{equal}$$
 groups. There is $1.8\ \mbox{in each}$ group.

In order to continue dividing, I'll rename the 4 remaining ones as 40 tenths.

 $40 \text{ tenths} \div 5 = 8 \text{ tenths}$

3. Four bakers shared 5.4 kilograms of sugar equally. How much sugar did they each receive?





Each baker received 1.35 kilograms of sugar.

Name	Date

- 1. Draw place value disks on the place value chart to solve. Show each step in the standard algorithm.
 - a. 0.7 ÷ 4 = _____

Ones	•	Tenths	Hundredths	Thousandths

b. 8.1 ÷ 5 = _____

Ones	•	Tenths	Hundredths	Thousandths

5 8.1



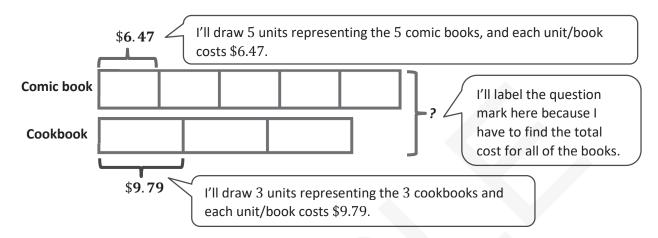
2. Solve using the standard algorithm.

a. 0.7 ÷ 2 =	b. 3.9 ÷ 6 =	c. 9 ÷ 4 =
d. 0.92 ÷ 2 =	e. 9.4 ÷ 4 =	f. 91 ÷ 8 =

3. A rope 8.7 meters long is cut into 5 equal pieces. How long is each piece?

4. Yasmine bought 6 gallons of apple juice. After filling up 4 bottles of the same size with apple juice, she had 0.3 gallon of apple juice left. How many gallons of apple juice are in each container?

- 1. A comic book costs \$6.47, and a cookbook costs \$9.79.
 - a. Zion buys 5 comic books and 3 cookbooks. What is the total cost for all of the books?



Comic book:

$$1 \text{ unit} = \$6.47$$

5 units =
$$5 \times \$6.47 = \$32.35$$

I'll find the total cost of the 5 comic books by multiplying 5 times \$6.47.

+4 tenths +7 hundredths 6 ones 5×4 5×7 5 5×6 ones tenths hundredths

30 ones
$$+$$
 20 tenths $+$ 35 hundredths $=$ 32.35

Cookbook:

$$1 \text{ unit} = \$9.79$$

$$3 \text{ units} = 3 \times \$9.79 = \$29.37$$

I'll find the total cost of the 3 cookbooks by multiplying 3 times \$9.79.

9 ones

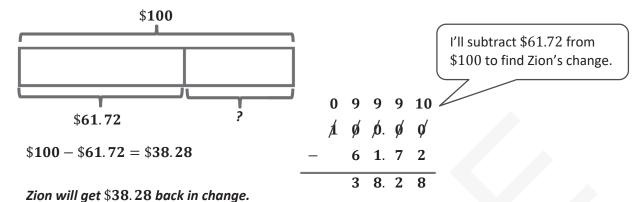
27 ones + 21 tenths + 27 hundredths = 29.37

+ 7 tenths + 9 hundredths

I'll add the total cost of 5 comic books and the total cost of 3 cookbooks together to find the total cost of all 8 books.

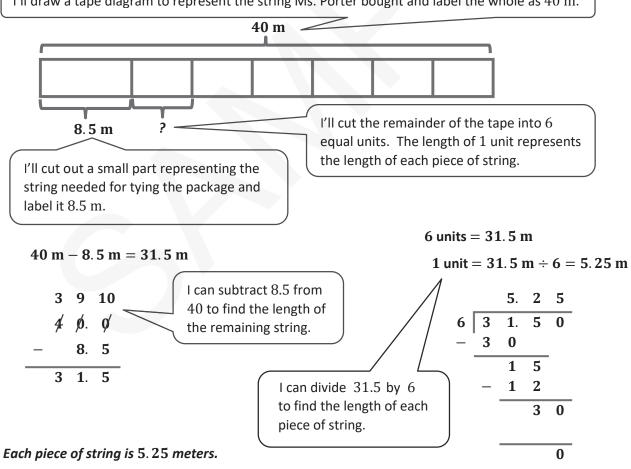


Lesson 16: Solve word problems using decimal operations. b. Zion wants to pay for the all the books with a \$100 bill. How much change will he get back?



2. Ms. Porter bought 40 meters of string. She used 8.5 meters to tie a package. Then she cuts the remainder into 6 equal pieces. Find the length of each piece. Give the answer in meters.

I'll draw a tape diagram to represent the string Ms. Porter bought and label the whole as 40 m.



Naı	me .	Date			
Sol	Solve using tape diagrams.				
1.	9.5	ardener installed 42.6 meters of fencing in a week. He installed 13.45 meters on Monday and meters on Tuesday. He installed the rest of the fence in equal lengths on Wednesday through Friday. It was many meters of fencing did he install on each of the last three days?			
2.	Jen	ny charges \$9.15 an hour to babysit toddlers and \$7.45 an hour to babysit school-aged children.			
	a.	If Jenny babysat toddlers for 9 hours and school-aged children for 6 hours, how much money did she earn in all?			
	b.	Jenny wants to earn \$1,300 by the end of the summer. How much more will she need to earn to meet her goal?			



3. A table and 8 chairs weigh 235.68 lb together. If the table weighs 157.84 lb, what is the weight of one chair in pounds?

4. Mrs. Cleaver mixes 1.24 liters of red paint with 3 times as much blue paint to make purple paint. She pours the paint equally into 5 containers. How much blue paint is in each container? Give your answer in liters.