

County: Any

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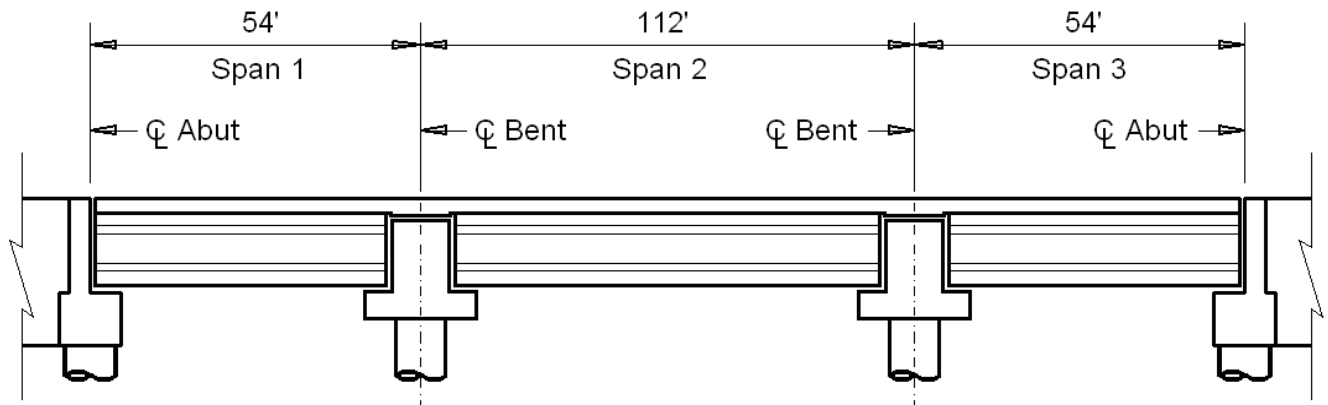
Design: BRG

Date: 6/2010

Inverted Tee Bent Cap Design Example

Design example is in accordance with the AASHTO LRFD Bridge Design Specifications, 5th Ed. (2010) as prescribed by TxDOT Bridge Design Manual - LRFD (May 2009).

Design Parameters



Span 1

54' Type TX54 Girders ($0.851 k/ft$)
 6 Girders Spaced @ 8.00' with 3' overhangs
 2" Haunch

Span 2

112' Type TX54 Girders ($0.851 k/ft$)
 6 Girders Spaced @ 8.00' with 3' overhangs
 3.75" Haunch

Span 3

54' Type TX54 Girders ($0.851 k/ft$)
 6 Girders Spaced @ 8.00' with 3' overhangs
 2" Haunch

All Spans

Deck is 46ft wide
 Type T551 Rail ($0.382k/ft$)
 8" Thick Slab ($0.100 ksf$)
 Assume 2" Overlay @ 140 pcf ($0.023 ksf$)
 Use Class "C" Concrete
 $f'_c = 3.60$ ksi
 $w_c = 150$ pcf (for weight)
 $w_c = 145$ pcf (for Modulus of Elasticity calculation)
 Grade 60 Reinforcing
 $F_y = 60$ ksi

"AASHTO LRFD" refers to the AASHTO LRFD Bridge Design Specification, 5th Ed. (2010)

"BDM-LRFD" refers to the TxDOT Bridge Design Manual - LRFD (May 2009)

"TxSP" refers to TxDOT guidance, recommendations, and standard practice.

"Furlong & Mirza" refers to "Strength and Servicability of Inverted T-Beam Bent Caps Subject to Combined Flexure, Shear, and Torsion", Center for Highway Research Report No. 153-1F, The University of Texas at Austin, August 1974

The basic bridge geometry can be found on the Bridge Layout located in the Appendices.

(TxSP)

(BDM-LRFD, Ch. 4, Sect. 5, Materials)

(BDM-LRFD, Ch. 4, Sect. 5, Materials)

Bents

Use 36" Diameter Columns (Typical for Type TX54 Girders)

Design Parameters (Con't)

Define Variables

Back Span

$$\text{Span1} = 54\text{ft}$$

$$\text{GdrSpa1} = 8\text{ft}$$

$$\text{GdrNo1} = 6$$

$$\text{GdrWt1} = 0.851\text{klf}$$

$$\text{Haunch1} = 2\text{in}$$

Forward Span

$$\text{Span2} = 112\text{ft}$$

$$\text{GdrSpa2} = 8\text{ft}$$

$$\text{GdrNo2} = 6$$

$$\text{GdrWt2} = 0.851\text{klf}$$

$$\text{Haunch2} = 3.75\text{in}$$

Span Length

Girder Spacing

Number of Girders in Span

Weight of Girder

Size of Haunch

Bridge

$$\text{Skew} = 0\text{deg}$$

$$\text{BridgeW} = 46\text{ft}$$

$$\text{RdwyW} = 44\text{ft}$$

$$\text{GirderD} = 54\text{in}$$

$$\text{BrgSeat} = 1.5\text{in}$$

$$\text{BrgPad} = 2.75\text{in}$$

$$\text{SlabThk} = 8\text{in}$$

$$\text{OverlayThk} = 2\text{in}$$

$$\text{RailWt} = 0.382\text{klf}$$

$$w_c = 0.150\text{kcf}$$

$$W_{\text{Olay}} = 0.140\text{kcf}$$

Skew of Bents

Width of Bridge Deck

Width of Roadway

Depth of Type TX54 Girder

Bearing Seat Buildup

Bearing Pad Thickness

Thickness of Bridge Slab

Thickness of Overlay

Weight of Rail

Unit Weight of Concrete for Loads

Unit Weight of Overlay

Bents

$$f_c = 3.60\text{ksi}$$

$$w_{cE} = 0.145\text{kcf}$$

$$E_c = 33,000 \cdot w_{cE}^{1.5} \cdot \sqrt{f_c}$$

$$E_c = 3457 \cdot \text{ksi}$$

Concrete Strength

Unit Weight of Concrete for E_c

Modulus of Elasticity of Concrete, (AASHTO LRFD Eq. 5.4.2.4-1)

Yield Strength of reinforcement

Modulus of Elasticity of Steel

Diameter of Columns

$$f_y = 60\text{ksi}$$

$$E_s = 29000\text{ksi}$$

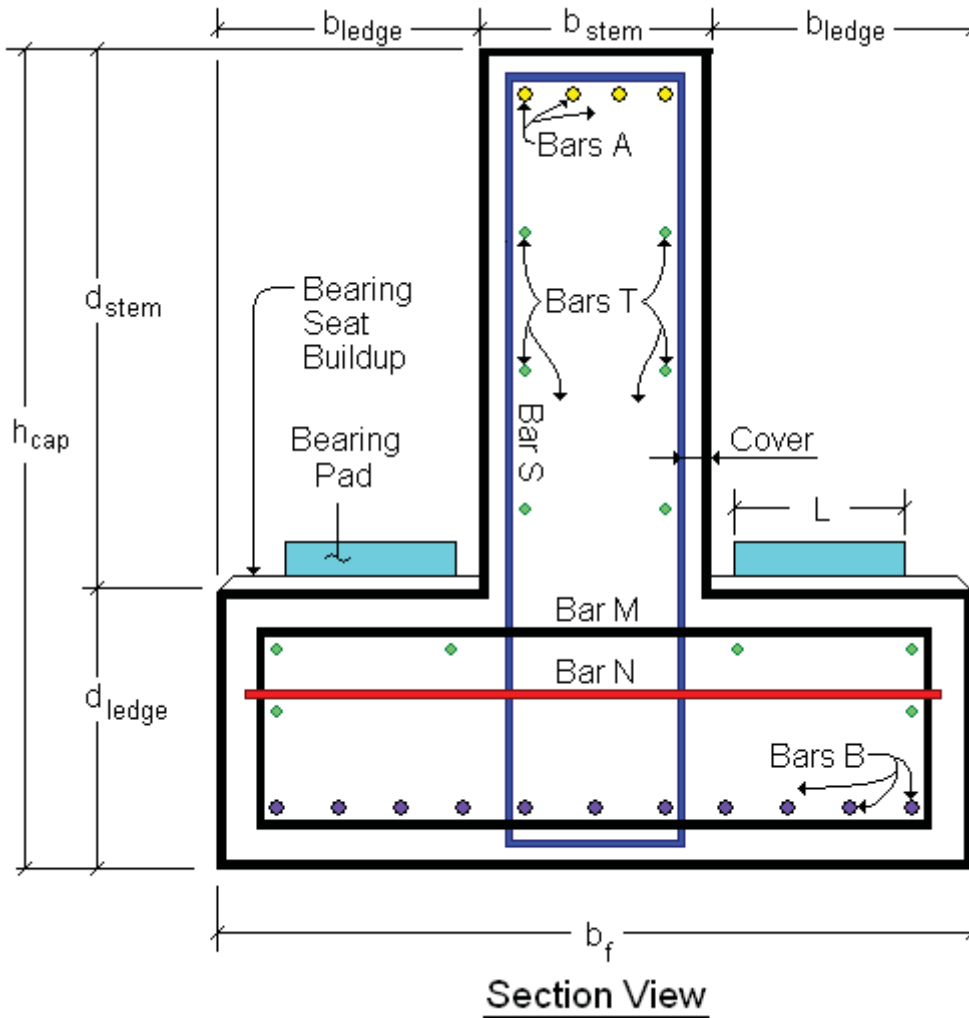
$$D_{\text{column}} = 36\text{in}$$

Other Variables

$$\text{IM} = 33\%$$

Dynamic load allowance, (AASHTO LRFD Table 3.6.2.1-1)

Determine Cap Dimensions



Stem Width

$$b_{\text{stem}} = D_{\text{column}} + 3\text{in}$$

$$b_{\text{stem}} = 39 \cdot \text{in}$$

The stem is typically at least 3" wider than the Diameter of the Column (36") to allow for the extension of the column reinforcement into the Cap. (TxSP)

Stem Height

Distance From Top of Slab to Top of Ledge

$$D_{\text{Slab_to_Ledge}} = \text{SlabThk} + \text{Haunch2} + \text{GirderD} + \text{BrgPad} + \text{BrgSeat}$$

Haunch 2 is the larger of the two haunches.

$$D_{\text{Slab_to_Ledge}} = 70.00 \cdot \text{in}$$

$$\text{StemHaunch} = 3.75 \cdot \text{in}$$

The top of the stem must be 2.5" below the bottom of the slab. (BDM-LRFD, Ch. 4, Sect. 5, Geometric Constraints)
Accounting for the 1/2" of bituminous fiber, the top of the stem must have at least 2" of haunch on it, but the haunch should not be less than either of the haunches of the adjacent spans.

$$d_{\text{stem}} = D_{\text{Slab_to_Ledge}} - \text{SlabThk} - \text{StemHaunch} - 0.5\text{in}$$

The stem must accommodate 1/2" of bituminous fiber.

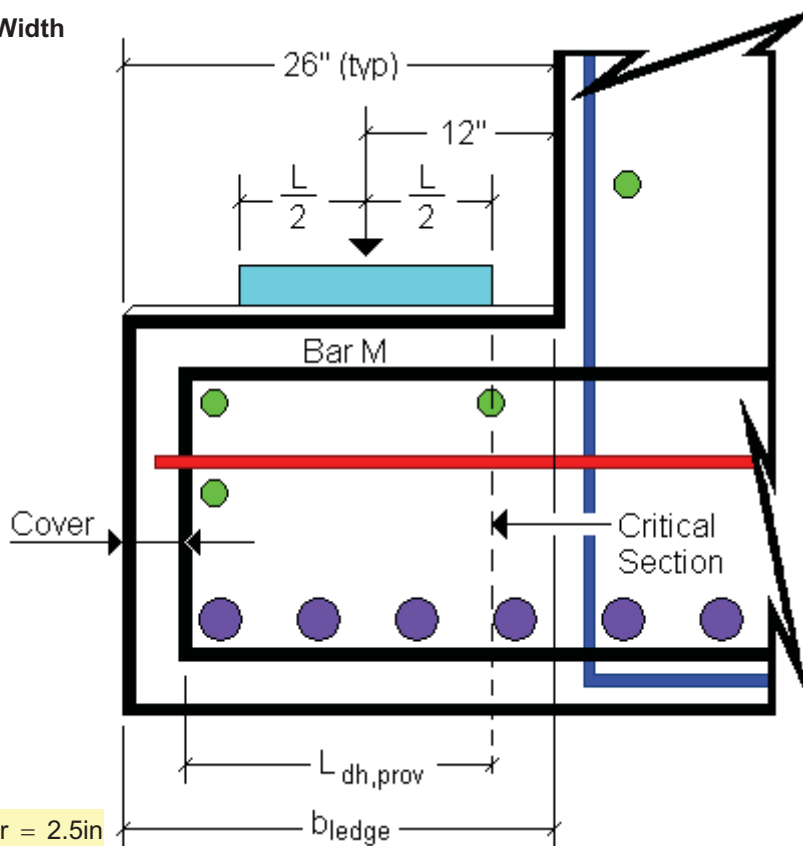
$$d_{\text{stem}} = 57.75 \cdot \text{in}$$

Use: $d_{\text{stem}} = 57 \cdot \text{in}$

Round the Stem Height down to the nearest 1". (TxSP)

Determine Cap Dimensions (Con't)

Ledge Width



cover = 2.5in

L = 8in

The Ledge Width must be adequate for Bar M to develop fully. 26" is typically used for TX54 girders, as it is adequate to develop a # 6 bar with the typical 2.5" cover. If the cover is increased to 3", allowing for a modification factor of 0.7, a 24" Ledge is adequate to develop a # 7 bar.

I-Beams have 9.5" from the face of the cap to the CL of Bearing. The typical ledge width for these bridges is 23".

" $L_{dh,prov}$ " must be greater than or equal to " $L_{dh,req}$ " for bar M.

"cover" is measured from the center of the transverse bars.

"L" is the length of the Bearing Pad along the girder. A typical type TX54 bearing pad is 8"x21" as shown in the IGEB standard.

Determine the Required Development Length of Bar M:

Try # 6 Bar for Bar M.

$$d_{bar_M} = 0.750in$$

$$A_{bar_M} = 0.44in^2$$

Basic Development Length

$$L_{dh} = \frac{38.0 \cdot d_{bar_M}}{\sqrt{f_c}}$$

$$L_{dh} = 15.02 \cdot in \quad (\text{AASHTO LRFD Eq. 5.11.2.4.1-1})$$

Modification Factors for L_{dh} :

(AASHTO LRFD 5.11.2.4.2)

Is Top Cover greater than or equal to 2.5", and Side Cover greater than or equal to 2"?

$$\text{SideCover} = \text{cover} - \frac{d_{bar_M}}{2}$$

$$\text{SideCover} = 2.13 \cdot in$$

"Side Cover" and "Top Cover" are the clear cover on the side and top of the hook respectively. The dimension "cover" is measured from the center of Bar M.

$$\text{TopCover} = \text{cover} - \frac{d_{bar_M}}{2}$$

$$\text{TopCover} = 2.13 \cdot in$$

No, Factor = 1.0

Determine Cap Dimensions (Con't)

The Required Development Length is the larger of the following:

(AASHTO LRFD 5.11.2.4.1)

$$L_{dh} \cdot \text{Factor} = 15.02 \cdot \text{in}$$

$$8 \cdot d_{\text{bar}_M} = 6.00 \cdot \text{in}$$

$$6 \text{in}$$

Therefore,

$$L_{dh_req} = 15.02 \cdot \text{in}$$

$$b_{\text{ledge_min}} = L_{dh_req} + \text{cover} + 12 \text{in} - \frac{L}{2}$$

$$b_{\text{ledge_min}} = 25.52 \cdot \text{in}$$

The distance from the face of the stem to the center of bearing is 12" for TxGirders. (IGEB)

Use:

$$b_{\text{ledge}} = 26 \cdot \text{in}$$

Width of Bottom Flange

$$b_f = 2 \cdot b_{\text{ledge}} + b_{\text{stem}}$$

$$b_f = 91 \cdot \text{in}$$

Ledge Depth

Use a Ledge Depth of 28"

$$d_{\text{ledge}} = 28 \text{in}$$

As a general rule of thumb Ledge Depth is greater than or equal to 2'-3". This is the depth at which a bent from a typical bridge will pass the punching shear check (calculations found on Pg. 21).

Total Depth of Cap

$$h_{\text{cap}} = d_{\text{stem}} + d_{\text{ledge}}$$

$$h_{\text{cap}} = 85 \cdot \text{in}$$

Summary of Cross Sectional Dimensions

$$b_{\text{stem}} = 39 \cdot \text{in}$$

From Pg. 3

$$d_{\text{stem}} = 57 \cdot \text{in}$$

From Pg. 3

$$b_{\text{ledge}} = 26 \cdot \text{in}$$

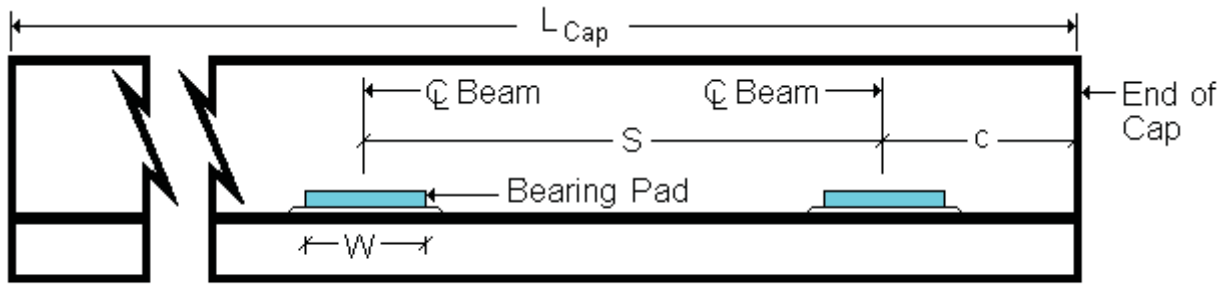
$$d_{\text{ledge}} = 28 \cdot \text{in}$$

$$h_{\text{cap}} = 85 \cdot \text{in}$$

Determine Cap Dimensions (Con't)

Length of Cap

First define Girder Spacing and End Distance:



$$S = 8\text{ft}$$

$$c = 2\text{ft}$$

$$L_{\text{Cap}} = S \cdot (\text{GdrNo}1 - 1) + 2 \cdot c$$

$$L_{\text{Cap}} = 44\text{ft}$$

Girder Spacing

"c" is the distance from the Center Line of the Exterior Girder to the Edge of the Cap measured along the Cap.

Length of Cap

TxDOT policy is as follows, "The edge distance between the exterior bearing pad and the end of the inverted T-beam shall not be less than 12in." (BDM-LRFD, Ch. 4, Sect. 5, Design Criteria) replacing the statement in AASHTO LRFD 5.13.2.5.5 stating it shall not be less than d_f . Preferably, the stem should extend at least 3" beyond the edge of the bearing seat.

Bearing Pad Dimensions

$$L = 8 \cdot \text{in}$$

$$W = 21 \cdot \text{in}$$

(IGEB standard)

Length of Bearing Pad

Width of Bearing Pad

Cross Sectional Properties of Cap

$$A_g = d_{\text{ledge}} \cdot b_f + d_{\text{stem}} \cdot b_{\text{stem}}$$

$$A_g = 4771 \cdot \text{in}^2$$

$$y_{\text{bar}} = \frac{d_{\text{ledge}} \cdot b_f \cdot \left(\frac{1}{2} \cdot d_{\text{ledge}}\right) + d_{\text{stem}} \cdot b_{\text{stem}} \cdot \left(d_{\text{ledge}} + \frac{1}{2} \cdot d_{\text{stem}}\right)}{A_g}$$

Distance from bottom of cap to the center of gravity of the cap

$$y_{\text{bar}} = 33.80 \cdot \text{in}$$

$$I_g = \frac{b_f \cdot d_{\text{ledge}}^3}{12} + b_f \cdot d_{\text{ledge}} \cdot \left(y_{\text{bar}} - \frac{1}{2} \cdot d_{\text{ledge}}\right)^2 + \frac{b_{\text{stem}} \cdot d_{\text{stem}}^3}{12} + b_{\text{stem}} \cdot d_{\text{stem}} \cdot \left[y_{\text{bar}} - \left(d_{\text{ledge}} + \frac{1}{2} \cdot d_{\text{stem}}\right)\right]^2$$

$$I_g = 2.91 \times 10^6 \cdot \text{in}^4$$

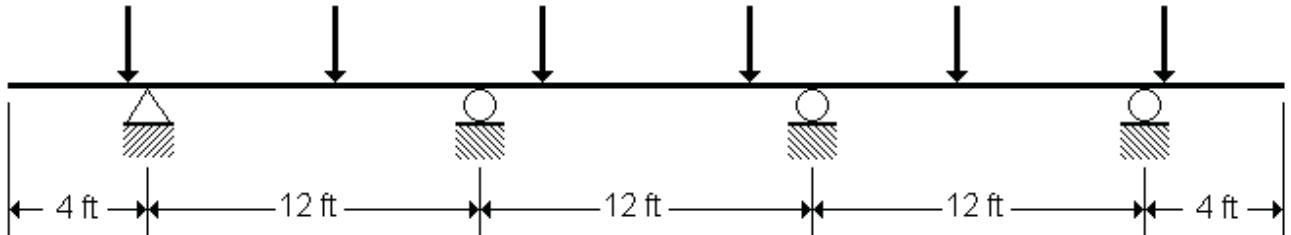
Cap Analysis

Cap Model

Assume:

4 Columns Spaced @ 12'-0"

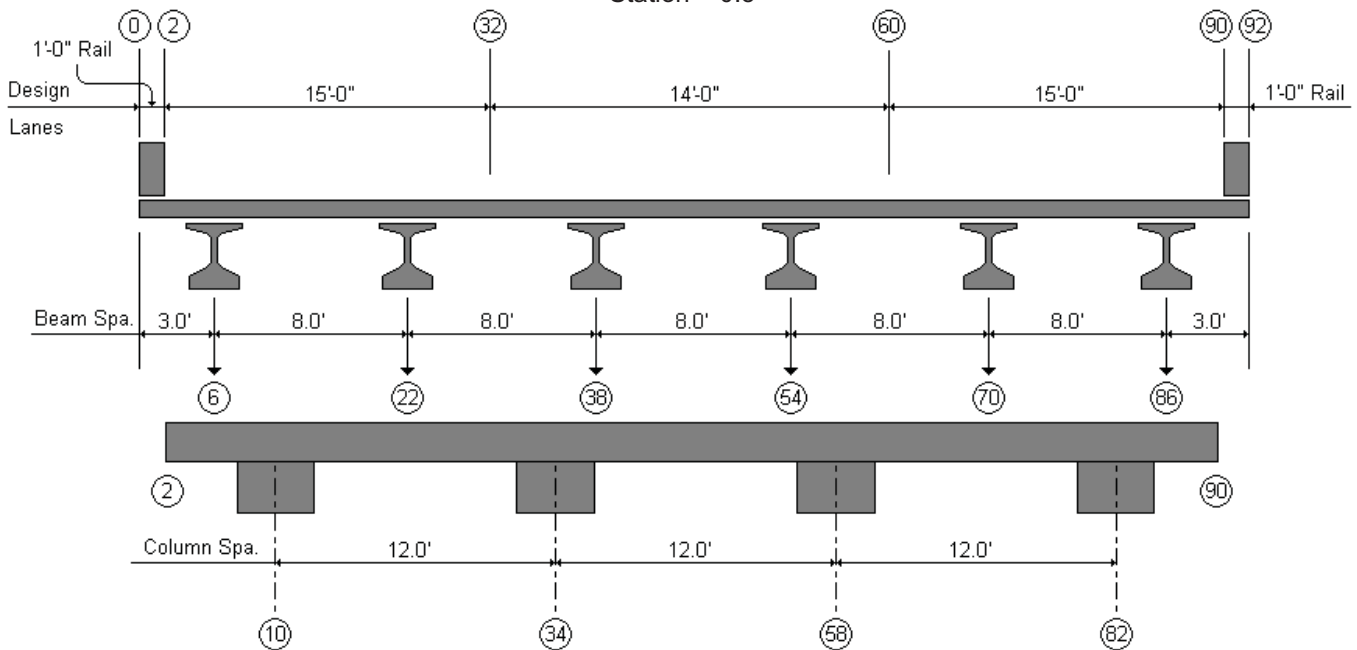
The cap will be modeled as a continuous beam with simple supports using TxDOT's CAP18 program.



TxDOT does not consider frame action for typical multi-column bents.
(BDM-LRFD, Ch. 4, Sect. 5, Structural Analysis)

Cap 18 Model

Station = 0.5'



The circled numbers are the stations that will be used in the CAP 18 input file. One station is 0.5ft in the direction perpendicular to the pgl, not parallel to the bent.

station = 0.5ft

Station increment for CAP18

Recall:

$$E_c = 3457.14 \cdot \text{ksi} \quad (\text{Pg. 2})$$

$$I_g = 2.91 \times 10^6 \cdot \text{in}^4 \quad (\text{Pg.6})$$

$$E_c \cdot I_g = 1.01 \times 10^{10} \cdot \text{kip} \cdot \text{in}^2 / \left(12 \frac{\text{in}}{\text{ft}}\right)^2 = E_c \cdot I_g = 6.99 \times 10^7 \cdot \text{kip} \cdot \text{ft}^2$$

Cap Analysis (Con't)

Dead Load

SPAN 1

Values used in the following equations can be found on Pg. 2.

$$\text{Rail1} = \frac{2 \cdot \text{RailWt} \cdot \frac{\text{Span1}}{2}}{\min(\text{GdrNo1}, 6)}$$

$$\text{Rail1} = 3.44 \cdot \frac{\text{kip}}{\text{girder}}$$

Rail weight is distributed evenly among stringers, up to 3 stringers per rail. (TxSP)

$$\text{Slab1} = w_c \cdot \text{GdrSpa1} \cdot \text{SlabThk} \cdot \frac{\text{Span1}}{2} \cdot 1.10$$

$$\text{Slab1} = 23.76 \cdot \frac{\text{kip}}{\text{girder}}$$

Increase slab DL by 10% to account for haunch and thickened slab ends.

$$\text{Girder1} = \text{GdrWt1} \cdot \frac{\text{Span1}}{2}$$

$$\text{Girder1} = 22.98 \cdot \frac{\text{kip}}{\text{girder}}$$

$$\text{DLRxn1} = \text{Rail1} + \text{Slab1} + \text{Girder1}$$

$$\text{DLRxn1} = 50.17 \cdot \frac{\text{kip}}{\text{girder}}$$

Overlay is calculated separately, because it has a different load factor than the rest of the dead loads.

$$\text{Overlay1} = W_{\text{Olay}} \cdot \text{GdrSpa1} \cdot \text{OverlayThk} \cdot \frac{\text{Span1}}{2}$$

$$\text{Overlay1} = 5.04 \cdot \frac{\text{kip}}{\text{girder}}$$

Design for future overlay.

SPAN 2

$$\text{Rail2} = \frac{2 \cdot \text{RailWt} \cdot \frac{\text{Span2}}{2}}{\min(\text{GdrNo2}, 6)}$$

$$\text{Rail2} = 7.13 \cdot \frac{\text{kip}}{\text{girder}}$$

$$\text{Slab2} = w_c \cdot \text{GdrSpa2} \cdot \text{SlabThk} \cdot \frac{\text{Span2}}{2} \cdot 1.10$$

$$\text{Slab2} = 49.28 \cdot \frac{\text{kip}}{\text{girder}}$$

$$\text{Girder2} = \text{GdrWt2} \cdot \frac{\text{Span2}}{2}$$

$$\text{Girder2} = 47.66 \cdot \frac{\text{kip}}{\text{girder}}$$

$$\text{DLRxn2} = \text{Rail2} + \text{Slab2} + \text{Girder2}$$

$$\text{DLRxn2} = 104.07 \cdot \frac{\text{kip}}{\text{girder}}$$

$$\text{Overlay2} = W_{\text{Olay}} \cdot \text{GdrSpa2} \cdot \text{OverlayThk} \cdot \frac{\text{Span2}}{2}$$

$$\text{Overlay2} = 10.45 \cdot \frac{\text{kip}}{\text{girder}}$$

CAP

$$\text{Cap} = w_c \cdot A_g = 4.970 \cdot \frac{\text{kip}}{\text{ft}} * \frac{0.5\text{ft}}{\text{station}} =$$

$$\text{Cap} = 2.485 \cdot \frac{\text{kip}}{\text{station}}$$

Cap Analysis (Con't)

Live Load (AASHTO LRFD 3.6.1.2.2 and 3.6.1.2.4)

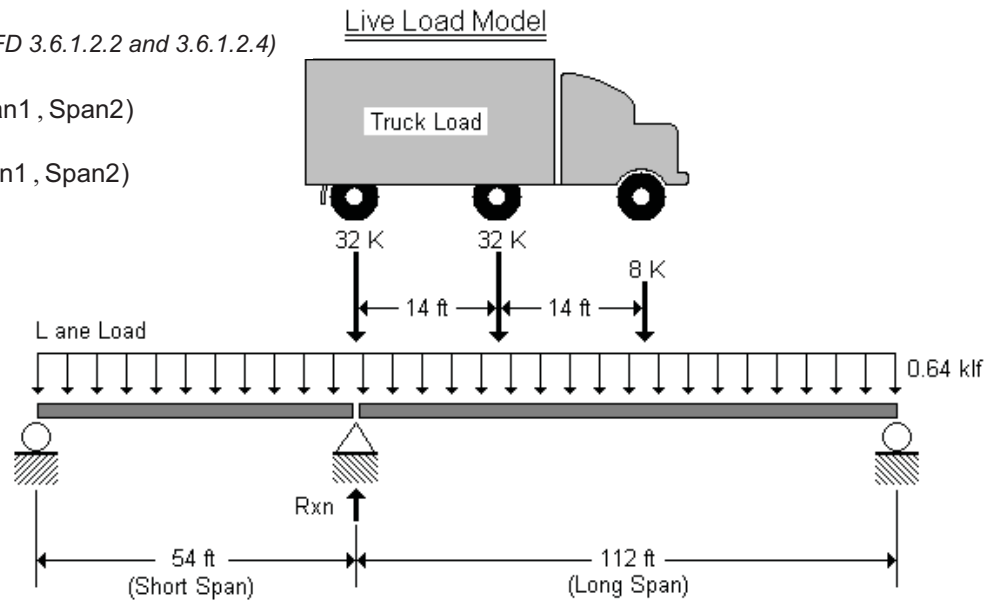
$$\text{LongSpan} = \max(\text{Span1}, \text{Span2})$$

$$\text{ShortSpan} = \min(\text{Span1}, \text{Span2})$$

$$\text{LongSpan} = 112.00 \text{ ft}$$

$$\text{ShortSpan} = 54.00 \text{ ft}$$

$$\text{IM} = 0.33$$



$$\text{Lane} = 0.64 \text{ klf} \cdot \left(\frac{\text{LongSpan} + \text{ShortSpan}}{2} \right)$$

$$\text{Lane} = 53.12 \cdot \frac{\text{kip}}{\text{lane}}$$

$$\text{Truck} = 32 \text{ kip} + 32 \text{ kip} \cdot \left(\frac{\text{LongSpan} - 14 \text{ ft}}{\text{LongSpan}} \right) + 8 \text{ kip} \cdot \left(\frac{\text{LongSpan} - 28 \text{ ft}}{\text{LongSpan}} \right)$$

$$\text{Truck} = 66.00 \cdot \frac{\text{kip}}{\text{lane}}$$

$$\text{LLRxn} = \text{Lane} + \text{Truck} \cdot (1 + \text{IM})$$

$$\text{LLRxn} = 140.90 \cdot \frac{\text{kip}}{\text{lane}}$$

Use HL-93 Live Load. For maximum reaction at interior bents, "Design Truck" will always govern over "Design Tandem". For the maximum reaction when the long span is more than twice as long as the short span, place the rear (32 kip) axle over the support and the middle (32 kip) and front (8 kip) axles on the long span. For the maximum reaction when the long span is less than twice as long as the short span, place the middle (32 kip) axle over the support, the front (8 kip) axle on the short span and the rear (32 kip) axle on the long span.

Combine "Design Truck" and "Design Lane" loadings. (AASHTO LRFD 3.6.1.3)

Dynamic load allowance, IM, does not apply to "Design Lane." (AASHTO LRFD 3.6.1.2.4)

The Live Load is applied to the slab by two 16 kip wheel loads increased by the dynamic load allowance with the remainder of the live load distributed over a 10 ft (AASHTO LRFD 3.6.1.2.1) design lane width. (TxSP)

The Live Load applied to the slab is distributed to the beams assuming the slab is hinged at each beam except the outside beam. (BDM-LRFD, Ch. 4, Sect. 5, Structural Analysis)

Cap 18 Live Load Model

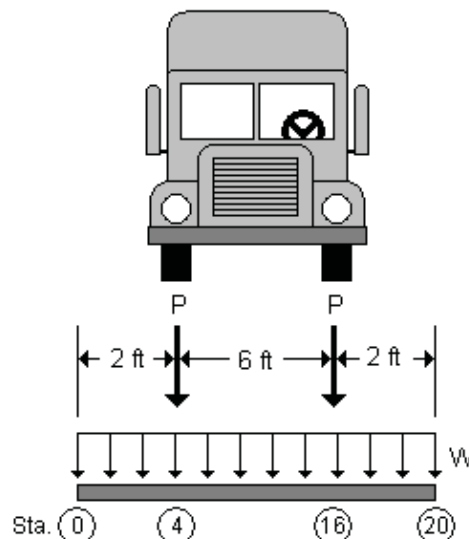
$$P = 16.0 \text{ kip} \cdot (1 + \text{IM})$$

$$P = 21.28 \cdot \text{kip}$$

$$w = \frac{\text{LLRxn} - (2 \cdot P)}{10 \text{ ft}}$$

$$w = 9.83 \cdot \frac{\text{kip}}{\text{ft}} \cdot \frac{0.5 \text{ ft}}{\text{station}}$$

$$w = 4.92 \cdot \frac{\text{kip}}{\text{station}}$$



Cap Analysis (Con't)

Cap 18 Input

Multiple Presence Factors, m (AASHTO LRFD Table 3.6.1.1.2-1)

No. of Lanes	Factor "m"
1	1.20
2	1.00
3	0.85
>3	0.65

Input "Multiple Presence Factors" into Cap18 as "Load Reduction Factors".

Limit States (AASHTO LRFD 3.4.1)

Strength I

Live Load and Dynamic Load Allowance LL + IM = 1.75

Dead Load Components DC = 1.25

Dead Load Wearing Surface (Overlay) DW = 1.50

Service I

Live Load and Dynamic Load Allowance LL + IM = 1.00

Dead Load and Wearing Surface DC & DW = 1.00

The cap design need only consider Strength I, Service I, and Service I with DL. (TxSP)

TxDOT allows the Overlay Factor to be reduced to 1.25 (TxSP), since overlay is typically used in design only to increase the safety factor, but in this example we will use DW = 1.50.

Dead Load

TxDOT considers Service level Dead Load only with a limit reinforcement stress of 22 ksi to minimize cracking.
(BDM-LRFD, Chapter 4, Section 5, Design Criteria)

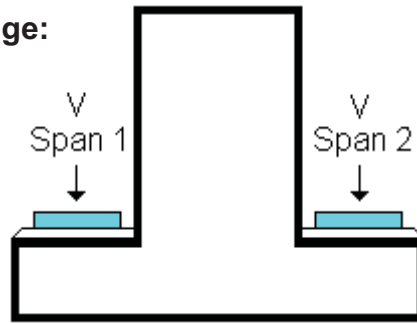
Cap 18 Output

	<u>Max +M</u>	<u>Max -M</u>
Dead Load:	$M_{\text{posDL}} = 250.1 \text{ kip}\cdot\text{ft}$	$M_{\text{negDL}} = -379.4 \text{ kip}\cdot\text{ft}$
Service Load:	$M_{\text{posServ}} = 492.5 \text{ kip}\cdot\text{ft}$	$M_{\text{negServ}} = -590.9 \text{ kip}\cdot\text{ft}$
Factored Load:	$M_{\text{posUlt}} = 741.7 \text{ kip}\cdot\text{ft}$	$M_{\text{negUlt}} = -852.1 \text{ kip}\cdot\text{ft}$

These loads are the maximum loads from the Cap 18 Output File located in the Appendices.

Cap Analysis (Con't)

Girder Reactions on Ledge:



Dead Load

$$DL_{Span1} = Rail1 + Slab1 + Girder1$$

$$DL_{Span1} = 50.17 \cdot \frac{\text{kip}}{\text{girder}} \quad \text{For calculations of these loads see Pg. 8.}$$

$$Overlay1 = 5.04 \cdot \frac{\text{kip}}{\text{girder}}$$

$$DL_{Span2} = Rail2 + Slab2 + Girder2$$

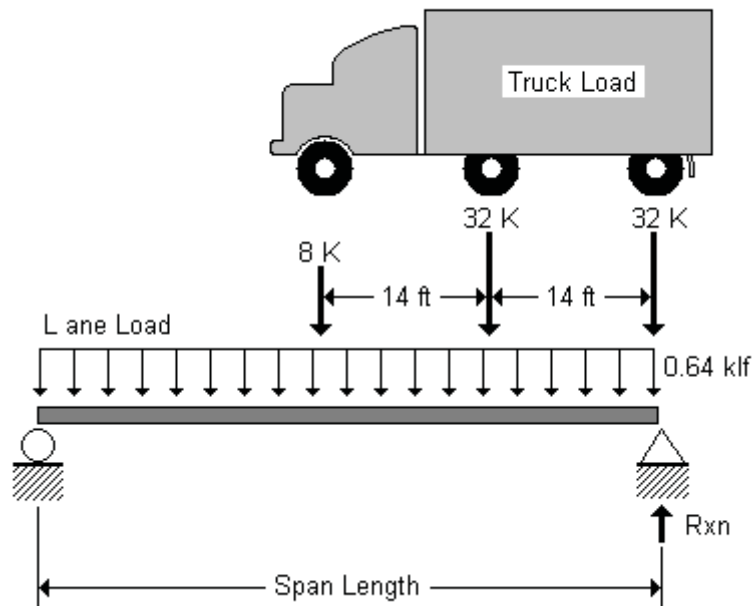
$$DL_{Span2} = 104.07 \cdot \frac{\text{kip}}{\text{girder}}$$

$$Overlay2 = 10.45 \cdot \frac{\text{kip}}{\text{girder}}$$

Live Load (AASHTO LRFD 3.6.1.2.2 and 3.6.1.2.4)

Loads per Lane:

Live Load Model



Use HL-93 Live Load. For maximum reaction at interior bents, "Design Truck" will always govern over "Design Tandem" for Spans greater than 26ft. For the maximum reaction, place the back (32 kip) axle over the support.

$$LaneSpan1 = 0.64\text{klf} \cdot \left(\frac{Span1}{2}\right)$$

$$LaneSpan1 = 17.28 \cdot \frac{\text{kip}}{\text{lane}}$$

$$LaneSpan2 = 0.64\text{klf} \cdot \left(\frac{Span2}{2}\right)$$

$$LaneSpan2 = 35.84 \cdot \frac{\text{kip}}{\text{lane}}$$

$$TruckSpan1 = 32.0\text{kip} + 32.0\text{kip} \cdot \left(\frac{Span1 - 14\text{ft}}{Span1}\right) + 8.0\text{kip} \cdot \left(\frac{Span1 - 28\text{ft}}{Span1}\right)$$

$$TruckSpan1 = 59.56 \cdot \frac{\text{kip}}{\text{lane}}$$

$$TruckSpan2 = 32.0\text{kip} + 32.0\text{kip} \cdot \left(\frac{Span2 - 14\text{ft}}{Span2}\right) + 8.0\text{kip} \cdot \left(\frac{Span2 - 28\text{ft}}{Span2}\right)$$

$$TruckSpan2 = 66.00 \cdot \frac{\text{kip}}{\text{lane}}$$

Cap Analysis (Con't)

Girder Reactions on Ledge (Con't) :

Live Load (Con't)

Loads per Lane (Con't) :

$$IM = 0.33$$

$$LLRxnSpan1 = LaneSpan1 + TruckSpan1 \cdot (1 + IM)$$

$$LLRxnSpan1 = 96.49 \cdot \frac{\text{kip}}{\text{lane}}$$

$$LLRxnSpan2 = LaneSpan2 + TruckSpan2 \cdot (1 + IM)$$

$$LLRxnSpan2 = 123.62 \cdot \frac{\text{kip}}{\text{lane}}$$

$$g^V_{Span1_Int} = 0.814$$

$$g^V_{Span1_Ext} = 0.814$$

$$g^V_{Span2_Int} = 0.814$$

$$g^V_{Span2_Ext} = 0.814$$

Combine "Design Truck" and "Design Lane" loadings.
(AASHTO LRFD 3.6.1.3)

Dynamic load allowance, "IM", does not apply to "Design Lane."
(AASHTO LRFD 3.6.1.2.4)

The Live Load Reactions are assumed to be the Shear Live Load Distribution Factor multiplied by the Live Load Reaction per Lane. The Shear Live Load Distribution Factor was calculated using the "LRFD Live Load Distribution Factors" Spreadsheet found in the Appendices.

The Exterior Girders must have a Live Load Distribution Factor equal to or greater than the Interior Girders. This is to accommodate a possible future bridge widening. Widening the bridge would cause the exterior girders to become interior girders.

$$LLSpan1Int = g^V_{Span1_Int} \cdot LLRxnSpan1$$

$$LLSpan1Int = 78.54 \cdot \frac{\text{kip}}{\text{girder}}$$

$$LLSpan1Ext = g^V_{Span1_Ext} \cdot LLRxnSpan1$$

$$LLSpan1Ext = 78.54 \cdot \frac{\text{kip}}{\text{girder}}$$

$$LLSpan2Int = g^V_{Span2_Int} \cdot LLRxnSpan2$$

$$LLSpan2Int = 100.63 \cdot \frac{\text{kip}}{\text{girder}}$$

$$LLSpan2Ext = g^V_{Span2_Ext} \cdot LLRxnSpan2$$

$$LLSpan2Ext = 100.63 \cdot \frac{\text{kip}}{\text{girder}}$$

Cap Analysis (Con't)

Girder Reactions on Ledge (Con't) :

Span 1

Interior Girder

Service Load *Service I Limit State, (AASHTO LRFD 3.4.1)*

$$V_{s_Span1Int} = DL_{Span1} + Overlay1 + LL_{Span1Int} \quad V_{s_Span1Int} = 134 \cdot \text{kip}$$

Factored Load *Strength I Limit State, (AASHTO LRFD 3.4.1)*

$$V_{u_Span1Int} = 1.25DL_{Span1} + 1.5 \cdot Overlay1 + 1.75LL_{Span1Int} \quad V_{u_Span1Int} = 208 \cdot \text{kip}$$

Exterior Girder

Service Load *Service I Limit State, (AASHTO LRFD 3.4.1)*

$$V_{s_Span1Ext} = DL_{Span1} + Overlay1 + LL_{Span1Ext} \quad V_{s_Span1Ext} = 134 \cdot \text{kip}$$

Factored Load *Strength I Limit State, (AASHTO LRFD 3.4.1)*

$$V_{u_Span1Ext} = 1.25DL_{Span1} + 1.5 \cdot Overlay1 + 1.75LL_{Span1Ext} \quad V_{u_Span1Ext} = 208 \cdot \text{kip}$$

Span 2

Interior Girder

Service Load *Service I Limit State, (AASHTO LRFD 3.4.1)*

$$V_{s_Span2Int} = DL_{Span2} + Overlay2 + LL_{Span2Int} \quad V_{s_Span2Int} = 215 \cdot \text{kip}$$

Factored Load *Strength I Limit State, (AASHTO LRFD 3.4.1)*

$$V_{u_Span2Int} = 1.25DL_{Span2} + 1.5 \cdot Overlay2 + 1.75LL_{Span2Int} \quad V_{u_Span2Int} = 322 \cdot \text{kip}$$

Exterior Girder

Service Load *Service I Limit State, (AASHTO LRFD 3.4.1)*

$$V_{s_Span2Ext} = DL_{Span2} + Overlay2 + LL_{Span2Ext} \quad V_{s_Span2Ext} = 215 \cdot \text{kip}$$

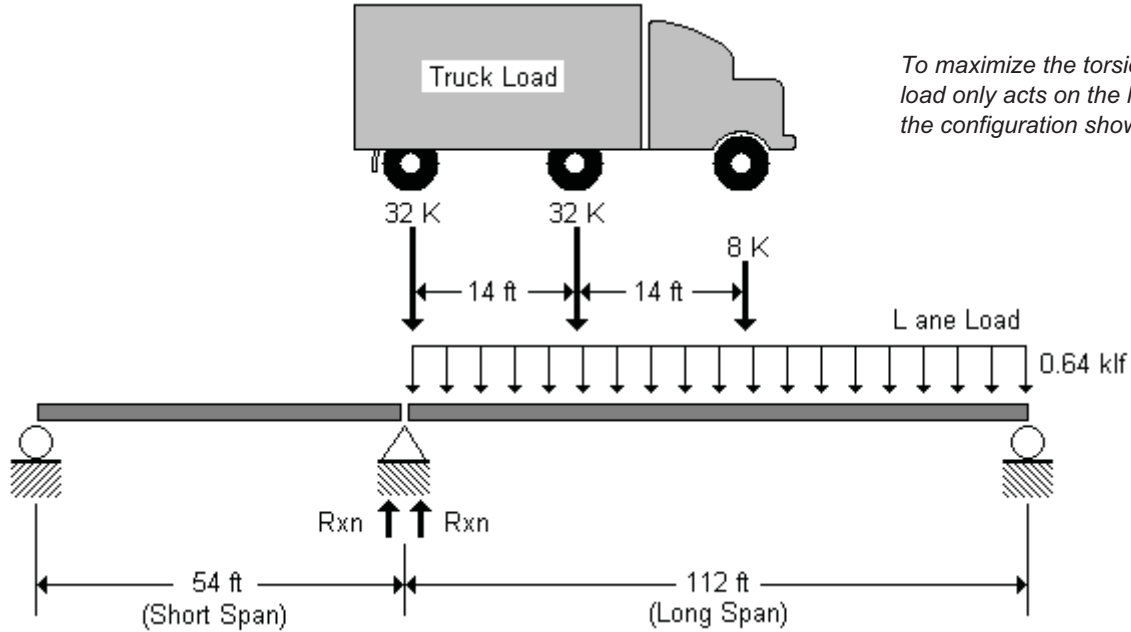
Factored Load *Strength I Limit State, (AASHTO LRFD 3.4.1)*

$$V_{u_Span2Ext} = 1.25DL_{Span2} + 1.5 \cdot Overlay2 + 1.75LL_{Span2Ext} \quad V_{u_Span2Ext} = 322 \cdot \text{kip}$$

Cap Analysis (Con't)

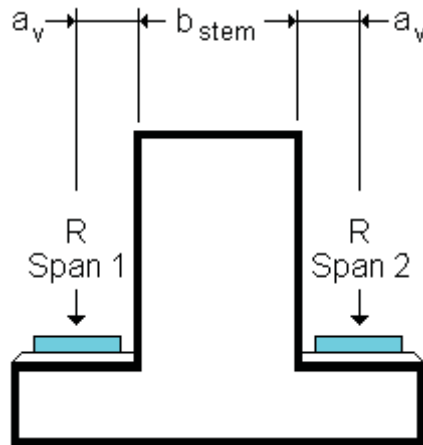
Torsional Loads

Strength I Limit State, (AASHTO LRFD 3.4.1)



To maximize the torsion, the live load only acts on the longer span in the configuration shown.

The loads are applied to the cap as depicted in the following picture:



$$a_v = 12\text{in}$$

" a_v " is the value for the distance from the face of the stem to the center of bearing for the girders. 12" is the typical value for TxGirders on Inverted Tee Bents (IGEB). 9" is the typical value for I-Beams (IBEB). The lever arm for the torsional loads is the distance from the center line of bearing to the centerline of the cap ($\frac{1}{2}b_{stem} + a_v$).

$$b_{stem} = 39\text{in}$$

From Pg. 3

$$\text{LeverArm} = a_v + \frac{1}{2} \cdot b_{stem}$$

$$\text{LeverArm} = 31.5\text{in}$$

Cap Analysis (Con't)

Torsional Loads (Con't)

Interior Girders

Girder Reactions

$$R_{u_Span1} = 1.25 \cdot DL_{Span1} + 1.5 \cdot Overlay1 \quad R_{u_Span1} = 70 \cdot \text{kip}$$

$$R_{u_Span2} = 1.25 \cdot DL_{Span2} + 1.5 \cdot Overlay2 + 1.75 \cdot gV_{Span2_Int} \cdot [LaneSpan2 + TruckSpan2 \cdot (1 + IM)]$$

$$R_{u_Span2} = 322 \cdot \text{kip}$$

Torsional Load

$$T_{u_Int} = |R_{u_Span1} - R_{u_Span2}| \cdot \text{LeverArm} \quad T_{u_Int} = 660 \cdot \text{kip} \cdot \text{ft}$$

Exterior Girders

Girder Reactions

$$R_{u_Span1} = 1.25 \cdot DL_{Span1} + 1.5 \cdot Overlay1 \quad R_{u_Span1} = 70 \cdot \text{kip}$$

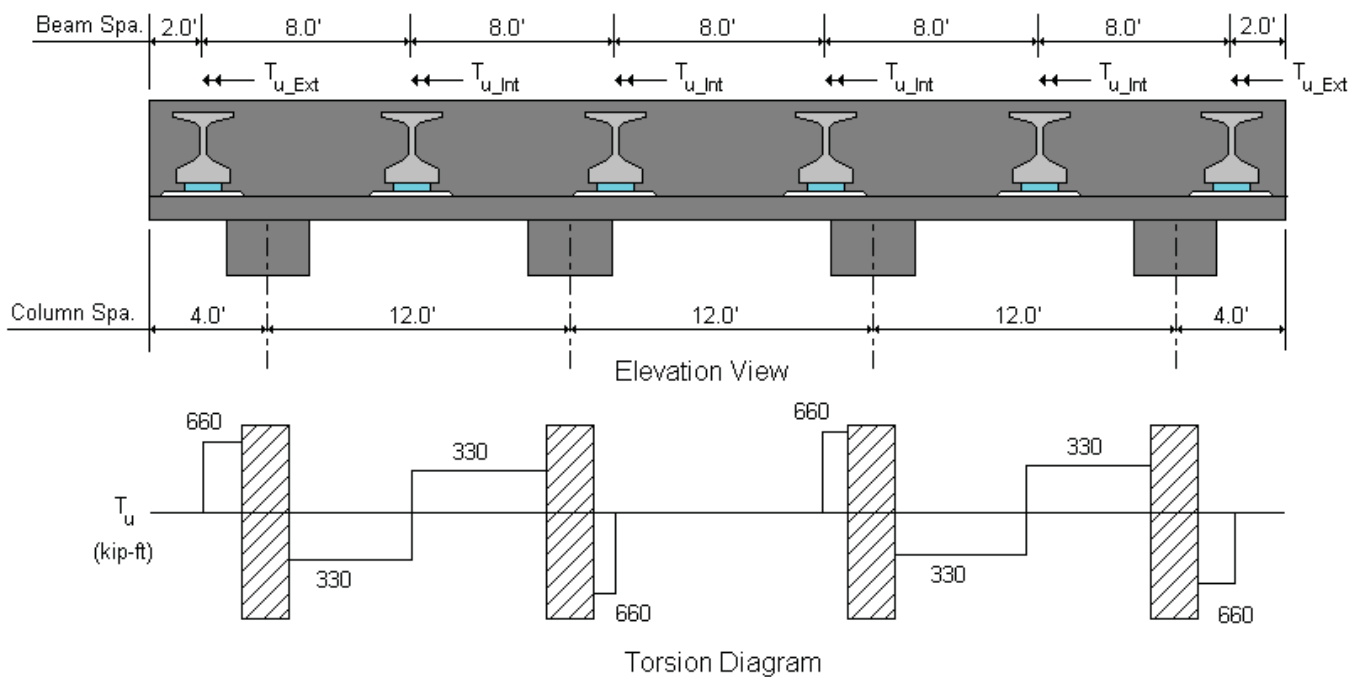
$$R_{u_Span2} = 1.25 \cdot DL_{Span2} + 1.5 \cdot Overlay2 + 1.75 \cdot gV_{Span2_Ext} \cdot [LaneSpan2 + TruckSpan2 \cdot (1 + IM)]$$

$$R_{u_Span2} = 322 \cdot \text{kip}$$

Torsional Load

$$T_{u_Ext} = |R_{u_Span1} - R_{u_Span2}| \cdot \text{LeverArm} \quad T_{u_Ext} = 660 \cdot \text{kip} \cdot \text{ft}$$

Torsion on Cap



Analyzed assuming Bents are torsionally rigid at Effective Face of Columns.

$$T_u = 660 \text{kip} \cdot \text{ft}$$

Maximum Torsion on Cap

Cap Analysis (Con't)

Load Summary

Ledge Loads

Interior Girder

Service Load

$$V_{s_Int} = \max(V_{s_Span1Int}, V_{s_Span2Int}) \quad V_{s_Int} = 215.15 \cdot \text{kip}$$

Factored Load

$$V_{u_Int} = \max(V_{u_Span1Int}, V_{u_Span2Int}) \quad V_{u_Int} = 321.86 \cdot \text{kip}$$

Exterior Girder

Service Load

$$V_{s_Ext} = \max(V_{s_Span1Ext}, V_{s_Span2Ext}) \quad V_{s_Ext} = 215.15 \cdot \text{kip}$$

Factored Load

$$V_{u_Ext} = \max(V_{u_Span1Ext}, V_{u_Span2Ext}) \quad V_{u_Ext} = 321.86 \cdot \text{kip}$$

Cap Loads

Positive Moment (From CAP 18)

Dead Load: $M_{\text{posDL}} = 250.10 \cdot \text{kip} \cdot \text{ft}$

Service Load: $M_{\text{posServ}} = 492.50 \cdot \text{kip} \cdot \text{ft}$

Factored Load: $M_{\text{posUlt}} = 741.70 \cdot \text{kip} \cdot \text{ft}$

Negative Moment (From CAP 18)

Dead Load: $M_{\text{negDL}} = -379.40 \cdot \text{kip} \cdot \text{ft}$

Service Load: $M_{\text{negServ}} = -590.90 \cdot \text{kip} \cdot \text{ft}$

Factored Load: $M_{\text{negUlt}} = -852.10 \cdot \text{kip} \cdot \text{ft}$

Maximum Torsion and Concurrent Shear and Moment (Strength I)

$$T_u = 660 \cdot \text{kip} \cdot \text{ft}$$

$$V_u = 448.1 \text{ kip}$$

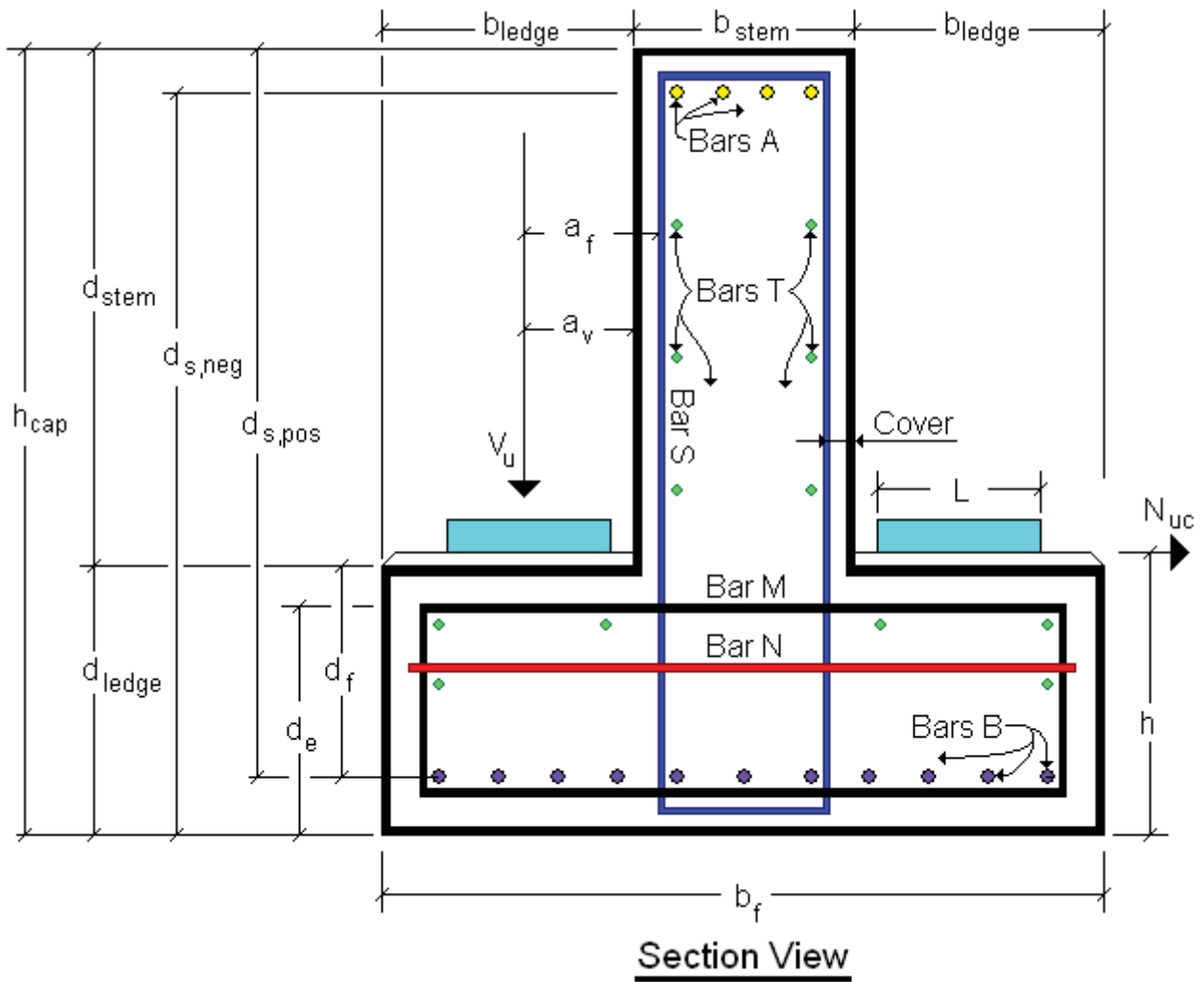
$$M_u = 335.6 \text{ kip} \cdot \text{ft}$$

Located two stations away from centerline of column.

V_u and M_u values are from CAP 18

In this example the maximum Torsion and the maximum Shear are concurrent with each other. If they are not, it becomes necessary to check the location of the maximum Torsion with its concurrent Shear and the location of the maximum Shear with its concurrent Torsion.

Locate and Describe Reinforcement



Recall:

$$b_{stem} = 39 \cdot \text{in}$$

From Pg. 3

$$d_{stem} = 57 \cdot \text{in}$$

From Pg. 3

$$b_{ledge} = 26 \cdot \text{in}$$

From Pg. 5

$$d_{ledge} = 28 \cdot \text{in}$$

From Pg. 5

$$b_f = 91 \cdot \text{in}$$

From Pg. 5

$$h_{cap} = 85 \cdot \text{in}$$

From Pg. 5

$$cover = 2.50 \cdot \text{in}$$

From Pg. 4
Measured from Center of bar

Locate and Describe Reinforcement (Con't)

Describe Reinforcing Bars

Use # 11 bars for Bar A

$$A_{\text{bar}_A} = 1.56\text{in}^2 \quad d_{\text{bar}_A} = 1.410\text{in}$$

Use # 11 bars for Bar B

$$A_{\text{bar}_B} = 1.56\text{in}^2 \quad d_{\text{bar}_B} = 1.410\text{in}$$

Use # 6 bars for Bar M

$$A_{\text{bar}_M} = 0.44\text{in}^2 \quad d_{\text{bar}_M} = 0.75\text{in}$$

Bar M must be a # 6 bar or smaller to allow it to fully develop, as stated on Pg 4.

Use # 6 bars for Bar N

$$A_{\text{bar}_N} = 0.44\text{in}^2 \quad d_{\text{bar}_N} = 0.75\text{in}$$

To prevent confusion, use the same bar size for Bar N as Bar M.

Use # 6 bars for Bar S

$$A_{\text{bar}_S} = 0.44\text{in}^2 \quad d_{\text{bar}_S} = 0.75\text{in}$$

Use # 6 bars for Bar T

$$A_{\text{bar}_T} = 0.44\text{in}^2 \quad d_{\text{bar}_T} = 0.750\text{in}$$

Calculate Dimensions

$$d_{s_neg} = h_{\text{cap}} - \text{cover} - \frac{1}{2} \cdot d_{\text{bar}_S} - \frac{1}{2} \cdot d_{\text{bar}_A}$$

$$d_{s_neg} = 81.42 \cdot \text{in}$$

$$d_{s_pos} = h_{\text{cap}} - \text{cover} - \frac{1}{2} \cdot \max(d_{\text{bar}_S}, d_{\text{bar}_M}) - \frac{1}{2} \cdot d_{\text{bar}_B}$$

$$d_{s_pos} = 81.42 \cdot \text{in}$$

$$a_v = 12 \cdot \text{in}$$

Typical for TX Girders on Inverted Tee Bent Caps (IGEB standard)

$$a_f = a_v + \text{cover}$$

$$a_f = 14.50 \cdot \text{in}$$

$$d_e = d_{\text{ledge}} - \text{cover}$$

$$d_e = 25.50 \cdot \text{in}$$

$$d_f = d_{\text{ledge}} - \text{cover} - \frac{1}{2} \cdot d_{\text{bar}_M} - \frac{1}{2} \cdot d_{\text{bar}_B} \quad d_f = 24.42 \cdot \text{in}$$

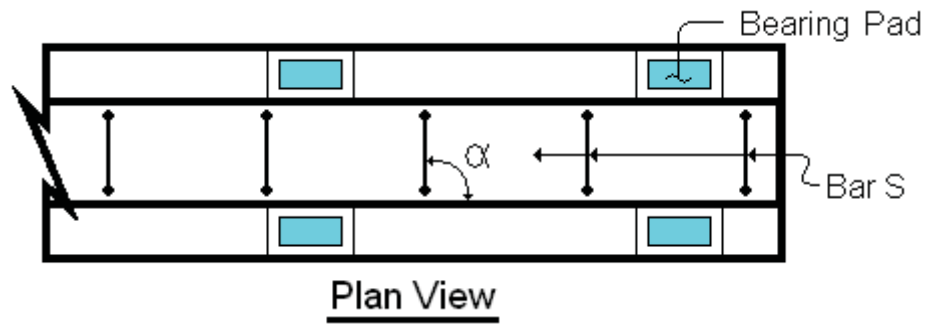
$$h = d_{\text{ledge}} + \text{BrgSeat}$$

$$h = 29.50 \cdot \text{in}$$

"BrgSeat" is the height of the Bearing Seat Buildup. This value is defined on Pg. 2.

Locate and Describe Reinforcement (Con't)

Calculate Dimensions (Con't)



$\alpha = 90\text{deg}$

Angle of Bars S

Recall:

$L = 8\cdot\text{in}$

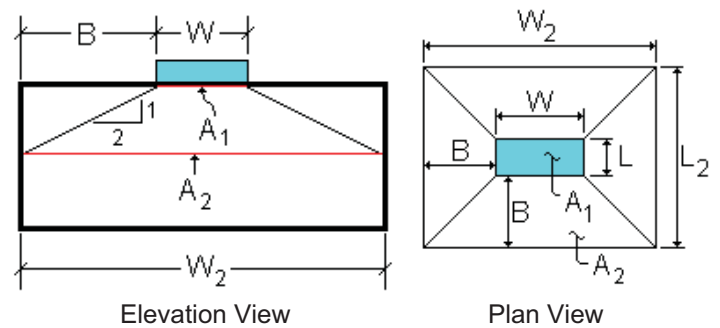
From Pg. 4

$W = 21\cdot\text{in}$

From Pg. 6

Check Bearing (AASHTO LRFD 5.7.5)

The load on the bearing pad propagates along a truncated pyramid whose top has the area A_1 and whose base has the area A_2 . A_1 is the loaded area (the bearing pad area: $L \times W$). A_2 is the area of the lowest rectangle contained wholly within the support (the Inverted Tee Cap). A_2 must not overlap the truncated pyramid of another load in either direction, nor can it extend beyond the edges of the cap in any direction.



(AASHTO LRFD 5.5.4.2.1)

$$\phi = 0.7$$

$$A_1 = W \cdot L$$

$$A_1 = 168 \cdot \text{in}^2$$

Area under Bearing Pad

Interior Girders

$$B = \min \left[\left(b_{\text{ledge}} - a_v \right) - \frac{1}{2} \cdot L, \left(a_v + \frac{1}{2} \cdot b_{\text{stem}} \right) - \frac{1}{2} \cdot L, 2d_{\text{ledge}}, \frac{1}{2} \cdot S - \frac{1}{2} \cdot W \right]$$

"B" is the distance from the perimeter of A_1 to the perimeter of A_2 , as seen in the above figures.

$$B = 10.00 \cdot \text{in}$$

$$L_2 = L + 2 \cdot B$$

$$L_2 = 28.00 \cdot \text{in}$$

$$W_2 = W + 2 \cdot B$$

$$W_2 = 41.00 \cdot \text{in}$$

$$A_2 = L_2 \cdot W_2$$

$$A_2 = 1148 \cdot \text{in}^2$$

m = the minimum of:

Modification Factor

$$\sqrt{\frac{A_2}{A_1}} = 2.61 \quad \& \quad 2$$

$$m = 2.00$$

(AASHTO LRFD Eq. 5.7.5-3)

$$\phi V_n = \phi \cdot 0.85 \cdot f_c \cdot A_1 \cdot m$$

$$\phi V_n = 720 \cdot \text{kip}$$

(AASHTO LRFD Eq. 5.7.5-1 & AASHTO LRFD Eq. 5.7.5-2)

$$V_{u_Int} = 322 \cdot \text{kip} < \phi V_n$$

BearingChk = "OK!"

V_{u_Int} From Pg. 16

Exterior Girders

$$B = \min \left[\left(b_{\text{ledge}} - a_v \right) - \frac{1}{2} \cdot L, \left(a_v + \frac{1}{2} \cdot b_{\text{stem}} \right) - \frac{1}{2} \cdot L, 2d_{\text{ledge}}, \frac{1}{2} \cdot S - \frac{1}{2} \cdot W, c - \frac{1}{2} \cdot W \right]$$

$$B = 10.00 \cdot \text{in}$$

"B" is the distance from the perimeter of A_1 to the perimeter of A_2 .

$$L_2 = L + 2 \cdot B$$

$$L_2 = 28.00 \cdot \text{in}$$

$$W_2 = W + 2 \cdot B$$

$$W_2 = 41.00 \cdot \text{in}$$

$$A_2 = L_2 \cdot W_2$$

$$A_2 = 1148 \cdot \text{in}^2$$

m = the minimum of:

Modification Factor

$$\sqrt{\frac{A_2}{A_1}} = 2.61 \quad \& \quad 2$$

$$m = 2.00$$

(AASHTO LRFD Eq. 5.7.5-3)

$$\phi V_n = \phi \cdot 0.85 \cdot f_c \cdot A_1 \cdot m$$

$$\phi V_n = 720 \cdot \text{kip}$$

(AASHTO LRFD Eq. 5.7.5-1 & AASHTO LRFD Eq. 5.7.5-2)

$$V_{u_Ext} = 322 \cdot \text{kip} < \phi V_n$$

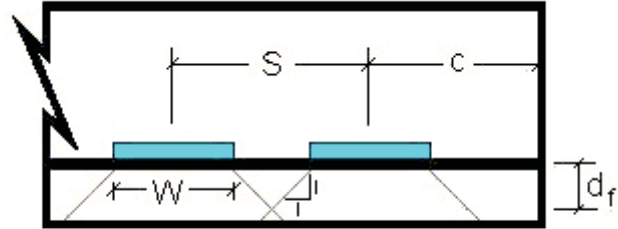
BearingChk = "OK!"

V_{u_Ext} From Pg. 16

Check Punching Shear

(AASHTO LRFD 5.13.2.5.4 with modifications from BDM-LRFD, Ch. 4, Sect. 5, Design Criteria)

$$\phi = 0.9 \quad (\text{AASHTO LRFD 5.5.4.2.1})$$



Elevation

Determine if the Shear Cones Intersect

$$\text{Is } \frac{1}{2} \cdot S - \frac{1}{2} \cdot W \geq d_f \quad ?$$

Yes. Therefore Shear Cones do not intersect in the longitudinal direction of the Cap.

$$\frac{1}{2} \cdot S - \frac{1}{2} \cdot W = 37.50 \cdot \text{in}$$

$$d_f = 24.42 \cdot \text{in}$$

TxDOT uses "d_f" instead of "d_e" for Punching Shear (BDM-LRFD, Ch. 4, Sect. 5, Design Criteria). This is because "d_f" has traditionally been used for inverted tee bents and was used in the Inverted Tee Research (Furlong & Mirza pg. 58).

$$\text{Is } \frac{1}{2} b_{\text{stem}} + a_v - \frac{1}{2} \cdot L \geq d_f \quad ?$$

Yes. Therefore Shear Cones do not intersect in the transverse direction of the Cap.

$$\frac{1}{2} b_{\text{stem}} + a_v - \frac{1}{2} \cdot L = 27.50 \cdot \text{in}$$

$$d_f = 24.42 \cdot \text{in}$$

Interior Girders

$$V_n = 0.125 \cdot \sqrt{f_c} \cdot (W + 2 \cdot L + 2 \cdot d_f) \cdot d_f$$

$$V_n = 497 \cdot \text{kip}$$

(BDM-LRFD, Ch. 4, Sect. 5, Design Criteria)

$$\phi V_n = 447 \cdot \text{kip}$$

$$V_{u_Int} = 322 \cdot \text{kip} < \phi V_n$$

PunchingShearChk = "OK!"

V_{u_Int} From Pg. 16

Exterior Girders

V_n = minimum of:

$$0.125 \cdot \sqrt{f_c} \cdot \left(\frac{1}{2} \cdot W + L + d_f + c \right) \cdot d_f = 388 \cdot \text{kip}$$

$$0.125 \cdot \sqrt{f_c} \cdot (W + 2 \cdot L + 2d_f) \cdot d_f = 497 \cdot \text{kip}$$

(BDM-LRFD, Ch. 4, Sect. 5, Design Criteria)

$$V_n = 388 \cdot \text{kip}$$

$$\phi V_n = 349 \cdot \text{kip}$$

$$V_{u_Ext} = 322 \cdot \text{kip} < \phi V_n$$

PunchingShearChk = "OK!"

V_{u_Ext} From Pg. 16

Check Shear Friction (AASHTO LRFD 5.13.2.5.2)

$$\phi = 0.9 \quad (\text{AASHTO LRFD 5.5.4.2.1})$$

Determine the Distribution Width (AASHTO LRFD 5.13.2.5.2)

Interior Girders

$$b_{s_Int} = \text{minimum of:}$$
$$W + 4 a_v = 69.00 \cdot \text{in}$$

$$S = 96.00 \cdot \text{in}$$

$$b_{s_Int} = 69.00 \cdot \text{in}$$

Checks are for concrete only see "Ledge Reinforcement" for reinforcement checks for Bars M and N.

"S" is the girder spacing.

Exterior Girders

$$b_{s_Ext} = \text{minimum of:}$$
$$W + 4 a_v = 69.00 \cdot \text{in}$$

$$S = 96.00 \cdot \text{in}$$

$$2 c = 48.00 \cdot \text{in}$$

$$b_{s_Ext} = 48.00 \cdot \text{in}$$

"S" is the girder spacing.

Interior Girders

$$A_{cv} = d_e \cdot b_{s_Int}$$

$$A_{cv} = 1759 \cdot \text{in}^2$$

$$V_n = \text{minimum of:}$$

$$0.2 f_c \cdot A_{cv} = 1267 \cdot \text{kip}$$

(AASHTO LRFD Eq. 5.13.2.4.2-1)

$$0.8 \text{ ksi} \cdot A_{cv} = 1408 \cdot \text{kip}$$

(AASHTO LRFD Eq. 5.13.2.4.2-2)

$$V_n = 1267 \cdot \text{kip}$$

$$\phi V_n = 1140 \cdot \text{kip}$$

$$V_{u_Int} = 322 \cdot \text{kip} < \phi V_n$$

ShearFrictionChk = "OK!"

V_{u_Int} From Pg. 16

Exterior Girders

$$A_{cv} = d_e \cdot b_{s_Ext}$$

$$A_{cv} = 1224 \cdot \text{in}^2$$

$$V_n = \text{minimum of:}$$

$$0.2 f_c \cdot A_{cv} = 881 \cdot \text{kip}$$

(AASHTO LRFD Eq. 5.13.2.4.2-1)

$$0.8 \text{ ksi} \cdot A_{cv} = 979 \cdot \text{kip}$$

(AASHTO LRFD Eq. 5.13.2.4.2-2)

$$V_n = 881 \cdot \text{kip}$$

$$\phi V_n = 793 \cdot \text{kip}$$

$$V_{u_Ext} = 322 \cdot \text{kip} < \phi V_n$$

ShearFrictionChk = "OK!"

V_{u_Ext} From Pg. 16

Flexural Reinforcement for Negative Bending (Bars A)

(Tension in Top)

$$M_{dl} = |M_{negDL}|$$

$$M_{dl} = 379.4 \cdot \text{kip} \cdot \text{ft}$$

$$M_s = |M_{negServ}|$$

$$M_s = 590.9 \cdot \text{kip} \cdot \text{ft}$$

From Cap 18 Output. See Pg. 10

$$M_u = |M_{negUlt}|$$

$$M_u = 852.1 \cdot \text{kip} \cdot \text{ft}$$

Minimum Flexural Reinforcement (AASHTO LRFD 5.7.3.3.2)

Factored Flexural Resistance, M_r , must be greater than or equal to the lesser of $1.2 M_{cr}$ (Cracking Moment) or $1.33 M_u$ (Ultimate Moment)

$$I_g = 2.91 \times 10^6 \cdot \text{in}^4$$

*Gross Moment of Inertia
(From Pg. 6)*

$$h_{cap} = 85 \cdot \text{in}$$

Depth of Cap (From Pg. 5)

$$y_{bar} = 33.80 \cdot \text{in}$$

Distance to the Center of Gravity of the Cap from the bottom of the Cap (From Pg. 6)

$$f_r = 0.24 \cdot \sqrt{f_c}$$

$$f_r = 0.455 \cdot \text{ksi}$$

*Modulus of Rupture
(BDM-LRFD, Ch. 4, Sect. 5, Design Criteria)*

$$y_t = h_{cap} - y_{bar}$$

$$y_t = 51.20 \cdot \text{in}$$

Distance from Center of Gravity to extreme tension fiber

$$S = \frac{I_g}{y_t}$$

$$S = 5.69 \times 10^4 \cdot \text{in}^3$$

Section Modulus for the extreme tension fiber

$$M_{cr} = S \cdot f_r \cdot \frac{1\text{ft}}{12\text{in}}$$

$$M_{cr} = 2158.9 \cdot \text{kip} \cdot \text{ft}$$

*Cracking Moment
(AASHTO LRFD Eq. 5.7.3.3.2-1)*

$M_f =$ minimum of:

$$1.2 \cdot M_{cr} = 2590.7 \cdot \text{kip} \cdot \text{ft}$$

$$1.33 \cdot M_u = 1133.3 \cdot \text{kip} \cdot \text{ft}$$

Design for the lesser of $1.2M_{cr}$ or $1.33M_u$ when determining minimum area of steel required.

Thus, M_r must be greater than

$$M_f = 1133.3 \cdot \text{kip} \cdot \text{ft}$$

Flexural Reinforcement for Negative Bending (Con't) (Bars A)

Moment Capacity Design

(AASHTO LRFD 5.7.3.2)

Try, 5 ~ #11's Top

$$\text{BarANo} = 5$$

Number of bars in tension

$$d_{\text{bar}_A} = 1.41 \text{ in}$$

Diameter of main reinforcing bars

$$A_{\text{bar}_A} = 1.56 \text{ in}^2$$

Area of one main reinforcing bar

$$A_s = (\text{BarANo}) \cdot A_{\text{bar}_A}$$

$$A_s = 7.80 \cdot \text{in}^2$$

Area of steel in tension

$$d_{\text{stirrup}} = d_{\text{bar}_S}$$

$$d_{\text{stirrup}} = 0.75 \cdot \text{in}$$

Diameter of shear reinforcing bars
From Pg. 18

$$d = d_{s_neg}$$

$$d = 81.42 \cdot \text{in}$$

See Pg. 18 for the calculation of
"d_{s_neg},"

$$b = b_f$$

$$b = 91 \cdot \text{in}$$

See Pg. 5 for the calculation of "b_f"

$$f_c = 3.60 \cdot \text{ksi}$$

Compressive Strength of Concrete

$$f_y = 60 \cdot \text{ksi}$$

Yield Strength of Rebar

$$\beta_1 = 0.85 - 0.05 \cdot (f_c - 4 \cdot \text{ksi})$$

(AASHTO LRFD 5.7.2.2)

$$\text{Bounded by: } 0.65 \leq \beta_1 \leq 0.85$$

$$\beta_1 = 0.85$$

$$c = \frac{A_s \cdot f_y}{0.85 \cdot f_c \cdot \beta_1 \cdot b}$$

$$c = 1.98 \cdot \text{in}$$

Depth of Cross Section under
Compression under Ultimate Load
(AASHTO LRFD Eq. 5.7.3.1.2-4)

This "c" is the distance from the extreme compression fiber to the neutral axis, not the distance from the center of bearing of the last girder to the end of the cap.

$$a = c \cdot \beta_1$$

$$a = 1.68 \cdot \text{in}$$

Depth of Equivalent Stress Block
(AASHTO LRFD 5.7.2.2)

Note: "a" is less than "d_{edge}" therefore the equivalent stress block acts over a rectangular area. If "a" was greater than "d_{edge}" it would act over a Tee shaped area.

$$M_n = A_s \cdot f_y \cdot \left(d - \frac{a}{2} \right) \cdot \frac{1 \text{ ft}}{12 \text{ in}}$$

$$M_n = 3142.6 \cdot \text{kip} \cdot \text{ft}$$

Nominal Flexural Resistance
(AASHTO LRFD Eq. 5.7.3.2.2-1)

$$\epsilon_s = 0.003 \cdot \frac{d - c}{c}$$

$$\epsilon_s = 0.121$$

Strain in Reinforcing at Ultimate

$$\epsilon_s > 0.005$$

FlexureBehavior = "Tension Controlled"

(AASHTO LRFD 5.7.2.1)

$$\phi_M = 0.90$$

(AASHTO LRFD 5.5.4.2.1)

$$M_r = \phi_M \cdot M_n$$

$$M_r = 2828.3 \cdot \text{kip} \cdot \text{ft}$$

Factored Flexural Resistance
(AASHTO LRFD Eq. 5.7.3.2.1-1)

$$M_f = 1133.3 \cdot \text{kip} \cdot \text{ft} < M_r$$

MinReinfChk = "OK!"

$$M_u = 852.1 \cdot \text{kip} \cdot \text{ft} < M_r$$

UltimateMom = "OK!"

Flexural Reinforcement for Negative Bending (Con't) (Bars A)

Check Serviceability (AASHTO LRFD 5.7.3.4)

To find s_{max} :

Modular Ratio:

$$n = \frac{E_s}{E_c}$$

Tension Reinforcement Ratio:

$$\rho = \frac{A_s}{b \cdot d}$$

$$k = \sqrt{(2 \cdot \rho \cdot n) + (\rho \cdot n)^2} - (\rho \cdot n)$$

$$d \cdot k = 10.13 \cdot \text{in} < d_{ledge} = 28.00 \cdot \text{in} \quad \text{Therefore, the compression force acts over a rectangular area.}$$

$$j = 1 - \frac{k}{3}$$

$$f_{ss} = \frac{M_s}{A_s \cdot j \cdot d} \cdot \frac{12 \text{in}}{1 \text{ft}}$$

$$f_a = 0.6 \cdot f_y$$

$$f_{ss} < f_a$$

$$d_c = \text{cover} + \frac{1}{2} \cdot d_{stirrup} + \frac{1}{2} \cdot d_{bar_A}$$

Exposure Condition Factor:

$$\gamma_e = 1.00$$

$$\beta_s = 1 + \frac{d_c}{0.7 \cdot (h_{cap} - d_c)}$$

s_{max} = minimum of:

$$\frac{700 \gamma_e}{\beta_s \cdot f_{ss}} - 2d_c = 49.38 \cdot \text{in}$$

& 12in

$$s_{max} = 12.00 \cdot \text{in}$$

$$s_{Actual} = \frac{b_{stem} - 2 \cdot \left(\text{cover} + \frac{1}{2} \cdot d_{stirrup} + \frac{1}{2} \cdot d_{bar_A} \right)}{\text{BarANo} - 1}$$

$$s_{Actual} = 7.96 \cdot \text{in} < s_{max}$$

ServiceabilityCheck = "OK!"

Check Dead Load

BDM-LRFD, Chapter 4, Section 5, Design Criteria

Check allowable M_{dl} :

$$f_{dl} = 22 \text{ksi}$$

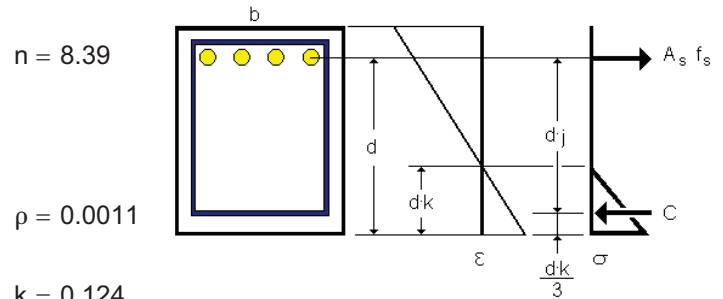
$$M_a = A_s \cdot d \cdot j \cdot f_{dl} \cdot \frac{1 \text{ft}}{12 \text{in}}$$

$$M_a = 1116.04 \cdot \text{kip} \cdot \text{ft} \quad \text{Allowable Dead Load Moment}$$

$$M_{dl} = 379.40 \cdot \text{kip} \cdot \text{ft} < M_a$$

DeadLoadMom = "OK!"

For service loads, the stress on the cross-section is located as drawn:



$$n = 8.39$$

$$\rho = 0.0011$$

$$k = 0.124$$

$$j = 0.959$$

$$f_{ss} = 11.65 \cdot \text{ksi}$$

$$f_a = 36.00 \cdot \text{ksi}$$

ServiceStress = "OK!"

$$d_c = 3.58 \cdot \text{in}$$

$$\beta_s = 1.06$$

If the compression force does not act over a rectangular area, j will not be $1-k/3$.

Service Load Bending Stress in outer layer of the reinforcing

Allowable Bending Stress in the outer layer of the reinforcing (BDM-LRFD Ch. 4, Sect. 5, Design Criteria)

"cover" is measured to center of shear reinforcement.

For class 1 exposure conditions. For areas where deicing chemicals are frequently used, design for Class 2 Exposure ($\gamma_e = 0.75$). (BDM-LRFD, Ch. 4, Sect. 5, Design Criteria)

(AASHTO LRFD Eq. 5.7.3.4-1)

A good practice is to place a bar every 12in along each surface of the bent. (TxSP)

Flexural Reinforcement for Positive Bending

(Bars B)

(Tension in Bottom)

$$M_{dl} = M_{posDL}$$

$$M_{dl} = 250.1 \cdot \text{kip} \cdot \text{ft}$$

$$M_s = M_{posServ}$$

$$M_s = 492.5 \cdot \text{kip} \cdot \text{ft}$$

From Cap 18 Output. See Pg. 10

$$M_u = M_{posUlt}$$

$$M_u = 741.7 \cdot \text{kip} \cdot \text{ft}$$

Minimum Flexural Reinforcement (AASHTO LRFD 5.7.3.3.2)

Factored Flexural Resistance, M_r , must be greater than or equal to the lesser of $1.2 M_{cr}$ (Cracking Moment) or $1.33 M_u$ (Ultimate Moment)

$$y_t = \bar{y}$$

$$y_t = 33.80 \cdot \text{in}$$

Distance to the Center of Gravity of the Cap from the top of the Cap
See Pg. 6 for calculations of " \bar{y} "

$$S = \frac{I_g}{y_t}$$

$$S = 8.62 \times 10^4 \cdot \text{in}^3$$

Section Modulus for the extreme tension fiber

$$M_{cr} = S \cdot f_r \cdot \frac{1\text{ft}}{12\text{in}}$$

$$M_{cr} = 3269.9 \cdot \text{kip} \cdot \text{ft}$$

Cracking Moment
(AASHTO LRFD Eq. 5.7.3.3.2-1)

M_f = minimum of:

$$1.2 \cdot M_{cr} = 3923.9 \cdot \text{kip} \cdot \text{ft}$$

Design for the lesser of $1.2M_{cr}$ or $1.33M_u$ when determining minimum area of steel required.

$$1.33 \cdot M_u = 986.5 \cdot \text{kip} \cdot \text{ft}$$

Thus, M_r must be greater than

$$M_f = 986.5 \cdot \text{kip} \cdot \text{ft}$$

Moment Capacity Design

(AASHTO LRFD 5.7.3.2)

Try, 11 ~ #11's Bottom

$$\text{BarBNo} = 11$$

Number of bars in tension

$$d_{\text{bar}_B} = 1.41\text{in}$$

Diameter of main reinforcing bars

$$A_{\text{bar}_B} = 1.56\text{in}^2$$

Area of one main reinforcing bar

$$A_s = (\text{BarBNo}) \cdot A_{\text{bar}_B}$$

$$A_s = 17.16 \cdot \text{in}^2$$

Area of steel in tension

$$d = d_{s_pos}$$

$$d = 81.42 \cdot \text{in}$$

See Pg. 18 for the calculation of " d_{s_pos} "

$$b = b_{\text{stem}}$$

$$b = 39 \cdot \text{in}$$

See Pg. 3 for the calculation of " b_{stem} "

$$c = \frac{A_s \cdot f_y}{0.85 \cdot f_c \cdot \beta_1 \cdot b}$$

$$c = 10.15 \cdot \text{in}$$

Depth of Cross Section under Compression under Ultimate Load
(AASHTO LRFD Eq. 5.7.3.1.2-4)

This " c " is the distance from the extreme compression fiber to the neutral axis, not the distance from the center of bearing of the last girder to the end of the cap.

$$a = c \cdot \beta_1$$

$$a = 8.63 \cdot \text{in}$$

Depth of Equivalent Stress Block
(AASHTO LRFD 5.7.2.2)

Note: " a " is less than " d_{stem} " therefore the equivalent stress block acts over a rectangular area. If " a " was greater than " d_{stem} " it would act over a Tee shaped area.

$$M_n = A_s \cdot f_y \cdot \left(d - \frac{a}{2} \right) \cdot \frac{1\text{ft}}{12\text{in}}$$

$$M_n = 6615.7 \cdot \text{kip} \cdot \text{ft}$$

Nominal Flexural Resistance
(AASHTO LRFD Eq. 5.7.3.2.2-1)

Flexural Reinforcement for Positive Bending (Con't) (Bars B)

Moment Capacity Design (Con't)

$$\epsilon_s = 0.003 \cdot \frac{d - c}{c} \quad \epsilon_s = 0.021 \quad \text{Strain in Reinforcing at Ultimate}$$

$$\epsilon_s > 0.005$$

FlexureBehavior = "Tension Controlled"

(AASHTO LRFD 5.7.2.1)

$$\phi_M = 0.90$$

(AASHTO LRFD 5.5.4.2.1)

$$M_r = \phi_M \cdot M_n$$

$$M_r = 5954.1 \cdot \text{kip} \cdot \text{ft} \quad \text{Factored Flexural Resistance (AASHTO LRFD Eq. 5.7.3.2.1-1)}$$

$$M_u = 741.7 \cdot \text{kip} \cdot \text{ft} < M_r$$

MinReinfChk = "OK!"

$$M_f = 986.5 \cdot \text{kip} \cdot \text{ft} < M_r$$

UltimateMom = "OK!"

Check Serviceability (AASHTO LRFD 5.7.3.4)

To find s_{\max} :

$$d_c = \text{cover} + \frac{1}{2} \cdot d_{\text{stirrup}} + \frac{1}{2} \cdot d_{\text{bar}_B} \quad d_c = 3.58 \cdot \text{in}$$

"cover" is measured to center of shear reinforcement.

Tension Reinforcement Ratio:

$$\rho = \frac{A_s}{b \cdot d}$$

$$\rho = 0.0054$$

For service loads, the stress on the cross-section is located as drawn:

$$k = \sqrt{(2 \cdot \rho \cdot n) + (\rho \cdot n)^2} - (\rho \cdot n)$$

$$k = 0.259$$

$$d \cdot k = 21.10 \cdot \text{in} < d_{\text{stem}} = 57.00 \cdot \text{in}$$

Therefore, the compression force acts over a rectangular area.

$$j = 1 - \frac{k}{3}$$

$$j = 0.914$$

$$f_{ss} = \frac{M_s}{A_s \cdot j \cdot d} \cdot \frac{12 \text{in}}{1 \text{ft}}$$

$$f_{ss} = 4.63 \cdot \text{ksi}$$

Service Load Bending Stress in outer layer of the reinforcing

$$f_a = 0.6 \cdot f_y$$

$$f_a = 36.00 \cdot \text{ksi}$$

Allowable Bending Stress in the outer layer of the reinforcing (BDM-LRFD Ch. 4, Sect. 5, Design Criteria)

$$f_{ss} < f_a$$

ServiceStress = "OK!"

Exposure Condition Factor:

$$\gamma_e = 1.00$$

$$\beta_s = 1 + \frac{d_c}{0.7 \cdot (h_{\text{cap}} - d_c)}$$

$$\beta_s = 1.06$$

For class 1 exposure conditions. For areas where deicing chemicals are frequently used, design for Class 2 Exposure ($\gamma_e = 0.75$). (BDM-LRFD, Ch. 4, Sect. 5, Design Criteria)

s_{\max} = minimum of:

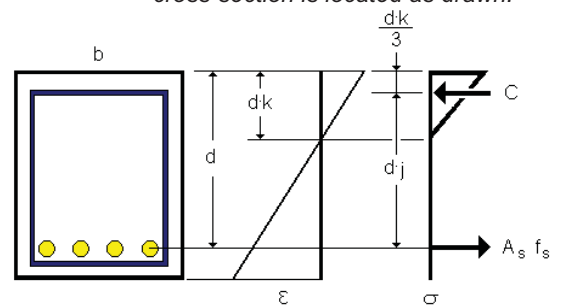
$$\frac{700 \gamma_e}{\beta_s \cdot f_{ss}} - 2d_c = 135.09 \cdot \text{in}$$

(AASHTO LRFD Eq. 5.7.3.4-1)

& 12in

A good practice is to place a bar every 12in along each surface of the bent. (TxSP)

$$s_{\max} = 12.00 \cdot \text{in}$$



Flexural Reinforcement for Positive Bending (Con't) (Bars B)

Check Serviceability (Con't)

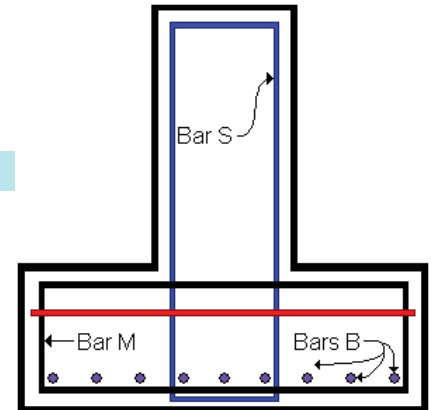
Bars Inside Stirrup Bar S

Try: BarBInsideSNo = 5

$$s_{\text{Actual}} = \frac{b_{\text{stem}} - 2 \cdot \left(\text{cover} + \frac{1}{2} \cdot d_{\text{bar}_S} + \frac{1}{2} \cdot d_{\text{bar}_B} \right)}{\text{BarBInsideSNo} - 1}$$

$$s_{\text{Actual}} = 7.96 \cdot \text{in} < s_{\text{max}} \quad \text{ServiceabilityCheck} = \text{"OK!"}$$

Number of bars B that are inside Stirrup bar S.



Number of bars B that are Outside Stirrup bar S.

Bars Outside Stirrup Bar S

$$\text{BarBOutsideSNo} = \text{BarBNo} - \text{BarBInsideSNo}$$

$$\text{BarBOutsideSNo} = 6$$

$$s_{\text{Actual}} = \frac{2b_{\text{ledge}} + 2 \cdot \left(\text{cover} + \frac{1}{2} \cdot d_{\text{bar}_S} + \frac{1}{2} \cdot d_{\text{bar}_B} - \text{cover} - \frac{1}{2} \cdot d_{\text{bar}_M} - \frac{1}{2} \cdot d_{\text{bar}_B} \right)}{\text{BarBOutsideSNo}}$$

$$s_{\text{Actual}} = 8.67 \cdot \text{in} < s_{\text{max}} \quad \text{ServiceabilityCheck} = \text{"OK!"}$$

Check Dead Load BDM-LRFD, Chapter 4, Section 5, Design Criteria

Check allowable M_{dl} : $f_{dl} = 22 \text{ksi}$

TxDOT limits dead load stress to 22 ksi. This is due to observed cracking under dead load.

$$M_a = A_s \cdot d \cdot j \cdot f_{dl} \cdot \frac{1 \text{ft}}{12 \text{in}}$$

$$M_a = 2340.19 \cdot \text{kip} \cdot \text{ft} \quad \text{Allowable Dead Load Moment}$$

$$M_{dl} = 250.10 \cdot \text{kip} \cdot \text{ft} < M_a$$

$$\text{DeadLoadMom} = \text{"OK!"}$$

Flexural Steel Summary:

Use 5~#11 Bars on Top
& 11~#11 Bars on Bottom

Ledge Reinforcement (Bars M&N)

Try Bars M at a 4.95" spacing, and Bars N at a 9.90" spacing.

$$s_{\text{bar}_M} = 4.95\text{in}$$

$$s_{\text{bar}_N} = 9.90\text{in}$$

Use trial and error to determine the spacing needed for the ledge reinforcing. Bars M @ 5" and Bars N @ 10" failed one of the checks by a small margin (1%). 4.95" spacing was chosen because it should pass all the checks.

It is typical for Bars N to be at every other Bar M.

Determine Distribution Widths

These distribution widths will be used on the following three pages to determine the required ledge reinforcement per foot of cap.

Distribution Width for Shear (AASHTO LRFD 5.13.2.5.2)

Note: These are the same distribution widths used for the Shear Friction check on Pg. 22.

Interior Girders

$$b_{s_Int} = \text{minimum of:}$$

$$W + 4 a_v = 69.00 \cdot \text{in}$$

$$S = 96.00 \cdot \text{in}$$

$$b_{s_Int} = 69.00 \cdot \text{in}$$

*"S" is the girder spacing.
(From Pg. 6)*

Exterior Girders

$$b_{s_Ext} = \text{minimum of:}$$

$$W + 4 a_v = 69.00 \cdot \text{in}$$

$$S = 96.00 \cdot \text{in}$$

$$2 c = 48.00 \cdot \text{in}$$

$$b_{s_Ext} = 48.00 \cdot \text{in}$$

"c" is the distance from the center of bearing of the outside beam to the end of the ledge. (From Pg. 6)

Distribution Width for Bending and Axial Loads (AASHTO LRFD 5.13.2.5.3)

Interior Girders

$$b_{m_Int} = \text{minimum of:}$$

$$W + 5 a_f = 93.50 \cdot \text{in}$$

$$S = 96.00 \cdot \text{in}$$

$$b_{m_Int} = 93.50 \cdot \text{in}$$

Exterior Girders

$$b_{m_Ext} = \text{minimum of:}$$

$$W + 5 a_f = 93.50 \cdot \text{in}$$

$$S = 96.00 \cdot \text{in}$$

$$2 c = 48.00 \cdot \text{in}$$

$$b_{m_Ext} = 48.00 \cdot \text{in}$$

Ledge Reinforcement (Con't) (Bars M&N)

The reinforcing required for shear friction, flexure, and axial tension will be calculated on Pgs. 30-32. The reinforcing provided by Bars M and Bars N must exceed the checks that are found on the bottom of Pg. 32 (These checked can be found on pages 33 and 34). These checks combine the reinforcing requirements for shear friction, flexure, and axial tension, as per AASHTO LRFD 5.13.2.4.2.

Reinforcing Required for Shear Friction (AASHTO LRFD 5.8.4.1)

$$\phi = 0.9$$

(AASHTO LRFD 5.5.4.2.1)

$$\mu = 1.4 \quad c_1 = 0 \text{ksi} \quad P_c = 0 \text{kip}$$

" μ " is 1.4 for monolithically placed concrete. (AASHTO LRFD 5.8.4.3)

Recall: $d_e = 25.5 \text{in}$ (From Pg. 18)

For clarity, the cohesion factor is labeled " c_1 ". This is to prevent confusion with " c ", the distance from the last girder to the edge of the cap. c_1 is 0ksi for corbels and ledges. (AASHTO LRFD 5.8.4.3)

Minimum Reinforcing (AASHTO LRFD 5.8.4.4-1)

$$A_{vf_min} = \frac{0.05 \text{ ksi} \cdot A_{cv}}{f_y}$$

(AASHTO LRFD 5.8.4.3)

$$A_{cv} = d_e \cdot b_s \quad \text{and} \quad a_{vf} = \frac{A_{vf}}{b_s}$$

" P_c " is zero as there is no axial compression.

$$a_{vf_min} = \frac{0.05 \text{ ksi} \cdot d_e}{f_y}$$

$$a_{vf_min} = 0.26 \cdot \frac{\text{in}^2}{\text{ft}} \quad \text{Minimum Reinforcing required for Shear Friction}$$

Interior Girders

$$A_{cv} = d_e \cdot b_{s_Int}$$

$$A_{cv} = 1759 \cdot \text{in}^2$$

$$V_{u_Int} = 322 \cdot \text{kip}$$

From Pg. 16

$$V_n = c_1 \cdot A_{cv} + \mu \cdot (A_{vf} \cdot f_y + P_c)$$

(AASHTO LRFD Eq. 5.8.4.1-3)

$$\phi V_n \geq V_u$$

(AASHTO LRFD Eq. 5.8.4.1-1 & AASHTO LRFD Eq. 5.8.4.1-2)

$$\phi \cdot [c_1 \cdot A_{cv} + \mu \cdot (A_{vf} \cdot f_y + P_c)] \geq V_u$$

$$A_{vf} = \left[(V_{u_Int} \div \phi - c_1 \cdot A_{cv}) \div \mu - P_c \right] \div f_y \quad A_{vf} = 4.26 \cdot \text{in}^2$$

Required Reinforcing for Shear Friction

$$a_{vf_Int} = \frac{A_{vf}}{b_{s_Int}}$$

$$a_{vf_Int} = 0.74 \cdot \frac{\text{in}^2}{\text{ft}} \quad \text{Required Reinforcing for Shear Friction per foot length of cap}$$

Exterior Girders

$$A_{cv} = d_e \cdot b_{s_Ext}$$

$$A_{cv} = 1224 \cdot \text{in}^2$$

$$V_{u_Ext} = 322 \cdot \text{kip}$$

From Pg. 16

$$V_n = c_1 \cdot A_{cv} + \mu \cdot (A_{vf} \cdot f_y + P_c)$$

(AASHTO LRFD Eq. 5.8.4.1-3)

$$\phi V_n \geq V_u$$

(AASHTO LRFD Eq. 5.8.4.1-1 & AASHTO LRFD Eq. 5.8.4.1-2)

$$\phi \cdot [c_1 \cdot A_{cv} + \mu \cdot (A_{vf} \cdot f_y + P_c)] \geq V_u$$

$$A_{vf} = \left[(V_{u_Ext} \div \phi - c_1 \cdot A_{cv}) \div \mu - P_c \right] \div f_y \quad A_{vf} = 4.26 \cdot \text{in}^2$$

Required Reinforcing for Shear Friction

$$a_{vf_Ext} = \frac{A_{vf}}{b_{s_Ext}}$$

$$a_{vf_Ext} = 1.06 \cdot \frac{\text{in}^2}{\text{ft}} \quad \text{Required Reinforcing for Shear Friction per foot length of cap}$$

Ledge Reinforcement (Con't) (Bars M&N)

Reinforcing Required for Flexure

(AASHTO LRFD 5.13.2.4.1)

Recall: $h = 29.50 \cdot \text{in}$ $d_e = 25.5 \cdot \text{in}$ $a_v = 12.00 \cdot \text{in}$

From Pg. 18

Interior Girders

$$V_{u_Int} = 322 \cdot \text{kip}$$

From Pg. 16

$$N_{uc_Int} = 0.2 \cdot V_{u_Int}$$

$$N_{uc_Int} = 64.37 \cdot \text{kip} \quad (\text{AASHTO LRFD 5.13.2.4.1})$$

$$M_{u_Int} = V_{u_Int} \cdot a_v + N_{uc_Int} \cdot (h - d_e)$$

$$M_{u_Int} = 343.3 \cdot \text{kip} \cdot \text{ft} \quad (\text{AASHTO LRFD Eq. 5.13.2.4.1-1})$$

Use the below equations to solve for A_f :

$$\phi M_n \geq M_{u_Int}$$

(AASHTO LRFD Eq. 1.3.2.1-1)

$$M_n = A_f \cdot f_y \cdot \left(d_e - \frac{a}{2} \right)$$

(AASHTO LRFD Eq. 5.7.3.2.2-1)

$$c = \frac{A_f \cdot f_y}{0.85 \cdot f_c \cdot \beta_1 \cdot b_{m_Int}}$$

(AASHTO LRFD Eq. 5.7.3.1.2-4)

This "c" is the distance from the extreme compression fiber to the neutral axis, not the distance from the center of bearing of the last girder to the end of the cap.

$$\beta_1 = 0.85$$

$$a = c \cdot \beta_1$$

(AASHTO LRFD Eq. 5.7.2.2)

$$\phi = 0.65 - 0.15 \cdot \left(\frac{d_e}{c} - 1 \right)$$

Bounded by: $0.75 \leq \phi \leq 0.9$ (AASHTO LRFD 5.5.4.2.1)

Solve for A_f :

$$A_f = 3.03 \cdot \text{in}^2$$

Required Reinforcing for Flexure

$$a_{f_Int} = \frac{A_f}{b_{m_Int}}$$

$$a_{f_Int} = 0.39 \cdot \frac{\text{in}^2}{\text{ft}}$$

Required Reinforcing for Flexure per foot length of cap

Exterior Girders

$$V_{u_Ext} = 322 \cdot \text{kip}$$

From Pg. 16

$$N_{uc_Ext} = 0.2 \cdot V_{u_Ext}$$

$$N_{uc_Ext} = 64.37 \cdot \text{kip} \quad (\text{AASHTO LRFD 5.13.2.4.1})$$

$$M_{u_Ext} = V_{u_Ext} \cdot a_v + N_{uc_Ext} \cdot (h - d_e)$$

$$M_{u_Ext} = 343.3 \cdot \text{kip} \cdot \text{ft} \quad (\text{AASHTO LRFD Eq. 5.13.2.4.1-1})$$

Use the below equations to solve for A_f :

$$\phi M_n \geq M_{u_Ext}$$

(AASHTO LRFD Eq. 1.3.2.1-1)

$$M_n = A_f \cdot f_y \cdot \left(d_e - \frac{a}{2} \right)$$

(AASHTO LRFD Eq. 5.7.3.2.2-1)

$$c = \frac{A_f \cdot f_y}{0.85 \cdot f_c \cdot \beta_1 \cdot b_{m_Ext}}$$

(AASHTO LRFD Eq. 5.7.3.1.2-4)

This "c" is the distance from the extreme compression fiber to the neutral axis, not the distance from the center of bearing of the last girder to the end of the cap.

$$\beta_1 = 0.85$$

$$a = c \cdot \beta_1$$

(AASHTO LRFD Eq. 5.7.2.2)

$$\phi = 0.65 - 0.15 \cdot \left(\frac{d_e}{c} - 1 \right)$$

Bounded by: $0.75 \leq \phi \leq 0.9$ (AASHTO LRFD 5.5.4.2.1)

Solve for A_f :

$$A_f = 3.07 \cdot \text{in}^2$$

Required Reinforcing for Flexure

$$a_{f_Ext} = \frac{A_f}{b_{m_Ext}}$$

$$a_{f_Ext} = 0.77 \cdot \frac{\text{in}^2}{\text{ft}}$$

Required Reinforcing for Flexure per foot length of cap

Ledge Reinforcement (Con't) (Bars M&N)

Reinforcing Required for Axial Tension (AASHTO LRFD 5.13.2.4.2)

$$\phi = 0.9 \quad (\text{AASHTO LRFD 5.5.4.2.1})$$

Interior Girders

$$N_{uc_Int} = 64.37 \cdot \text{kip}$$

From Pg. 31

$$A_n = \frac{N_{uc_Int}}{\phi \cdot f_y}$$

$$A_n = 1.19 \cdot \text{in}^2$$

Required Reinforcing for Axial Tension
(AASHTO LRFD Eq. 5.13.2.4.2-7)

$$a_{n_Int} = \frac{A_n}{b_{m_Int}}$$

$$a_{n_Int} = 0.15 \cdot \frac{\text{in}^2}{\text{ft}}$$

Required Reinforcing for Axial Tension per foot length of cap

Exterior Girders

$$N_{uc_Ext} = 64.37 \cdot \text{kip}$$

From Pg. 31

$$A_n = \frac{N_{uc_Ext}}{\phi \cdot f_y}$$

$$A_n = 1.19 \cdot \text{in}^2$$

Required Reinforcing for Axial Tension
(AASHTO LRFD Eq. 5.13.2.4.2-7)

$$a_{n_Ext} = \frac{A_n}{b_{m_Ext}}$$

$$a_{n_Ext} = 0.30 \cdot \frac{\text{in}^2}{\text{ft}}$$

Required Reinforcing for Axial Tension per foot length of cap

Minimum Reinforcing (AASHTO LRFD 5.13.2.4.1)

$$a_{s_min} = 0.04 \cdot \frac{f_c}{f_y} \cdot d_e$$

$$a_{s_min} = 0.73 \cdot \frac{\text{in}^2}{\text{ft}}$$

Minimum Required Reinforcing
(AASHTO LRFD 5.13.2.4.1)

Check Required Reinforcing (AASHTO LRFD 5.13.2.4)

Actual Reinforcing:

$$a_s = \frac{A_{bar_M}}{s_{bar_M}}$$

$$a_s = 1.07 \cdot \frac{\text{in}^2}{\text{ft}}$$

Primary Ledge Reinforcing Provided

$$a_h = \frac{A_{bar_N}}{s_{bar_N}}$$

$$a_h = 0.53 \cdot \frac{\text{in}^2}{\text{ft}}$$

Auxiliary Ledge Reinforcing Provided

The area of one bar M and N can be found on Pg. 18. The spacing of bars M and N can be found on Pg. 29.

Checks:

$$A_s \geq A_{s_min}$$

(AASHTO LRFD 5.13.2.4.1)

$$A_s \geq A_f + A_n$$

(AASHTO LRFD 5.13.2.4.2)

$$A_s \geq \frac{2 \cdot A_{vf}}{3} + A_n$$

(AASHTO LRFD Eq. 5.13.2.4.2-5)

$$A_h \geq 0.5 \cdot (A_s - A_n)$$

(AASHTO LRFD Eq. 5.13.2.4.2-6)

Ledge Reinforcement (Con't) (Bars M&N)

Check Required Reinforcing (Con't)

The following checks bars M and N. These are the checks found on Pg. 32, modified to check the steel per unit length instead of the total steel.

Check Interior Girders

Bar M:

$$\text{Check if: } a_s \geq a_{s_min} \quad (\text{AASHTO LRFD 5.13.2.4.1})$$

$$a_s \geq a_{f_Int} + a_{n_Int} \quad (\text{AASHTO LRFD 5.13.2.4.2})$$

$$a_s \geq \frac{2 \cdot a_{vf_Int}}{3} + a_{n_Int} \quad (\text{AASHTO LRFD Eq. 5.13.2.4.2-5})$$

$$a_s = 1.07 \cdot \frac{\text{in}^2}{\text{ft}}$$

$$a_{s_min} = 0.73 \cdot \frac{\text{in}^2}{\text{ft}} < a_s$$

$$a_{f_Int} + a_{n_Int} = 0.54 \cdot \frac{\text{in}^2}{\text{ft}} < a_s$$

$$\frac{2 \cdot a_{vf_Int}}{3} + a_{n_Int} = 0.65 \cdot \frac{\text{in}^2}{\text{ft}} < a_s$$

BarMCheck = "OK!"

Bar N:

$$\text{Check if: } a_h \geq 0.5 \cdot (a_s - a_{n_Int}) \quad (\text{AASHTO LRFD Eq. 5.13.2.4.2-6})$$

a_s = The maximum of:

$$a_{f_Int} + a_{n_Int}$$

$$\frac{2 \cdot a_{vf_Int}}{3} + a_{n_Int}$$

$$a_s = 0.54 \cdot \frac{\text{in}^2}{\text{ft}}$$

$$a_h = 0.53 \cdot \frac{\text{in}^2}{\text{ft}}$$

$$0.5 \cdot (a_s - a_{n_Int}) = 0.19 \cdot \frac{\text{in}^2}{\text{ft}} < a_h$$

BarNCheck = "OK!"

" a_s " in this equation is the steel required for Bar M, based on the requirements for Bar M in AASHTO LRFD 5.13.2.4.2.

This is derived from the suggestion that A_h should not be less than $A_f/2$ nor less than $A_{vf}/3$ (Furlong & Mirza pg. 73 & 74)

Ledge Reinforcement (Con't) (Bars M&N)

Check Required Reinforcing (Con't)

Check Exterior Girders

Bar M

Check if: $a_s \geq a_{s_min}$ (AASHTO LRFD 5.13.2.4.1)

$$a_s \geq a_{f_Ext} + a_{n_Ext} \quad (\text{AASHTO LRFD 5.13.2.4.2})$$

$$a_s \geq \frac{2 \cdot a_{vf_Ext}}{3} + a_{n_Ext} \quad (\text{AASHTO LRFD Eq. 5.13.2.4.2-5})$$

$$a_s = 1.07 \cdot \frac{\text{in}^2}{\text{ft}}$$

$$a_{s_min} = 0.73 \cdot \frac{\text{in}^2}{\text{ft}} < a_s$$

$$a_{f_Ext} + a_{n_Ext} = 1.06 \cdot \frac{\text{in}^2}{\text{ft}} < a_s$$

$$\frac{2 \cdot a_{vf_Ext}}{3} + a_{n_Ext} = 1.01 \cdot \frac{\text{in}^2}{\text{ft}} < a_s$$

BarMCheck = "OK!"

Bar N

Check if: $a_h \geq 0.5 \cdot (a_s - a_{n_Int})$ (AASHTO LRFD Eq. 5.13.2.4.2-6)

a_s = The maximum of:

$$a_{f_Int} + a_{n_Int}$$

$$\frac{2 \cdot a_{vf_Int}}{3} + a_{n_Int}$$

$$a_s = 1.06 \cdot \frac{\text{in}^2}{\text{ft}}$$

$$a_h = 0.53 \cdot \frac{\text{in}^2}{\text{ft}}$$

$$0.5 \cdot (a_s - a_{n_Int}) = 0.46 \cdot \frac{\text{in}^2}{\text{ft}} < a_h$$

BarNCheck = "OK!"

Ledge Reinforcement Summary:

Use #6 primary ledge reinforcing @ 4.95" maximum spacing
& #6 auxiliary ledge reinforcing @ 9.90" maximum spacing

Hanger Reinforcement (Bars S)

Try Double # 6 Stirrups at a 8" spacing.

$$s_{\text{bar}_S} = 8.5\text{in}$$

$$A_{\text{hr}} = 2\text{stirrups} \cdot A_{\text{bar}_S}$$

$$A_V = 2\text{legs} \cdot A_{\text{hr}}$$

$$A_{\text{hr}} = 0.88 \cdot \text{in}^2$$

$$A_V = 1.76 \cdot \text{in}^2$$

Use trial and error to determine the spacing needed for the hanger reinforcing.

A_{hr} is the area of one leg of hanger reinforcement. In this example the area of the bar is multiplied by 2 because the Inverted Tee has double stirrups.

Check Minimum Transverse Reinforcement

$$b_V = b_{\text{stem}}$$

$$b_V = 39.00 \cdot \text{in}$$

$$A_{V_{\text{min}}} = 0.0316 \cdot \sqrt{f_c} \cdot \frac{b_V \cdot s_{\text{bar}_S}}{f_y}$$

$$A_{V_{\text{min}}} = 0.33 \cdot \text{in}^2 \quad (\text{AASHTO LRFD Eq. 5.8.2.5-1})$$

$$A_V = 1.76 \cdot \text{in}^2 > A_{V_{\text{min}}}$$

MinimumSteelCheck = "OK!"

Check Service Limit State

(AASHTO LRFD 5.13.2.5.5 with modifications from BDM-LRFD Ch.4, Sect. 5, Design Criteria)

Interior Girders

V_{all} = minimum of:

$$\frac{A_{\text{hr}} \cdot \left(\frac{2}{3} \cdot f_y\right)}{s_{\text{bar}_S}} \cdot (W + 3 \cdot a_V) = 236 \cdot \text{kip}$$

$$\frac{A_{\text{hr}} \cdot \left(\frac{2}{3} \cdot f_y\right)}{s_{\text{bar}_S}} \cdot S = 398 \cdot \text{kip}$$

$$V_{\text{all}} = 236 \cdot \text{kip}$$

$$V_{s_{\text{Int}}} = 215 \cdot \text{kip} < V_{\text{all}}$$

TxDOT uses " $\frac{2}{3} f_y$ " from the original research (Furlong & Mirza Eq. 5.4) instead of " $0.5 f_y$ " from AASHTO LRFD Eq. 5.13.2.5.5-1.

(BDM-LRFD Ch.4, Sect. 5, Design Criteria)

(BDM-LRFD Ch.4, Sect. 5, Design Criteria ~ Modified to limit the distribution width to the girder spacing. This will prevent distribution widths from overlapping)

ServiceCheck = "OK!"

Exterior Girders

V_{all} = minimum of:

V_{all} for the interior girder

$$\frac{A_{\text{hr}} \cdot \left(\frac{2}{3} \cdot f_y\right)}{s_{\text{bar}_S}} \cdot \left(\frac{W + 3 \cdot a_V}{2} + c\right) = 217 \cdot \text{kip}$$

$$\frac{A_{\text{hr}} \cdot \left(\frac{2}{3} \cdot f_y\right)}{s_{\text{bar}_S}} \cdot \left(\frac{S}{2} + c\right) = 298 \cdot \text{kip}$$

$$V_{\text{all}} = 217 \cdot \text{kip}$$

$$V_{s_{\text{Ext}}} = 215 \cdot \text{kip} < V_{\text{all}}$$

ServiceCheck = "OK!"

(BDM-LRFD Ch.4, Sect. 5, Design Criteria ~ Modified to limit the distribution width to the edge of the cap. This will prevent distribution widths from extending over the edge of the cap.)

(BDM-LRFD Ch.4, Sect. 5, Design Criteria ~ Modified to limit the distribution width to half the girder spacing and the distance to the edge of the cap. This will prevent distribution widths from overlapping or extending over the edge of the cap.)

Hanger Reinforcement (Con't) (Bars S)

Check Strength Limit State (AASHTO LRFD 5.13.2.5.5)

(AASHTO LRFD 5.5.4.2.1)

$$\phi = 0.9$$

Interior Girders

V_n = minimum of:

$$\frac{A_{hr} \cdot f_y}{s_{bar_S}} \cdot S = 596 \cdot \text{kip} \quad (\text{AASHTO LRFD Eq. 5.13.2.5.5-2})$$

$$\left(0.063 \cdot \sqrt{f_c} \cdot b_f \cdot d_f\right) + \frac{A_{hr} \cdot f_y}{s_{bar_S}} \cdot (W + 2 \cdot d_f) = 699 \cdot \text{kip} \quad (\text{AASHTO LRFD Eq. 5.13.2.5.5-3})$$

$$V_n = 596 \cdot \text{kip}$$

$$\phi V_n = 537 \cdot \text{kip}$$

$$V_{u_Int} = 322 \cdot \text{kip} < \phi V_n$$

UltimateCheck = "OK!"

Exterior Girders

V_n = minimum of:

V_n for the interior girder

$$\frac{A_{hr} \cdot f_y}{s_{bar_S}} \cdot \left(\frac{S}{2} + c\right) = 447 \cdot \text{kip} \quad (\text{AASHTO LRFD Eq. 5.13.2.5.5-2})$$

Modified to limit the distribution width to the edge of the cap.

$$\left(0.063 \cdot \sqrt{f_c} \cdot b_f \cdot d_f\right) + \frac{A_{hr} \cdot f_y}{s_{bar_S}} \cdot \left(\frac{W + 2 \cdot d_f}{2} + c\right) = 632 \cdot \text{kip} \quad (\text{AASHTO LRFD Eq. 5.13.2.5.5-3})$$

Modified to limit the distribution width to the edge of the cap.

$$V_n = 447 \cdot \text{kip}$$

$$\phi V_n = 403 \cdot \text{kip}$$

$$V_{u_Ext} = 322 \cdot \text{kip} < \phi V_n$$

UltimateCheck = "OK!"

Hanger Reinforcement (Con't) (Bars S)

Combined Shear and Torsion

The following calculations are for Station 36. All critical locations must be checked. See the the Concrete Section Shear Capacity spreadsheet in the appendices for calculations at other locations. Shear and Moments were calculated using the CAP 18 program.

$$M_u = 335.6 \text{ kip}\cdot\text{ft} \quad V_u = 448.1 \cdot \text{kip} \quad N_u = 0 \text{ kip} \quad T_u = 660 \cdot \text{kip}\cdot\text{ft} \quad \text{These loads can be found on Pg. 16}$$

$$\begin{aligned} \text{Recall: } \beta_1 &= 0.85 & f_y &= 60 \cdot \text{ksi} \\ f_c &= 3.6 \cdot \text{ksi} & E_s &= 29000 \cdot \text{ksi} \\ b_f &= 91 \cdot \text{in} & h_{\text{cap}} &= 85 \cdot \text{in} & b_{\text{stem}} &= 39 \cdot \text{in} \end{aligned}$$

$$b_v = b_{\text{stem}} \quad b_v = 39.00 \cdot \text{in}$$

Find d_v :

$$A_s = A_{\text{bar}_A} \cdot \text{BarANo} \quad A_s = 7.80 \cdot \text{in}^2$$

$$c = \frac{A_s \cdot f_y}{0.85 \cdot f_c \cdot \beta_1 \cdot b_f} \quad c = 1.98 \cdot \text{in}$$

$$a = c \cdot \beta_1 \quad a = 1.68 \cdot \text{in}$$

$$d_s = d_{s_neg} \quad d = 81.42 \cdot \text{in}$$

$$M_n = A_s \cdot f_y \cdot \left(d - \frac{a}{2} \right) \quad M_n = 3142.6 \cdot \text{kip}\cdot\text{ft}$$

$$A_{ps} = 0 \text{ in}^2$$

$$d_e = \frac{A_{ps} \cdot f_{ps} \cdot d_p + A_s \cdot f_y \cdot d_s}{A_{ps} \cdot f_{ps} + A_s \cdot f_y} \quad d_e = 81.42 \cdot \text{in} \quad (\text{AASHTO LRFD Eq. 5.8.2.9-2})$$

d_v need not be less than the greater of $0.9d_e$ and $0.72h$: (AASHTO LRFD 5.8.2.9)

d_v = maximum of:

$$\frac{M_n}{A_s \cdot f_y + A_{ps} \cdot f_{ps}} = 80.58 \cdot \text{in} \quad (\text{AASHTO LRFD Eq. C5.8.2.9-1})$$

$$0.9 \cdot d_e = 73.28 \cdot \text{in}$$

$$0.72 \cdot h = 21.24 \cdot \text{in}$$

$$d_v = 80.58 \cdot \text{in}$$

The method for calculating θ and β used in this design example are from AASHTO LRFD Appendix B5. The method from AASHTO LRFD 5.8.3.4.2 may be used instead. The method from 5.8.3.4.2 is based on the method from Appendix B5; however, it is less accurate and more conservative (often excessively conservative). The method from Appendix B5 is preferred because it is more accurate, but it requires iterating to a solution. The method from 5.8.3.4.2 can be used when doing calculations by hand.

Hanger Reinforcement (Con't) (Bars S)

Check Combined Shear and Torsion (Con't)

Determine θ and β :

$$\phi_V = 0.9$$

(AASHTO LRFD 5.5.4.2.1)

$$v_u = \frac{|V_u - (\phi_V \cdot V_p)|}{\phi_V \cdot b_V \cdot d_V}$$

$$v_u = 0.16 \cdot \text{ksi}$$

Shear Stress on the Concrete
(AASHTO LRFD Eq. 5.8.2.9-1)

$$\frac{v_u}{f_c} = 0.04$$

Using Table B5.2-1 with $\frac{v_u}{f_c} = 0.04$ and $\epsilon_x = 0.001$

Determining θ and β is an iterative process, therefore, assume initial shear strain value ϵ_x of 0.001 per LRFD B5.2 and then verify that the assumption was valid.

$$\theta = 36.4 \text{ deg and } \beta = 2.23$$

$$\epsilon_x = \frac{\left(\frac{|M_u|}{d_V} + 0.5 N_u + 0.5 |V_u - V_p| \cot(\theta) - A_{ps} \cdot f_{po} \right)}{2 (E_s \cdot A_s + E_p \cdot A_{ps})}$$

Strain halfway between the compressive and tensile resultants
(AASHTO LRFD Eq. B5.2-1)

where, $|M_u| = 335.60 \cdot \text{kip} \cdot \text{ft}$ Must be $> |V_u - V_p| \cdot d_V = 3008.98 \cdot \text{kip} \cdot \text{ft}$

If $\epsilon_x < 0$, then use equation B5.2-3 and re-solve for ϵ_x .

$$\epsilon_x = 1.66 \cdot 10^{-3} \frac{\text{in}}{\text{in}} > 1.00 \times 10^{-3} \frac{\text{in}}{\text{in}}$$

$$\text{use } \epsilon_x = 1.00 \times 10^{-3} \frac{\text{in}}{\text{in}}$$

For values of ϵ_x greater than 0.001, the tensile strain in the reinforcing, ϵ_t is greater than 0.002.

($\epsilon_t = 2 \epsilon_x - \epsilon_c$, where ϵ_c is < 0)

Grade 60 steel yields at a strain of 60 ksi / 29,000 ksi = 0.002.

By limiting the tensile strain in the steel to the yield strain and using the Modulus of Elasticity of the steel prior to yield, this limits the tensile stress of the steel to the yield stress. ϵ_x has not changed from the assumed value, therefore no iterations are required.

$$V_p = 0 \text{ kip}$$

" V_p " is zero as there is no prestressing.

$$A_c = b_{\text{stem}} \cdot \frac{h_{\text{cap}}}{2}$$

$$A_c = 1657.5 \cdot \text{in}^2$$

(AASHTO LRFD B5.2)

" A_c " is the area of concrete on the flexural tension side of the cap, from the extreme tension fiber to one half the cap depth.

$$s = s_{\text{bar}_S}$$

$$s = 8.50 \cdot \text{in}$$

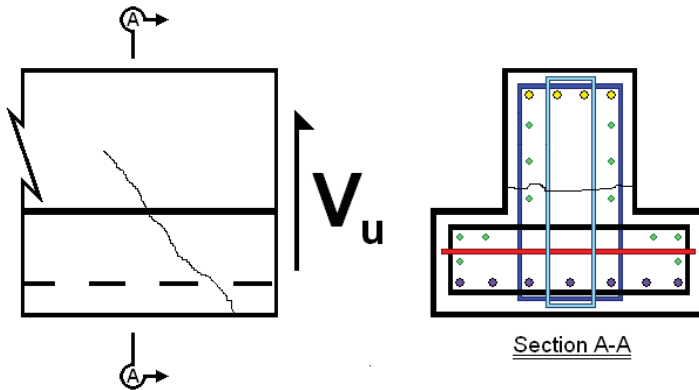
" A_c " is needed if AASHTO LRFD Eq. B5.2-1 is negative.

Hanger Reinforcement (Con't) (Bars S)

Check Combined Shear and Torsion (Con't)

$$A_v = 2 \text{ legs} \cdot 2 \text{ stirrups} \cdot A_{\text{bar}_S}$$

$$A_v = 1.76 \cdot \text{in}^2$$



The transverse reinforcement, " A_v ", is double closed stirrups. The failure surface intersects four stirrup legs, therefore the area of the shear steel is four times the stirrup bar's area (0.44in^2). See the sketch of the failure plane to the left.

$$A_t = 1 \text{ leg} \cdot A_{\text{bar}_S}$$

$$A_t = 0.44 \cdot \text{in}^2$$

" A_t " is the area of the outer stirrup. A_t is not independent of A_v , but it is one leg of the outer stirrup of A_v .

$$A_{oh} = (d_{\text{stem}}) \cdot (b_{\text{stem}} - 2 \cdot \text{cover}) + (d_{\text{ledge}} - 2 \cdot \text{cover}) \cdot (b_f - 2 \cdot \text{cover})$$

" A_{oh} " is the area inside the centerline of the exterior stirrup.

$$A_{oh} = 3916 \cdot \text{in}^2$$

$$A_o = 0.85 \cdot A_{oh}$$

$$A_o = 3329 \cdot \text{in}^2$$

(AASHTO LRFD C5.8.2.1)

$A_o = 0.85 \cdot$ the area inside the centerline of the exterior stirrup.

$$p_h = (b_{\text{stem}} - 2 \cdot \text{cover}) + 2 \cdot (b_{\text{ledge}}) + (b_f - 2 \cdot \text{cover}) + 2 \cdot (h_{\text{cap}} - 2 \cdot \text{cover})$$

" p_h " is the perimeter of the centerline of Bar S.

$$p_h = 332.0 \cdot \text{in}$$

Equivalent Shear Force

$$V_{u_Eq} = \sqrt{V_u^2 + \left(\frac{0.9 \cdot p_h \cdot T_u}{2 \cdot A_o} \right)^2}$$

$$V_{u_Eq} = 572.0 \cdot \text{kip} \quad (\text{AASHTO LRFD Eq. 5.8.2.1-6})$$

Shear Steel Required

V_n = the lesser of:

$$V_c + V_s + V_p$$

(AASHTO LRFD Eq. 5.8.3.3-1)

$$0.25 \cdot f_c \cdot b_v \cdot d_v + V_p$$

(AASHTO LRFD Eq. 5.8.3.3-2)

check maximum ϕV_n for section:

$$\phi V_{n_max} = \phi \cdot (0.25 \cdot f_c \cdot b_v \cdot d_v + V_p)$$

$$\phi V_{n_max} = 2546 \cdot \text{kip}$$

$$V_u = 448.1 \cdot \text{kip} < \phi V_{n_max}$$

MaxShearCheck = "OK!"

Hanger Reinforcement (Con't) (Bars S)

Check Combined Shear and Torsion (Con't)

Shear Steel Required (Con't)

calculate required shear steel:

$$V_u \leq \phi V_n \quad (\text{AASHTO LRFD Eq. 1.3.2.1-1})$$

$$V_c = 0.0316 \cdot \beta \cdot \sqrt{f_c} \cdot b_v \cdot d_v \quad V_c = 420 \cdot \text{kip} \quad (\text{AASHTO LRFD Eq. 5.8.3.3-3})$$

$$V_u \leq \phi (V_c + V_s + V_p)$$

$$V_s = \frac{A_v \cdot f_y \cdot d_v \cdot (\cot(\theta) + \cot(\alpha)) \cdot \sin(\alpha)}{s_{\text{req}}} \quad (\text{AASHTO LRFD Eq. 5.8.3.3-4})$$

$$a_{v_req} = \frac{\frac{V_u}{\phi_v} - V_c - V_p}{f_y \cdot d_v \cdot (\cot(\theta) + \cot(\alpha)) \cdot \sin(\alpha)} \quad a_{v_req} = 0.14 \cdot \frac{\text{in}^2}{\text{ft}}$$

Torsional Steel Required

$$\phi_T = 0.9 \quad (\text{AASHTO LRFD 5.5.4.2.1})$$

$$T_u \leq \phi_T \cdot T_n \quad (\text{AASHTO LRFD Eq. 1.3.2.1-1})$$

$$T_n = \frac{2 \cdot A_o \cdot A_t \cdot f_y \cdot \cot(\theta)}{s_{\text{bar}_S}} \quad (\text{AASHTO LRFD Eq. 5.8.3.6.2-1})$$

$$a_{t_req} = \frac{T_u}{\phi_T \cdot 2 \cdot A_o \cdot f_y \cdot \cot(\theta)} \quad a_{t_req} = 0.19 \cdot \frac{\text{in}^2}{\text{ft}}$$

Total Required Transverse Steel (AASHTO LRFD 5.8.3.6.1)

$$a_{\text{req}} = a_{v_req} + 2 \text{ sides} \cdot a_{t_req} \quad a_{\text{req}} = 0.53 \cdot \frac{\text{in}^2}{\text{ft}}$$

$$a_{\text{prov}} = \frac{A_v}{s_{\text{bar}_S}} \quad a_{\text{prov}} = 2.48 \cdot \frac{\text{in}^2}{\text{ft}}$$

The transverse reinforcement is designed for the side of the section where the effects of shear and torsion are additive. (AASHTO LRFD C5.8.3.6.1) Both sides of the section need this reinforcing because the torsion can act on either side of the section.

$$a_{\text{prov}} > a_{\text{req}}$$

TransverseSteelCheck = "OK"

Hanger Reinforcement (Con't) (Bars S)

Maximum Spacing of Transverse Reinforcement (AASHTO LRFD 5.8.2.7)

Shear Stress

$$v_u = \frac{|V_u - \phi_V \cdot V_p|}{\phi_V \cdot b_V \cdot d_V} \qquad v_u = 0.158 \cdot \text{ksi} \qquad (\text{AASHTO LRFD Eq. 5.8.2.9-1})$$

$$0.125 \cdot f_c = 0.450 \cdot \text{ksi}$$

$$\text{if } v_u < 0.125 \cdot f_c, \quad s_{\max} = \text{minimum of:} \qquad (\text{AASHTO LRFD Eq. 5.8.2.7-1})$$
$$0.8 \cdot d_V = 64.46 \cdot \text{in}$$

& 24in

$$\text{if } v_u \geq 0.125 \cdot f_c, \quad s_{\max} = \text{minimum of:} \qquad (\text{AASHTO LRFD Eq. 5.8.2.7-2})$$
$$0.4 \cdot d_V = 32.23 \cdot \text{in}$$

& 12in

$$\text{Since } v_u < 0.125 \cdot f_c, \quad s_{\max} = 24.00 \cdot \text{in}$$

TxDOT limits the maximum transverse reinforcement spacing to 12", therefore:

(BDM-LRFD, Ch. 4, Sect. 4, Detailing)

$$s_{\max} = 12.00 \cdot \text{in}$$

$$s_{\text{bar}_S} = 8.50 \cdot \text{in} < s_{\max}$$

SpacingCheck = "OK!"

Hanger Reinforcement Summary:

Use double #6 stirrups @ 8.5" maximum spacing

Vertical End Reinforcement (Bars C)

(BDM-LRFD, Ch. 4, Sect. 5, Detailing)

Extra vertical reinforcing across end surfaces of the stem is provided to resist cracking which has been observed in existing bridges. (BDM-LRFD, Ch. 4, Sect. 5, Detailing) We will place #5 bars at approximately 6 in spacing. (TxSP) See the Bent Cap Details in the Appendices for detail of Bar C.

Use 6~#5 bars evenly spaced across each end of the stem

Skin Reinforcement (Bars T)

Try 7~#6 bars in stem and 3~#6 bars in Ledge on each side

$$A_{\text{bar}_T} = 0.44 \cdot \text{in}^2$$

$$\text{NoTBarsStem} = 7$$

$$\text{NoTBarsLedge} = 3$$

"a" must be within $\frac{2}{3}$ of d_e

(AASHTO LRFD 5.13.2.4.1)

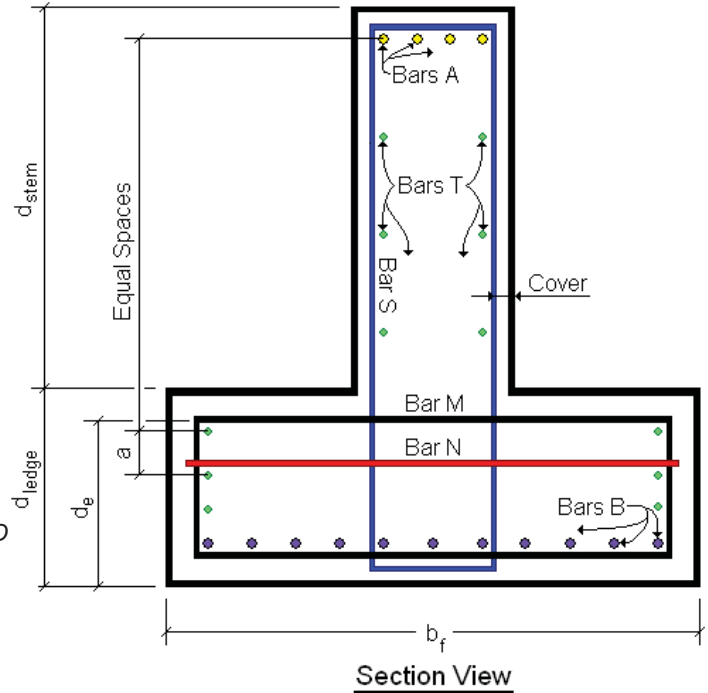
$$\frac{2}{3} \cdot d_e = 17.00 \cdot \text{in}$$

TxDOT typically uses: $a = 6 \text{ in}$ (TxSP)

Required Area of Skin Reinforcement

$$A_{\text{sk_Req}} = 0.012 \cdot (d - 30) \quad \text{(AASHTO LRFD Eq. 5.7.3.4-2)}$$

$$A_{\text{sk_Req}} = 0.62 \cdot \frac{\text{in}^2}{\text{ft}}$$



A_{sk} need not be greater than one quarter of the main reinforcing ($A_s/4$) per side face within $d/2$ of the main reinforcing. (AASHTO LRFD Eq. 5.7.3.4)

$A_{\text{sk_max}}$ = maximum of:

$$\frac{A_{\text{bar}_A} \cdot \text{BarANo}}{4} \div \frac{d_{s_neg}}{2} = 0.57 \cdot \frac{\text{in}^2}{\text{ft}}$$

$$\frac{A_{\text{bar}_B} \cdot \text{BarBNo}}{4} \div \frac{d_{s_pos}}{2} = 1.26 \cdot \frac{1}{\text{ft}} \cdot \text{in}^2$$

$$A_{\text{sk_max}} = 1.26 \cdot \frac{\text{in}^2}{\text{ft}}$$

A_{skReq} = minimum of:

$$A_{\text{sk_Req}} = 0.62 \cdot \frac{\text{in}^2}{\text{ft}}$$

$$A_{\text{sk_max}} = 1.26 \cdot \frac{1}{\text{ft}} \cdot \text{in}^2$$

$$A_{\text{skReq}} = 0.62 \cdot \frac{\text{in}^2}{\text{ft}}$$

Skin Reinforcement (Con't) (Bars T)

Required Spacing of Skin Reinforcement

(AASHTO LRFD 5.7.3.4)

s_{req} = minimum of:

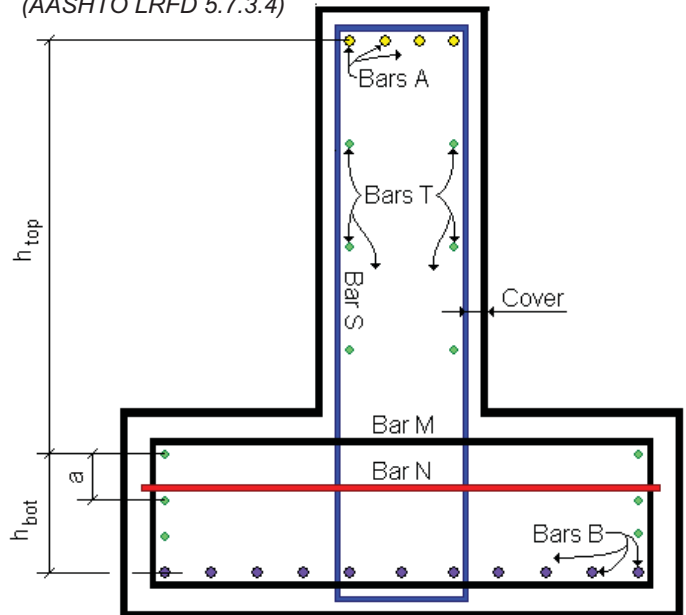
$$\frac{A_{bar_T}}{A_{skReq}} = 8.56 \cdot \text{in}$$

$$\frac{d_{s_neg}}{6} = 13.57 \cdot \text{in}$$

$$\frac{d_{s_pos}}{6} = 13.57 \cdot \text{in}$$

& 12in

$$s_{req} = 8.56 \cdot \text{in}$$



Actual Spacing of Skin Reinforcement

Check T bars Spacing in Stem:

Section View

$$h_{top} = d_{stem} - \left(\text{cover} + \frac{d_{bar_S}}{2} + \frac{d_{bar_A}}{2} \right) + \left(\text{cover} + \frac{d_{bar_M}}{2} + \frac{d_{bar_T}}{2} \right)$$

"cover" is measured to center of shear reinforcement.

$$h_{top} = 56.67 \cdot \text{in}$$

$$s_{skStem} = \frac{h_{top}}{\text{NoTBarsStem} + 1}$$

$$s_{skStem} = 7.08 \cdot \text{in}$$

$$s_{req} = 8.56 \cdot \text{in} > s_{skStem}$$

SkinSpacing = "OK!"

Check T bars Spacing in Ledge:

$$h_{bot} = d_{ledge} - \left(\text{cover} + \frac{d_{bar_M}}{2} + \frac{d_{bar_T}}{2} \right) - \left(\text{cover} + \frac{d_{bar_S}}{2} + \frac{d_{bar_B}}{2} \right)$$

"cover" is measured to center of shear reinforcement.

$$h_{bot} = 21.17 \cdot \text{in}$$

$$s_{skLedge} = \frac{h_{bot} - a}{\text{NoTBarsLedge} - 1}$$

$$s_{skLedge} = 7.58 \cdot \text{in}$$

$$s_{req} = 8.56 \cdot \text{in} > s_{skLedge}$$

SkinSpacing = "OK!"

Check if "a" dimension is less than or equal to s_{req} :

$$a = 6.00 \cdot \text{in} < s_{req} = 8.56 \cdot \text{in}$$

SkinSpacing = "OK!"

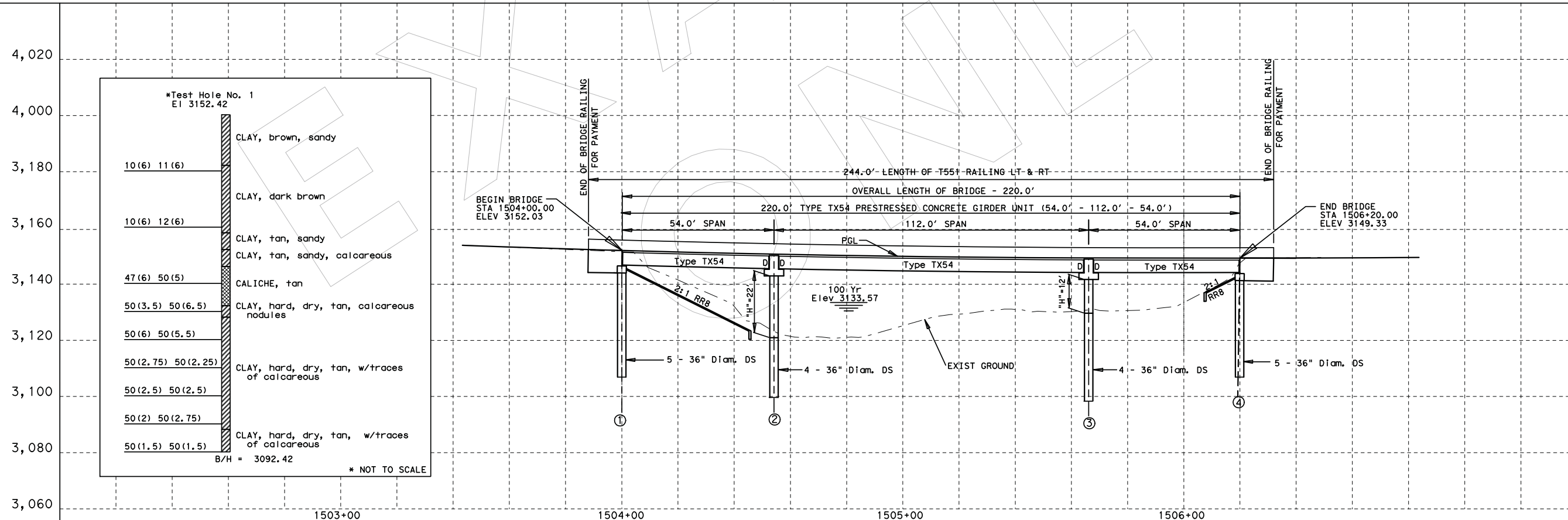
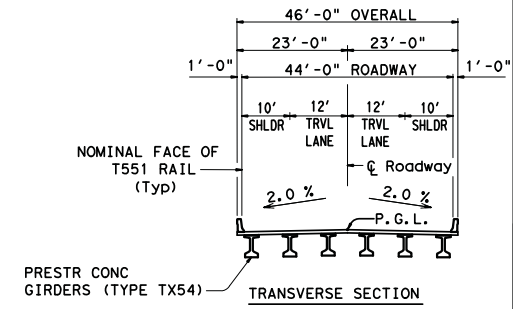
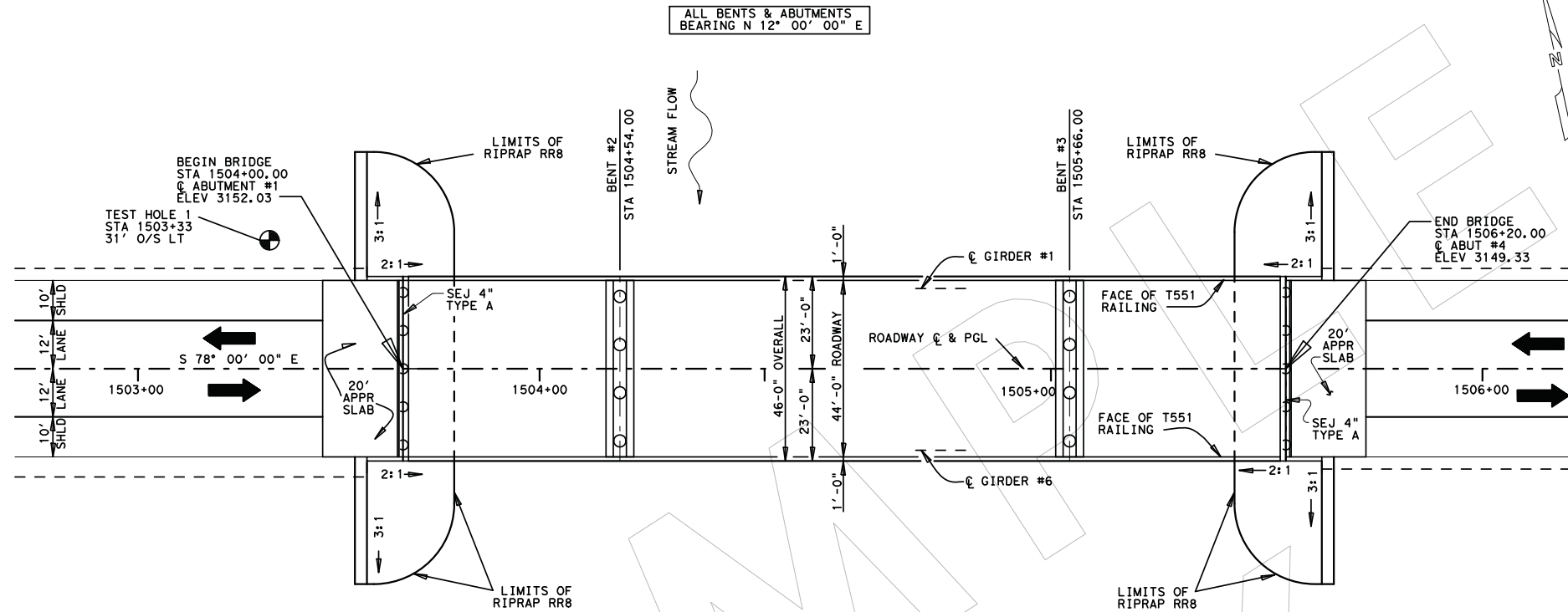
Skin Reinforcement Summary:

Use 7~#6 bars in stem and 3~#6 bars in Ledge on each side

See the Bent Cap Detail Sheet in the Appendices for the resulting design of all the preceding calculations.

Appendices

Bridge Layout	Pg. 45
CAP 18 Input File	Pg. 46
CAP 18 Output File	Pg. 47
Live Load Distribution Factor Spreadsheet	Pg. 70
Concrete Section Shear Capacity Spreadsheet ...	Pg. 86
Bent Cap Details	Pg. 87



FILE NAME: XXXX1Y01.DGN
 DATE:
 COMMENTS:

© 2010 Texas Department of Transportation	
FED. RD. DIV. NO.	FEDERAL AID PROJECT NO.
X	XX XXXX (XXX) XXX
STATE	COUNTY
TEXAS	ANY
CONT.	SECT. JOB HIGHWAY NO.
XXXX	XX XXX ANY

00001	County	Highway	Pro#	XXXX-XX-XXX	BRG						Comment
CAP18 Version 6.10 Inverted Tee Cap Design Example, Skew = 0.00											
1 E (Spans 54'-112'-54', Type TX54 Girder @ 8.0', 8" Slab, 2" O'lay)											
Table 1						16					0.0
Table 2	92	5.000E-01		20	2	70	1	3	1.25		1.75
	1.50	3	1.2	1.0		0.85		0.65	0.65		
Table 3	3	6	4	11	8						
(Lane Left)	2	32	60								
(Lane Right)	32	60	90								
(Stringers)	6	22	38	54	70	86					
(Supports)	10	34	58	82							
(Mom CP)	6	10	22	34	38	46	54	58	70	82	
(Mom CP)	86										
(Shear CP)	8	12	32	36	56	60	80	84			
Table 4 (Cap)	2	90		6.990E+07							
(DL Span1, Bm1)	6	6									-5.04
(DL Span1, Bm2)	22	22									-5.04
(DL Span1, Bm3)	38	38									-5.04
(DL Span1, Bm4)	54	54									-5.04
(DL Span1, Bm5)	70	70									-5.04
(DL Span1, Bm6)	86	86									-5.04
(DL Span2, Bm1)	6	6									-10.5
(DL Span2, Bm2)	22	22									-10.5
(DL Span2, Bm3)	38	38									-10.5
(DL Span2, Bm4)	54	54									-10.5
(DL Span2, Bm5)	70	70									-10.5
(DL Span2, Bm6)	86	86									-10.5
(Dist. Lane Ld)	0	20									-4.92
(Conc. Lane Ld)	4	4									-21.3
(Conc. Lane Ld)	16	16									-21.3

PSF HIGHWAY PD- CONTROL- CODED
NO COUNTY NO IPE SECTION-JOB BY DATE
00001 County Highway Pro# XXXX-XX-XXX BRG APR 22, 2010 Comment

CAP18 Version 6.10 Inverted Tee Cap Design Example, Skew = 0.00
PROB 1 (Spans 54'-112'-54', Type TX54 Girder @ 8.0', 8" Slab, 2" O'lay)

ENGLISH SYSTEM UNITS

TABLE 1. CONTROL DATA

	ENVELOPES OF MAXIMUMS	TABLE 2	NUMBER 3	4
KEEP FROM PRECEDING PROBLEM (1=YES) CARDS INPUT THIS PROBLEM	0	0	0	0 16
OPTION TO CLEAR ENVELOPES BEFORE LANE LOADINGS (1=YES)				0
OPTION TO OMIT PRINT (-1=TABLE 4A, -2=TABLE 5, -3=BOTH)				0
SKEW ANGLE, DEGREES				0.000

TABLE 2. CONSTANTS

NUMBER OF INCREMENTS FOR SLAB AND CAP				92
INCREMENT LENGTH, FT				0.500
NUMBER OF INCREMENTS FOR MOVABLE LOAD				20
START POSITION OF MOVABLE-LOAD STA ZERO				2
STOP POSITION OF MOVABLE-LOAD STA ZERO				70
NUMBER OF INCREMENTS BETWEEN EACH POSITION OF MOVABLE LOAD				1
ANALYSIS OPTION (1=WORKING STRESS, 2=LOAD FACTOR, 3=BOTH)				3
LOAD FACTOR FOR DEAD LOAD				1.25
LOAD FACTOR FOR OVERLAY LOAD				1.50
LOAD FACTOR FOR LIVE LOAD				1.75
MAXIMUM NUMBER OF LANES TO BE LOADED SIMULTANEOUSLY				3
LIST OF LOAD COEFFICIENTS CORRESPONDING TO NUMBER OF LANES LOADED				
1	2	3	4	5
1.200	1.000	0.850		

PROB 1 (Spans 54'-112'-54', Type TX54 Girder @ 8.0', 8" Slab, 2" O'lay)
(CONTINUED)

TABLE 3. LISTS OF STATIONS

	NUM OF LANES	NUM OF STRINGERS		NUM OF SUPPORTS			NUM MOM CONTR PTS		NUM SHEAR CONTR PTS	
TOTAL	3	6		4			11		8	
LANE LEFT	2	32	60							
LANE RIGHT	32	60	90							
STRINGERS	6.0	22.0	38.0	54.0	70.0	86.0				
SUPPORTS	10	34	58	82						
MOM CONTR	6	10	22	34	38	46	54	58	70	82
	86									
SHEAR CONTR	8	12	32	36	56	60	80	84		

TABLE 4. STIFFNESS AND LOAD DATA

FIXED-OR-MOVABLE			FIXED-POSITION DATA				MOVABLE-
STA FROM	STA TO	CONTD IF=1	CAP BENDING STIFFNESS (K-FT*FT)	SIDEWALK, SLAB LOADS (K)	STRINGER, CAP LOADS (K)	OVERLAY LOADS (K)	POSITION SLAB LOADS (K)
2	90	0	69900000.000	0.000	-2.485	0.000	0.000
6	6	0	0.000	0.000	-50.170	-5.040	0.000
22	22	0	0.000	0.000	-50.170	-5.040	0.000
38	38	0	0.000	0.000	-50.170	-5.040	0.000
54	54	0	0.000	0.000	-50.170	-5.040	0.000
70	70	0	0.000	0.000	-50.170	-5.040	0.000
86	86	0	0.000	0.000	-50.170	-5.040	0.000
6	6	0	0.000	0.000	-104.100	-10.500	0.000
22	22	0	0.000	0.000	-104.100	-10.500	0.000
38	38	0	0.000	0.000	-104.100	-10.500	0.000
54	54	0	0.000	0.000	-104.100	-10.500	0.000
70	70	0	0.000	0.000	-104.100	-10.500	0.000
86	86	0	0.000	0.000	-104.100	-10.500	0.000
0	20	0	0.000	0.000	0.000	0.000	-4.920
4	4	0	0.000	0.000	0.000	0.000	-21.300
16	16	0	0.000	0.000	0.000	0.000	-21.300

PROB 1 (Spans 54'-112'-54', Type TX54 Girder @ 8.0', 8" Slab, 2" O'lay)
(CONTINUED)

TABLE 4A. DEAD LOAD RESULTS (WORKING STRESS)

STA	DIST X (FT)	DEFLECTION (FT)	MOMENT (K-FT)	SHEAR (K)
-1	-0.50	0.000000	0.0	0.0
0	0.00	0.000000	0.0	0.0
1	0.50	-0.000039	0.0	0.0
2	1.00	-0.000034	0.0	-0.6
3	1.50	-0.000029	-0.6	-2.5
4	2.00	-0.000025	-2.5	-5.0
5	2.50	-0.000020	-5.6	-7.5
6	3.00	-0.000015	-9.9	-94.8
7	3.50	-0.000011	-100.4	-182.2
8	4.00	-0.000006	-192.2	-184.7
9	4.50	-0.000003	-285.2	-187.2
10	5.00	0.000000	-379.4	-34.9
11	5.50	0.000001	-320.1	117.3
12	6.00	0.000001	-262.0	114.9
13	6.50	0.000001	-205.2	112.4
14	7.00	-0.000001	-149.7	109.9
15	7.50	-0.000003	-95.4	107.4
16	8.00	-0.000006	-42.3	104.9
17	8.50	-0.000008	9.6	102.4
18	9.00	-0.000011	60.1	99.9
19	9.50	-0.000013	109.5	97.5
20	10.00	-0.000015	157.6	95.0
21	10.50	-0.000016	204.5	92.5
22	11.00	-0.000017	250.1	5.1
23	11.50	-0.000017	209.6	-82.3
24	12.00	-0.000016	167.8	-84.8
25	12.50	-0.000014	124.8	-87.3
26	13.00	-0.000012	80.5	-89.7
27	13.50	-0.000010	35.0	-92.2
28	14.00	-0.000008	-11.7	-94.7
29	14.50	-0.000005	-59.7	-97.2
30	15.00	-0.000003	-108.9	-99.7
31	15.50	-0.000001	-159.4	-102.2
32	16.00	0.000000	-211.1	-104.7
33	16.50	0.000000	-264.0	-107.1
34	17.00	0.000000	-318.2	45.0
35	17.50	-0.000002	-219.0	197.1
36	18.00	-0.000004	-121.1	194.7
37	18.50	-0.000007	-24.4	192.2
38	19.00	-0.000010	71.1	104.8
39	19.50	-0.000012	80.4	17.4
40	20.00	-0.000015	88.5	14.9
41	20.50	-0.000017	95.3	12.4
42	21.00	-0.000019	100.9	9.9
43	21.50	-0.000020	105.3	7.5

PROB 1 (Spans 54'-112'-54', Type TX54 Girder @ 8.0', 8" Slab, 2" O'lay)
(CONTINUED)

TABLE 4A. DEAD LOAD RESULTS (WORKING STRESS)

STA	DIST X (FT)	DEFLECTION (FT)	MOMENT (K-FT)	SHEAR (K)
44	22.00	-0.000021	108.4	5.0
45	22.50	-0.000021	110.2	2.5
46	23.00	-0.000022	110.9	0.0
47	23.50	-0.000021	110.2	-2.5
48	24.00	-0.000021	108.4	-5.0
49	24.50	-0.000020	105.3	-7.5
50	25.00	-0.000019	100.9	-9.9
51	25.50	-0.000017	95.3	-12.4
52	26.00	-0.000015	88.5	-14.9
53	26.50	-0.000012	80.4	-17.4
54	27.00	-0.000010	71.1	-104.8
55	27.50	-0.000007	-24.4	-192.2
56	28.00	-0.000004	-121.1	-194.7
57	28.50	-0.000002	-219.0	-197.1
58	29.00	0.000000	-318.2	-45.0
59	29.50	0.000000	-264.0	107.1
60	30.00	0.000000	-211.1	104.7
61	30.50	-0.000001	-159.4	102.2
62	31.00	-0.000003	-108.9	99.7
63	31.50	-0.000005	-59.7	97.2
64	32.00	-0.000008	-11.7	94.7
65	32.50	-0.000010	35.0	92.2
66	33.00	-0.000012	80.5	89.7
67	33.50	-0.000014	124.8	87.3
68	34.00	-0.000016	167.8	84.8
69	34.50	-0.000017	209.6	82.3
70	35.00	-0.000017	250.1	-5.1
71	35.50	-0.000016	204.5	-92.5
72	36.00	-0.000015	157.6	-95.0
73	36.50	-0.000013	109.5	-97.5
74	37.00	-0.000011	60.1	-99.9
75	37.50	-0.000008	9.6	-102.4
76	38.00	-0.000006	-42.3	-104.9
77	38.50	-0.000003	-95.4	-107.4
78	39.00	-0.000001	-149.7	-109.9
79	39.50	0.000001	-205.2	-112.4
80	40.00	0.000001	-262.0	-114.9
81	40.50	0.000001	-320.1	-117.3
82	41.00	0.000000	-379.4	34.9
83	41.50	-0.000003	-285.2	187.2
84	42.00	-0.000006	-192.2	184.7
85	42.50	-0.000011	-100.4	182.2
86	43.00	-0.000015	-9.9	94.8
87	43.50	-0.000020	-5.6	7.5
88	44.00	-0.000025	-2.5	5.0

PROB 1 (Spans 54'-112'-54', Type TX54 Girder @ 8.0', 8" Slab, 2" O'lay)
(CONTINUED)

TABLE 4A. DEAD LOAD RESULTS (WORKING STRESS)

STA	DIST X (FT)	DEFLECTION (FT)	MOMENT (K-FT)	SHEAR (K)
89	44.50	-0.000029	-0.6	2.5
90	45.00	-0.000034	0.0	0.6
91	45.50	-0.000039	0.0	0.0
92	46.00	0.000000	0.0	0.0
93	46.50	0.000000	0.0	0.0

PROB 1 (Spans 54'-112'-54', Type TX54 Girder @ 8.0', 8" Slab, 2" O'lay)
(CONTINUED)

TABLE 5. MULTI-LANE LOADING SUMMARY (WORKING STRESS)
(*--CRITICAL NUMBER OF LANE LOADS)

MOMENT (FT-K)

AT STA	DEAD LD EFFECT	LANE ORDER	POSITIVE MAXIMUM	LOAD AT LANE STA	LANE ORDER	NEGATIVE MAXIMUM	LOAD AT LANE STA
6	-9.9	0	0.0		0	0.0	
		1	0.0		1	0.0	
		2	0.0		2	0.0	
		3	0.0		3	0.0	
		0*			0*		
10	-379.4	0	0.0		0	-176.2	1 2
		1	0.0		1	-176.2	1 2
		2	0.0		2	0.0	
		3	0.0		3	0.0	
		0*			0*		
22	250.1	0	202.0	0 13	0	-33.4	2 36
		1	201.2	1 12	1	-33.4	2 36
		2	9.3	3 62	2	0.0	
		3	0.0		3	0.0	
		0*			0*		
34	-318.2	0	18.7	3 62	0	-136.3	0 18
		1	18.7	3 62	1	-116.6	1 12
		2	0.0		2	-84.7	2 32
		3	0.0		3	0.0	
		0*			2*		
38	71.1	0	83.6	2 32	0	-58.8	1 9
		1	83.6	2 32	1	-58.8	1 9
		2	3.2	3 62	2	0.0	
		3	0.0		3	0.0	
		0*			0*		
46	110.9	0	69.4	2 36	0	-27.8	1 9
		1	69.4	2 36	1	-27.8	1 9
		2	0.0		2	-27.8	3 63
		3	0.0		3	0.0	
		0*			2*		

PROB 1 (Spans 54'-112'-54', Type TX54 Girder @ 8.0', 8" Slab, 2" O'lay)
(CONTINUED)

MOMENT (FT-K)

AT STA	DEAD LD EFFECT	LANE ORDER	POSITIVE MAXIMUM	LOAD AT LANE STA	AT STA	LANE ORDER	NEGATIVE MAXIMUM	LOAD AT LANE STA
54	71.1	0	83.6	2	40	0	-58.8	3 63
		1	83.6	2	40	1	-58.8	3 63
		2	3.2	1	10	2	0.0	
		3	0.0			3	0.0	
		0*				0*		
58	-318.2	0	18.7	1	9	0	-136.3	0 54
		1	18.7	1	9	1	-116.6	3 60
		2	0.0			2	-84.7	2 40
		3	0.0			3	0.0	
		0*				2*		
70	250.1	0	202.0	0	59	0	-33.4	2 36
		1	201.2	3	60	1	-33.4	2 36
		2	9.3	1	9	2	0.0	
		3	0.0			3	0.0	
		0*				0*		
82	-379.4	0	0.0			0	-176.3	3 70
		1	0.0			1	-176.3	3 70
		2	0.0			2	0.0	
		3	0.0			3	0.0	
		0*				0*		
86	-9.9	0	0.0			0	0.0	
		1	0.0			1	0.0	
		2	0.0			2	0.0	
		3	0.0			3	0.0	
		0*				0*		

PROB 1 (Spans 54'-112'-54', Type TX54 Girder @ 8.0', 8" Slab, 2" O'lay)
(CONTINUED)

SHEAR (K)

AT STA	DEAD LD EFFECT	LANE ORDER	POSITIVE MAXIMUM	LOAD AT LANE STA	LANE ORDER	NEGATIVE MAXIMUM	LOAD AT LANE STA
8	-184.7	0	0.0		0	-88.1	1 2
		1	0.0		1	-88.1	1 2
		2	0.0		2	0.0	
		3	0.0		3	0.0	
		0*			0*		
12	114.9	0	44.8	1 6	0	-5.6	2 36
		1	44.8	1 6	1	-5.6	2 36
		2	1.6	3 62	2	0.0	
		3	0.0		3	0.0	
		0*			0*		
32	-104.7	0	1.6	3 62	0	-54.6	0 15
		1	1.6	3 62	1	-53.0	1 12
		2	0.0		2	-11.2	2 32
		3	0.0		3	0.0	
		0*			0*		
36	194.7	0	87.6	0 28	0	-7.8	3 63
		1	84.1	2 32	1	-7.8	3 63
		2	30.7	1 12	2	0.0	
		3	0.0		3	0.0	
		2*			0*		
56	-194.7	0	7.8	1 9	0	-87.6	0 44
		1	7.8	1 9	1	-84.1	2 40
		2	0.0		2	-30.7	3 60
		3	0.0		3	0.0	
		0*			2*		
60	104.7	0	54.6	0 57	0	-1.6	1 9
		1	53.0	3 60	1	-1.6	1 9
		2	11.2	2 40	2	0.0	
		3	0.0		3	0.0	
		0*			0*		

PROB 1 (Spans 54'-112'-54', Type TX54 Girder @ 8.0', 8" Slab, 2" O'lay)
(CONTINUED)

SHEAR (K)

AT STA	DEAD LD EFFECT	LANE ORDER	POSITIVE MAXIMUM	LOAD AT LANE STA	LANE ORDER	NEGATIVE MAXIMUM	LOAD AT LANE STA
80	-114.9	0	5.6	2 36	0	-44.8	3 66
		1	5.6	2 36	1	-44.8	3 66
		2	0.0		2	-1.6	1 9
		3	0.0		3	0.0	
		0*			0*		
84	184.7	0	88.1	3 70	0	0.0	
		1	88.1	3 70	1	0.0	
		2	0.0		2	0.0	
		3	0.0		3	0.0	
		0*			0*		

PROB 1 (Spans 54'-112'-54', Type TX54 Girder @ 8.0', 8" Slab, 2" O'lay)
(CONTINUED)

REACTION (K)

AT STA	DEAD LD EFFECT	LANE ORDER	POSITIVE MAXIMUM	LOAD LANE	AT STA	LANE ORDER	NEGATIVE MAXIMUM	LOAD LANE	AT STA
10	309.5	0	127.9	1	2	0	-5.6	2	36
		1	127.9	1	2	1	-5.6	2	36
		2	1.6	3	62	2	0.0		
		3	0.0			3	0.0		
		0*				0*			
34	309.3	0	117.1	0	22	0	-9.3	3	63
		1	95.3	2	32	1	-9.3	3	63
		2	83.6	1	12	2	0.0		
		3	0.0			3	0.0		
		2*				0*			
58	309.3	0	117.1	0	50	0	-9.3	1	9
		1	95.3	2	40	1	-9.3	1	9
		2	83.6	3	60	2	0.0		
		3	0.0			3	0.0		
		2*				0*			
82	309.5	0	127.9	3	70	0	-5.6	2	36
		1	127.9	3	70	1	-5.6	2	36
		2	1.6	1	9	2	0.0		
		3	0.0			3	0.0		
		0*				0*			

PROB 1 (Spans 54'-112'-54', Type TX54 Girder @ 8.0', 8" Slab, 2" O'lay)
(CONTINUED)

TABLE 6. ENVELOPES OF MAXIMUM VALUES (WORKING STRESS)

STA	DIST X (FT)	MAX + MOM (FT-K)	MAX - MOM (FT-K)	MAX + SHEAR (K)	MAX - SHEAR (K)
-1	-0.50	0.0	0.0	0.0	0.0
0	0.00	0.0	0.0	0.0	0.0
1	0.50	0.0	0.0	0.0	0.0
2	1.00	0.0	0.0	-0.6	-0.6
3	1.50	-0.6	-0.6	-2.5	-2.5
4	2.00	-2.5	-2.5	-5.0	-5.0
5	2.50	-5.6	-5.6	-7.5	-7.5
6	3.00	-9.9	-9.9	-94.8	-147.7
7	3.50	-100.4	-153.3	-182.2	-288.0
8	4.00	-192.2	-297.9	-184.7	-290.5
9	4.50	-285.2	-443.8	-187.2	-293.0
10	5.00	-379.4	-590.9	-18.0	-64.0
11	5.50	-307.0	-507.7	171.1	110.7
12	6.00	-231.2	-425.8	168.6	108.2
13	6.50	-156.0	-345.2	166.2	105.7
14	7.00	-82.0	-265.8	163.7	103.2
15	7.50	-9.0	-187.6	161.2	100.7
16	8.00	64.1	-110.7	158.7	98.2
17	8.50	136.9	-35.0	156.2	95.8
18	9.00	209.5	33.5	153.7	93.3
19	9.50	281.3	79.5	151.2	90.8
20	10.00	352.6	124.2	148.8	88.3
21	10.50	422.8	167.8	146.3	85.8
22	11.00	492.5	210.1	21.1	-8.0
23	11.50	419.6	165.8	-80.4	-147.8
24	12.00	345.7	120.2	-82.9	-150.3
25	12.50	270.9	73.1	-85.4	-152.8
26	13.00	195.0	24.6	-87.9	-155.3
27	13.50	118.7	-25.5	-90.4	-157.8
28	14.00	47.5	-76.9	-92.9	-160.3
29	14.50	-23.4	-129.5	-95.3	-162.8
30	15.00	-90.2	-183.8	-97.8	-165.2
31	15.50	-139.8	-264.5	-100.3	-167.7
32	16.00	-190.5	-348.2	-102.8	-170.2
33	16.50	-242.5	-433.2	-105.3	-172.7
34	17.00	-295.8	-519.5	88.8	27.4
35	17.50	-201.3	-362.9	311.9	187.8
36	18.00	-107.9	-225.2	309.5	185.4
37	18.50	26.3	-109.4	307.0	182.9
38	19.00	171.4	0.5	163.2	95.5
39	19.50	177.7	14.5	26.7	8.1
40	20.00	183.2	27.2	24.2	5.6
41	20.50	187.6	38.7	21.7	3.1
42	21.00	191.1	45.3	19.2	0.6

PROB 1 (Spans 54'-112'-54', Type TX54 Girder @ 8.0', 8" Slab, 2" O'lay)
(CONTINUED)

TABLE 6. ENVELOPES OF MAXIMUM VALUES (WORKING STRESS)

STA	DIST X (FT)	MAX + MOM (FT-K)	MAX - MOM (FT-K)	MAX + SHEAR (K)	MAX - SHEAR (K)
43	21.50	193.3	49.6	16.8	-1.8
44	22.00	194.4	52.7	14.3	-4.3
45	22.50	194.2	54.6	11.8	-6.8
46	23.00	194.1	55.2	9.3	-9.3
47	23.50	194.2	54.6	6.8	-11.8
48	24.00	194.4	52.7	4.3	-14.3
49	24.50	193.3	49.6	1.8	-16.8
50	25.00	191.1	45.3	-0.6	-19.2
51	25.50	187.6	38.7	-3.1	-21.7
52	26.00	183.2	27.2	-5.6	-24.2
53	26.50	177.7	14.5	-8.1	-26.7
54	27.00	171.4	0.5	-95.5	-163.2
55	27.50	26.3	-109.4	-182.9	-307.0
56	28.00	-107.9	-225.2	-185.4	-309.5
57	28.50	-201.3	-362.9	-187.8	-311.9
58	29.00	-295.8	-519.5	-27.4	-88.8
59	29.50	-242.5	-433.2	172.7	105.3
60	30.00	-190.5	-348.2	170.2	102.8
61	30.50	-139.8	-264.5	167.7	100.3
62	31.00	-90.2	-183.8	165.2	97.8
63	31.50	-23.4	-129.5	162.8	95.3
64	32.00	47.5	-76.9	160.3	92.9
65	32.50	118.7	-25.5	157.8	90.4
66	33.00	195.0	24.6	155.3	87.9
67	33.50	270.9	73.1	152.8	85.4
68	34.00	345.7	120.2	150.3	82.9
69	34.50	419.6	165.8	147.8	80.4
70	35.00	492.5	210.1	8.0	-21.1
71	35.50	422.8	167.8	-85.8	-146.3
72	36.00	352.6	124.2	-88.3	-148.8
73	36.50	281.3	79.5	-90.8	-151.2
74	37.00	209.5	33.5	-93.3	-153.7
75	37.50	136.9	-35.0	-95.8	-156.2
76	38.00	64.1	-110.7	-98.2	-158.7
77	38.50	-9.0	-187.6	-100.7	-161.2
78	39.00	-82.0	-265.8	-103.2	-163.7
79	39.50	-156.0	-345.2	-105.7	-166.2
80	40.00	-231.2	-425.8	-108.2	-168.6
81	40.50	-307.0	-507.7	-110.7	-171.1
82	41.00	-379.4	-590.9	64.0	18.0
83	41.50	-285.2	-443.8	293.0	187.2
84	42.00	-192.2	-297.9	290.5	184.7
85	42.50	-100.4	-153.3	288.0	182.2
86	43.00	-9.9	-9.9	147.7	94.8

PROB 1 (Spans 54'-112'-54', Type TX54 Girder @ 8.0', 8" Slab, 2" O'lay)
(CONTINUED)

TABLE 6. ENVELOPES OF MAXIMUM VALUES (WORKING STRESS)

STA	DIST X (FT)	MAX + MOM (FT-K)	MAX - MOM (FT-K)	MAX + SHEAR (K)	MAX - SHEAR (K)
87	43.50	-5.6	-5.6	7.5	7.5
88	44.00	-2.5	-2.5	5.0	5.0
89	44.50	-0.6	-0.6	2.5	2.5
90	45.00	0.0	0.0	0.6	0.6
91	45.50	0.0	0.0	0.0	0.0
92	46.00	0.0	0.0	0.0	0.0
93	46.50	0.0	0.0	0.0	0.0

PROB 1 (Spans 54'-112'-54', Type TX54 Girder @ 8.0', 8" Slab, 2" O'lay)
(CONTINUED)

TABLE 7. MAXIMUM SUPPORT REACTIONS (WORKING STRESS)

STA	DIST X (FT)	MAX + REACT (K)	MAX - REACT (K)
10	5.00	463.0	302.8
34	17.00	488.2	298.1
58	29.00	488.2	298.1
82	41.00	463.0	302.8

PROB 1 (Spans 54'-112'-54', Type TX54 Girder @ 8.0', 8" Slab, 2" O'lay)
(CONTINUED)

TABLE 5. MULTI-LANE LOADING SUMMARY (LOAD FACTOR)
(*--CRITICAL NUMBER OF LANE LOADS)

MOMENT (FT-K)

AT STA	DEAD LD EFFECT	LANE ORDER	POSITIVE MAXIMUM	LOAD AT LANE STA	LANE ORDER	NEGATIVE MAXIMUM	LOAD AT LANE STA
6	-12.4	0	0.0		0	0.0	
		1	0.0		1	0.0	
		2	0.0		2	0.0	
		3	0.0		3	0.0	
		0*			0*		
10	-482.0	0	0.0		0	-308.4	1 2
		1	0.0		1	-308.4	1 2
		2	0.0		2	0.0	
		3	0.0		3	0.0	
		0*			0*		
22	317.5	0	353.5	0 13	0	-58.4	2 36
		1	352.1	1 12	1	-58.4	2 36
		2	16.3	3 62	2	0.0	
		3	0.0		3	0.0	
		0*			0*		
34	-403.6	0	32.7	3 62	0	-238.5	0 18
		1	32.7	3 62	1	-204.0	1 12
		2	0.0		2	-148.2	2 32
		3	0.0		3	0.0	
		0*			2*		
38	90.8	0	146.3	2 32	0	-102.9	1 9
		1	146.3	2 32	1	-102.9	1 9
		2	5.6	3 62	2	0.0	
		3	0.0		3	0.0	
		0*			0*		
46	140.5	0	121.4	2 36	0	-48.7	1 9
		1	121.4	2 36	1	-48.7	1 9
		2	0.0		2	-48.7	3 63
		3	0.0		3	0.0	
		0*			2*		

PROB 1 (Spans 54'-112'-54', Type TX54 Girder @ 8.0', 8" Slab, 2" O'lay)
(CONTINUED)

MOMENT (FT-K)

AT STA	DEAD LD EFFECT	LANE ORDER	POSITIVE MAXIMUM	LOAD AT LANE STA	AT STA	LANE ORDER	NEGATIVE MAXIMUM	LOAD AT LANE STA
54	90.8	0	146.3	2	40	0	-102.9	3 63
		1	146.3	2	40	1	-102.9	3 63
		2	5.6	1	10	2	0.0	
		3	0.0			3	0.0	
		0*				0*		
58	-403.6	0	32.7	1	9	0	-238.5	0 54
		1	32.7	1	9	1	-204.0	3 60
		2	0.0			2	-148.2	2 40
		3	0.0			3	0.0	
		0*				2*		
70	317.5	0	353.5	0	59	0	-58.4	2 36
		1	352.1	3	60	1	-58.4	2 36
		2	16.3	1	9	2	0.0	
		3	0.0			3	0.0	
		0*				0*		
82	-482.0	0	0.0			0	-308.4	3 70
		1	0.0			1	-308.4	3 70
		2	0.0			2	0.0	
		3	0.0			3	0.0	
		0*				0*		
86	-12.4	0	0.0			0	0.0	
		1	0.0			1	0.0	
		2	0.0			2	0.0	
		3	0.0			3	0.0	
		0*				0*		

PROB 1 (Spans 54'-112'-54', Type TX54 Girder @ 8.0', 8" Slab, 2" O'lay)
(CONTINUED)

SHEAR (K)

AT STA	DEAD LD EFFECT	LANE ORDER	POSITIVE MAXIMUM	LOAD AT LANE STA	LANE ORDER	NEGATIVE MAXIMUM	LOAD AT LANE STA
8	-234.8	0	0.0		0	-154.2	1 2
		1	0.0		1	-154.2	1 2
		2	0.0		2	0.0	
		3	0.0		3	0.0	
		0*			0*		
12	145.7	0	78.4	1 6	0	-9.7	2 36
		1	78.4	1 6	1	-9.7	2 36
		2	2.7	3 62	2	0.0	
		3	0.0		3	0.0	
		0*			0*		
32	-132.6	0	2.7	3 62	0	-95.6	0 15
		1	2.7	3 62	1	-92.7	1 12
		2	0.0		2	-19.5	2 32
		3	0.0		3	0.0	
		0*			0*		
36	247.2	0	153.2	0 28	0	-13.6	3 63
		1	147.2	2 32	1	-13.6	3 63
		2	53.7	1 12	2	0.0	
		3	0.0		3	0.0	
		2*			0*		
56	-247.2	0	13.6	1 9	0	-153.2	0 44
		1	13.6	1 9	1	-147.2	2 40
		2	0.0		2	-53.7	3 60
		3	0.0		3	0.0	
		0*			2*		
60	132.6	0	95.6	0 57	0	-2.7	1 9
		1	92.7	3 60	1	-2.7	1 9
		2	19.5	2 40	2	0.0	
		3	0.0		3	0.0	
		0*			0*		

PROB 1 (Spans 54'-112'-54', Type TX54 Girder @ 8.0', 8" Slab, 2" O'lay)
(CONTINUED)

SHEAR (K)

AT STA	DEAD LD EFFECT	LANE ORDER	POSITIVE MAXIMUM	LOAD AT LANE STA	LANE ORDER	NEGATIVE MAXIMUM	LOAD AT LANE STA
80	-145.7	0	9.7	2 36	0	-78.4	3 66
		1	9.7	2 36	1	-78.4	3 66
		2	0.0		2	-2.7	1 9
		3	0.0		3	0.0	
		0*			0*		
84	234.8	0	154.2	3 70	0	0.0	
		1	154.2	3 70	1	0.0	
		2	0.0		2	0.0	
		3	0.0		3	0.0	
		0*			0*		

PROB 1 (Spans 54'-112'-54', Type TX54 Girder @ 8.0', 8" Slab, 2" O'lay)
(CONTINUED)

REACTION (K)

AT STA	DEAD LD EFFECT	LANE ORDER	POSITIVE MAXIMUM	LOAD AT LANE STA	AT STA	LANE ORDER	NEGATIVE MAXIMUM	LOAD AT LANE STA
10	392.9	0	223.8	1	2	0	-9.7	2 36
		1	223.8	1	2	1	-9.7	2 36
		2	2.7	3	62	2	0.0	
		3	0.0			3	0.0	
		0*				0*		
34	392.2	0	205.0	0	22	0	-16.3	3 63
		1	166.8	2	32	1	-16.3	3 63
		2	146.3	1	12	2	0.0	
		3	0.0			3	0.0	
		2*				0*		
58	392.2	0	205.0	0	50	0	-16.3	1 9
		1	166.8	2	40	1	-16.3	1 9
		2	146.3	3	60	2	0.0	
		3	0.0			3	0.0	
		2*				0*		
82	392.9	0	223.8	3	70	0	-9.7	2 36
		1	223.8	3	70	1	-9.7	2 36
		2	2.7	1	9	2	0.0	
		3	0.0			3	0.0	
		0*				0*		

PROB 1 (Spans 54'-112'-54', Type TX54 Girder @ 8.0', 8" Slab, 2" O'lay)
(CONTINUED)

TABLE 6. ENVELOPES OF MAXIMUM VALUES (LOAD FACTOR)

STA	DIST X (FT)	MAX + MOM (FT-K)	MAX - MOM (FT-K)	MAX + SHEAR (K)	MAX - SHEAR (K)
-1	-0.50	0.0	0.0	0.0	0.0
0	0.00	0.0	0.0	0.0	0.0
1	0.50	0.0	0.0	0.0	0.0
2	1.00	0.0	0.0	-0.8	-0.8
3	1.50	-0.8	-0.8	-3.1	-3.1
4	2.00	-3.1	-3.1	-6.2	-6.2
5	2.50	-7.0	-7.0	-9.3	-9.3
6	3.00	-12.4	-12.4	-120.5	-213.0
7	3.50	-127.5	-220.0	-231.7	-416.7
8	4.00	-244.1	-429.2	-234.8	-419.8
9	4.50	-362.3	-639.9	-237.9	-423.0
10	5.00	-482.0	-852.1	-15.0	-95.4
11	5.50	-383.9	-735.2	242.9	137.1
12	6.00	-279.2	-619.9	239.8	134.0
13	6.50	-174.9	-506.1	236.7	130.9
14	7.00	-72.2	-393.8	233.6	127.8
15	7.50	29.4	-283.2	230.5	124.7
16	8.00	131.8	-174.0	227.4	121.6
17	8.50	234.4	-66.4	224.3	118.5
18	9.00	337.2	29.1	221.2	115.4
19	9.50	439.2	86.0	218.1	112.2
20	10.00	540.9	141.4	215.0	109.1
21	10.50	641.5	195.2	211.8	106.0
22	11.00	741.7	247.4	34.5	-16.5
23	11.50	633.5	189.4	-101.4	-219.4
24	12.00	524.1	129.6	-104.5	-222.5
25	12.50	413.8	67.7	-107.6	-225.6
26	13.00	302.3	4.0	-110.7	-228.7
27	13.50	190.6	-61.8	-113.8	-231.8
28	14.00	88.6	-129.2	-116.9	-234.9
29	14.50	-12.5	-198.1	-120.0	-238.0
30	15.00	-105.7	-269.4	-123.1	-241.1
31	15.50	-168.0	-386.3	-126.2	-244.2
32	16.00	-231.9	-507.9	-129.3	-247.3
33	16.50	-297.4	-631.1	-132.4	-250.4
34	17.00	-364.4	-755.8	133.9	26.5
35	17.50	-246.6	-529.4	451.2	234.0
→ 36	18.00	-130.3	-335.6	448.1	230.9
37	18.50	58.2	-179.2	445.0	227.8
38	19.00	266.4	-32.7	235.2	116.6
39	19.50	272.8	-12.9	38.0	5.5
40	20.00	278.2	5.3	34.9	2.4
41	20.50	282.6	22.0	31.8	-0.7
42	21.00	285.9	30.7	28.7	-3.9
43	21.50	287.7	36.1	25.6	-7.0

PROB 1 (Spans 54'-112'-54', Type TX54 Girder @ 8.0', 8" Slab, 2" O'lay)
(CONTINUED)

TABLE 6. ENVELOPES OF MAXIMUM VALUES (LOAD FACTOR)

STA	DIST X (FT)	MAX + MOM (FT-K)	MAX - MOM (FT-K)	MAX + SHEAR (K)	MAX - SHEAR (K)
44	22.00	287.9	40.0	22.5	-10.1
45	22.50	286.6	42.4	19.4	-13.2
46	23.00	286.2	43.1	16.3	-16.3
47	23.50	286.6	42.4	13.2	-19.4
48	24.00	287.9	40.0	10.1	-22.5
49	24.50	287.7	36.1	7.0	-25.6
50	25.00	285.9	30.7	3.9	-28.7
51	25.50	282.6	22.0	0.7	-31.8
52	26.00	278.2	5.3	-2.4	-34.9
53	26.50	272.8	-12.9	-5.5	-38.0
54	27.00	266.4	-32.7	-116.6	-235.2
55	27.50	58.2	-179.2	-227.8	-445.0
56	28.00	-130.3	-335.6	-230.9	-448.1
57	28.50	-246.6	-529.4	-234.0	-451.2
58	29.00	-364.4	-755.8	-26.5	-133.9
59	29.50	-297.4	-631.1	250.4	132.4
60	30.00	-231.9	-507.9	247.3	129.3
61	30.50	-168.0	-386.3	244.2	126.2
62	31.00	-105.7	-269.4	241.1	123.1
63	31.50	-12.5	-198.1	238.0	120.0
64	32.00	88.6	-129.2	234.9	116.9
65	32.50	190.6	-61.8	231.8	113.8
66	33.00	302.3	4.0	228.7	110.7
67	33.50	413.8	67.7	225.6	107.6
68	34.00	524.1	129.6	222.5	104.5
69	34.50	633.5	189.4	219.4	101.4
70	35.00	741.7	247.4	16.5	-34.5
71	35.50	641.5	195.2	-106.0	-211.8
72	36.00	540.9	141.4	-109.1	-215.0
73	36.50	439.2	86.0	-112.2	-218.1
74	37.00	337.2	29.1	-115.4	-221.2
75	37.50	234.4	-66.4	-118.5	-224.3
76	38.00	131.8	-174.0	-121.6	-227.4
77	38.50	29.4	-283.2	-124.7	-230.5
78	39.00	-72.2	-393.8	-127.8	-233.6
79	39.50	-174.9	-506.1	-130.9	-236.7
80	40.00	-279.2	-619.9	-134.0	-239.8
81	40.50	-383.9	-735.2	-137.1	-242.9
82	41.00	-482.0	-852.1	95.4	15.0
83	41.50	-362.3	-639.9	423.0	237.9
84	42.00	-244.1	-429.2	419.8	234.8
85	42.50	-127.5	-220.0	416.7	231.7
86	43.00	-12.4	-12.4	213.0	120.5
87	43.50	-7.0	-7.0	9.3	9.3

PROB 1 (Spans 54'-112'-54', Type TX54 Girder @ 8.0', 8" Slab, 2" O'lay)
(CONTINUED)

TABLE 6. ENVELOPES OF MAXIMUM VALUES (LOAD FACTOR)

STA	DIST X (FT)	MAX + MOM (FT-K)	MAX - MOM (FT-K)	MAX + SHEAR (K)	MAX - SHEAR (K)
88	44.00	-3.1	-3.1	6.2	6.2
89	44.50	-0.8	-0.8	3.1	3.1
90	45.00	0.0	0.0	0.8	0.8
91	45.50	0.0	0.0	0.0	0.0
92	46.00	0.0	0.0	0.0	0.0
93	46.50	0.0	0.0	0.0	0.0

PROB 1 (Spans 54'-112'-54', Type TX54 Girder @ 8.0', 8" Slab, 2" O'lay)
(CONTINUED)

TABLE 7. MAXIMUM SUPPORT REACTIONS (LOAD FACTOR)

STA	DIST X (FT)	MAX + REACT (K)	MAX - REACT (K)
10	5.00	661.4	381.2
34	17.00	705.3	372.7
58	29.00	705.3	372.7
82	41.00	661.4	381.2

TXDOT	County:	ANY	Highway:	Any	Design:	BRG	Date:	2/2/10	2007 LRFD Specs Rev. 8/08 - (No Interim)
BRIDGE	C-S-J:	XXX-XX-XXXX	ID #:	XXXX	Ck Dsn:	BRG	Date:		
DIVISION	Descrip:	Inverted Tee Design Example, Spans 1 & 3			File:	distribution_factors_i.xls		Sheet:	

LRFD Live Load Distribution Factors*

Live Load Distribution Factors are calculated according to AASHTO LRFD Bridge Design Specifications, 4th Edition (2007 with no interim revisions) as prescribed by TxDOT policies (LRFD Design Manual July 2008) and practices. The Lever Rule is used when outside the Range of Applicability. The Range of Applicability for the Skew Correction Factors is ignored.

INPUT:

Beam Type = Tx54
 No. Beams, N_b = 6
 CL_{brg} to CL_{brg} , L = 50.38 ft
 Beam Spacing, S = 8.00 ft
 Avg. Skew Angle, θ = 0.00 deg
 Slab Thickness, t_s = 8 in
 Slab Overhang, OH = 3 ft
 Rail Width, RW = 1 ft
 Roadway Width, W = 44 ft
 Number of Lanes, N_L = 3

Deck Slab		Beam	
Conc wt =	0.145 k/ft ³	weight =	0.145 k/ft ³
f'_c =	4.0 ksi	f'_c =	8.5 ksi
E_{slab} =	3644 ksi	E_{beam} =	5312 ksi
		y_t =	30.49 in
		A =	817.0 in ²
		I =	299740 in ⁴

Longitudinal Stiffness Parameter: (4.6.2.2.1-1)

e_g (in) = 34.49 (dist. b/w cog of bm & deck)
 n = 1.000
 $K_g = n(I + Ae_g^2) = 1271611 \text{ in}^4$

*For typical cross sections (a,e,i,j & k). Table 4.6.2.2.1-1

RESULTS:

	Final LLDF
Interior Shear LLDF, $gV_{interior}$	0.814
Interior Moment LLDF, $gM_{interior}$	0.794
Exterior Shear LLDF, $gV_{exterior}$	0.814
Exterior Moment LLDF, $gM_{exterior}$	0.794

The Final LLDF may be modified according to the following TxDOT policies:

- ◆ Exterior beams use the interior LLDF when $OH \leq S/2$.
- ◆ When $OH > S/2$ the exterior beam LLDF is determined by the lever rule for a single lane with a multiple presence factor of 1.0.
- ◆ In no case shall the LLDF for the exterior beams be less than the LLDFs for the interior beams.
- ◆ When the Roadway width is less than 20ft, all beams are designed for one lane loaded only.
- ◆ In no case shall the LLDF be less than $m \cdot N_L \cdot N_b$.

CALCULATIONS:

Shear LLDF Correction for Skew (Table 4.6.2.2.3c-1)

$$\text{Corr.} = 1.0 + 0.20 \left(\frac{12.0 L t_s^3}{K_g} \right)^{0.3} \tan \theta$$

$$= 1.0 + 0.20 * [(12.0 * 50.4 * 8^3) / (1,271,611)]^{0.3} * \tan(0)$$

Corr. = 1.000

Check θ : $0^\circ \leq 0^\circ \leq 60^\circ$ OK

Check S : $3.5' \leq 8.0' \leq 16.0'$ OK

Check L : $20' \leq 50.4' \leq 240'$ OK

Check N_b : $6 \geq 4$ OK

Moment LLDF Correction for Skew (Table 4.6.2.2.2e-1)

$$\text{Corr.} = 1 - c_1 (\tan \theta)^{1.5}$$

$$= 1 - 0 (\tan 0)^{1.5}$$

Corr. = 1.000

Check θ : $0^\circ < 30^\circ$

Set $\theta = 0^\circ$

where: $c_1 = 0.25 \left(\frac{K_g}{12.0 L t_s^3} \right)^{0.25} \left(\frac{S}{L} \right)^{0.5}$

$c_1 = 0.000$ because $\theta < 30^\circ$

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INTERIOR BEAM:

Shear LL Distribution Per Lane (Table 4.6.2.2.3a-1):

One Lane Loaded

Lever Rule (Table 3.6.1.1.2)

$$mg = 0.625 * 1.2 = 0.750$$

Modify for Skew:

$$\text{skew correction} = 1.000$$

$$mg = 0.750 * 1.000 = 0.750$$

Equation

$$g = 0.36 + \left(\frac{S}{25} \right)$$

$$g = 0.36 + (8 / 25) = 0.680$$

Modify for Skew:

$$\text{skew correction} = 1.000$$

$$g = 0.680 * 1.000 = 0.680$$

Range of Applicability (ROA) Checks

$$\text{Check S: } 3.5' \leq 8.0' \leq 16.0' \quad \text{OK}$$

$$\text{Check } t_s: 4.5" \leq 8.0" \leq 12.0" \quad \text{OK}$$

$$\text{Check L: } 20' \leq 50.4' \leq 240' \quad \text{OK}$$

$$\text{Check } N_b: 6 \geq 4 \quad \text{OK}$$

Use Equation from Table 4.6.2.2.3a-1 because all criteria is OK.

$$gV_{int1} = 0.680$$

Two or More Lanes Loaded

Lever Rule (Table 3.6.1.1.2)

$$mg = \text{Max}(0.875 * 1.0, 0.875 * 0.85, 0.875 * 0.65) = 0.875$$

Modify for Skew:

$$\text{skew correction} = 1.000$$

$$mg = 0.875 * 1.000 = 0.875$$

Equation

$$g = 0.2 + \left(\frac{S}{12} \right) - \left(\frac{S}{35} \right)^{2.0}$$

$$g = 0.2 + (8 / 12) - (8 / 35)^{2.0} = 0.814$$

Modify for Skew:

$$\text{skew correction} = 1.000$$

$$g = 0.814 * 1.000 = 0.814$$

Range of Applicability (ROA) Checks (same as for one lane loaded)

Use Equation from Table 4.6.2.2.3a-1 because all criteria is OK.

$$gV_{int2+} = 0.814$$

TxDOT Policy states $gV_{Interior}$ must be $\geq m \cdot N_L + N_b$

$$m \cdot N_L + N_b = 0.85 * 3 / 6 = 0.425$$

Is $W \geq 20\text{ft}$? **Yes**

TxDOT Policy states that if $W < 20\text{ft}$, $gV_{Interior}$ is the Maximum of: gV_{int1} and $m \cdot N_L + N_b$.

>> TxDOT Policy states that if $W \geq 20\text{ft}$, $gV_{Interior}$ is the Maximum of: gV_{int1} , gV_{int2+} , $m \cdot N_L + N_b$.

$gV_{interior} = 0.814$

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INTERIOR BEAM:

Moment LL Distribution Per Lane (Table 4.6.2.2.2b-1):

One Lane Loaded

Lever Rule (Table 3.6.1.1.2)

$$mg = 0.625 * 1.2 = 0.750$$

Modify for Skew:

$$\text{skew correction} = 1.000$$

$$mg = 0.750 * 1.000 = 0.750$$

Equation

$$g = 0.06 + \left(\frac{S}{14}\right)^{0.4} \left(\frac{S}{L}\right)^{0.3} \left(\frac{K_g}{12Lt_s^3}\right)^{0.1}$$

$$g = 0.06 + (8/14)^{0.4} * (8/50.4)^{0.3} * (1,271,611/(12*50.4*8^3))^{0.1} = 0.590$$

Modify for Skew:

$$\text{skew correction} = 1.000$$

$$g = 0.590 * 1.000 = 0.590$$

Range of Applicability (ROA) Checks

$$\text{Check S: } 3.5' \leq 8.0' \leq 16.0' \quad \text{OK}$$

$$\text{Check } t_s: 4.5" \leq 8.0" \leq 12.0" \quad \text{OK}$$

$$\text{Check L: } 20' \leq 50.4' \leq 240' \quad \text{OK}$$

$$\text{Check } N_b: 6 \geq 4 \quad \text{OK}$$

$$\text{Check } K_g: 10,000 \leq 1,271,611 \leq 7,000,000 \quad \text{OK}$$

Use Equation from Table 4.6.2.2.2b-1 because all criteria is OK.

$$gM_{int1} = 0.590$$

Two or More Lanes Loaded

Lever Rule (Table 3.6.1.1.2)

$$mg = \text{Max}(0.875 * 1.0, 0.875 * 0.85, 0.875 * 0.65) = 0.875$$

Modify for Skew:

$$\text{skew correction} = 1.000$$

$$mg = 0.875 * 1.000 = 0.875$$

Equation

$$g = 0.075 + \left(\frac{S}{9.5}\right)^{0.6} \left(\frac{S}{L}\right)^{0.2} \left(\frac{K_g}{12Lt_s^3}\right)^{0.1}$$

$$g = 0.075 + (8/9.5)^{0.6} * (8/50.4)^{0.2} * (1,271,611/(12*50.4*8^3))^{0.1} = 0.794$$

Modify for Skew:

$$\text{skew correction} = 1.000$$

$$g = 0.794 * 1.000 = 0.794$$

Range of Applicability (ROA) Checks (same as for one lane loaded)

Use Equation from Table 4.6.2.2.2b-1 because all criteria is OK.

$$gM_{int2+} = 0.794$$

TxDOT Policy states $gM_{Interior}$ must be $\geq m \cdot N_L \div N_b$

$$m \cdot N_L \div N_b = 0.85 * 3 / 6 = 0.425$$

Is $W \geq 20\text{ft}$? **Yes**

TxDOT Policy states that if $W < 20\text{ft}$, $gM_{Interior}$ is the Maximum of: gM_{int1} and $m \cdot N_L \div N_b$.

>> TxDOT Policy states that if $W \geq 20\text{ft}$, $gM_{Interior}$ is the Maximum of: gM_{int1} , gM_{int2+} , $m \cdot N_L \div N_b$.

$$gM_{interior} = 0.794$$

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EXTERIOR BEAM:

Shear LL Distribution Per Lane (Table 4.6.2.2.3b-1):

One Lane Loaded

Lever Rule (Table 3.6.1.1.2)

$$mg = 0.625 * 1.0 = 0.625$$

TxDOT uses a multiple presence factor of 1.0 for one lane loaded on the exterior beam.

Modify for Skew:

$$\text{skew correction} = 1.000$$

$$mg = 0.625 * 1.000 = 0.625$$

Use Lever Rule, as per AASHTO LRFD Table 4.6.2.2.3b-1.

$$gV_{\text{ext1}} = 0.625$$

Two or More Lanes Loaded

Lever Rule (Table 3.6.1.1.2)

$$mg = \text{Max}(0.625 * 1.0, 0.625 * 0.85, 0.625 * 0.65) = 0.625$$

Modify for Skew:

$$\text{skew correction} = 1.000$$

$$mg = 0.625 * 1.000 = 0.625$$

Equation

d_e = dist. b/w CL web to curb

d_e = OH - Rail Width

$$d_e = 3\text{ft} - 1\text{ft} = 2.0\text{ft}$$

$$e = 0.6 + \left(\frac{d_e}{10}\right)$$

$$e = 0.6 + (2.0/10) = 0.800$$

$g = e * gV_{\text{int2+Eq}}$

$$g = 0.800 * 0.814 = 0.651$$

Skew Correction is included in $gV_{\text{(interior)}}$.

Range of Applicability (ROA) Checks

Interior ROA is implicitly applied to the exterior beam.

Check Interior Beam ROA: OK

Check d_e : $-1.0' \leq 2.0' \leq 5.5'$ OK

Check N_b : $6 \neq 3$ OK

Use Equation from Table 4.6.2.2.3b-1 because all criteria is OK.

$$gV_{\text{ext2+}} = 0.651$$

TxDOT Policy states gV_{Exterior} must be $\geq gV_{\text{interior}}$

$$gV_{\text{interior}} = 0.814$$

TxDOT Policy states gV_{Exterior} must be $\geq m \cdot N_L + N_b$

$$m \cdot N_L + N_b = 0.85 * 3 / 6 = 0.425$$

Is $OH \leq S/2$? Yes

Is $W \geq 20\text{ft}$? Yes

>> TxDOT Policy states that if $OH \leq S/2$, gV_{Exterior} is gV_{interior} .

TxDOT Policy states that if $OH > S/2$ and $W < 20\text{ft}$, gV_{Exterior} is the Maximum of: gV_{ext1} , gV_{interior} , and $m \cdot N_L + N_b$.

TxDOT Policy states that if $OH > S/2$ and $W \geq 20\text{ft}$, gV_{Exterior} is the Maximum of: gV_{ext1} , $gV_{\text{ext2+}}$, gV_{interior} , and $m \cdot N_L + N_b$.

$gV_{\text{exterior}} = 0.814$

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EXTERIOR BEAM:

Moment LL Distribution Per Lane (Table 4.6.2.2d-1):

One Lane Loaded

Lever Rule

$mg = 0.625 * 1.0 = 0.625$ TxDOT uses a multiple presence factor of 1.0 for one lane loaded on the exterior beam.

Modify for Skew:

skew correction = 1.000

$mg = 0.625 * 1.000 = 0.625$

Use Lever Rule as per AASHTO LRFD Table 4.6.2.2d-1.

$gM_{ext1} = 0.625$

Two or More Lanes Loaded

Lever Rule (Table 3.6.1.1.2)

$mg = \text{Max}(0.625 * 1.0, 0.625 * 0.85, 0.625 * 0.65) = 0.625$

Modify for Skew:

skew correction = 1.000

$mg = 0.625 * 1.000 = 0.625$

Equation

$$e = 0.77 + \left(\frac{d_e}{9.1} \right)$$

$e = 0.77 + (2.0/9.1) = 0.990$

$g = e * gM_{int2+Eq}$

$g = 0.99 * 0.794 = 0.786$

Skew Correction included in $gM_{interior}$.

Range of Applicability (ROA) Checks

Interior ROA is implicitly applied to the exterior beam.

Check Interior Beam ROA: OK

Check d_e : $-1.0' \leq 2.0' \leq 5.5'$ OK

Check N_b : $6 \neq 3$ OK

Use Equation from Table 4.6.2.2d-1 because all criteria is OK.

$gM_{ext2+} = 0.786$

TxDOT Policy states $gM_{Exterior}$ must be $\geq gM_{interior}$

$gM_{interior} = 0.794$

TxDOT Policy states $gM_{Exterior}$ must be $\geq m \cdot N_L \div N_b$

$m \cdot N_L \div N_b = 0.85 * 3 / 6 = 0.425$

Is $OH \leq S/2$? Yes

Is $W \geq 20ft$? Yes

>> TxDOT Policy states that if $OH \leq S/2$, $gM_{Exterior}$ is $gM_{interior}$.

TxDOT Policy states that if $OH > S/2$ and $W < 20ft$, $gM_{Exterior}$ is the Maximum of: gM_{ext1} , $gM_{interior}$, and $m \cdot N_L \div N_b$.

TxDOT Policy states that if $OH > S/2$ and $W \geq 20ft$, $gM_{Exterior}$ is the Maximum of: gM_{ext1} , gM_{ext2+} , $gM_{interior}$, and $m \cdot N_L \div N_b$.

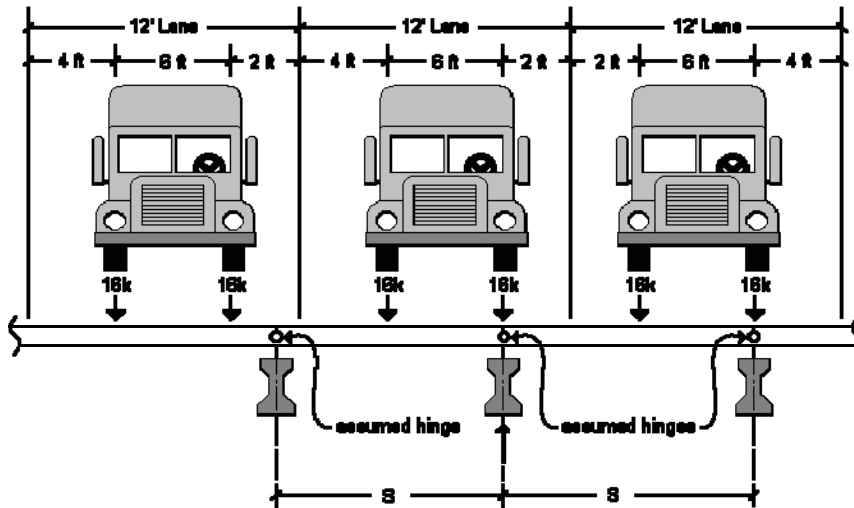
$gM_{exterior} = 0.794$

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LEVER RULE

$$S = 8.0 \text{ ft}$$

INTERIOR



For $S < 4$:

$$\text{One Lane} = \frac{16}{32} = 0.500$$

For $4 \leq S < 6$:

$$\text{One Lane} = \frac{16}{32} = 0.500$$

$$\text{Two Lanes} = \frac{16}{32} \left(1 + \frac{S-4}{S} \right) = 0.750$$

>: For $6 \leq S < 10$:

$$\text{One Lane} = \frac{16}{32} \left(1 + \frac{S-6}{S} \right) = 0.625$$

$$\text{Two Lanes} = \frac{16}{32} \left(1 + \frac{S-6}{S} + \frac{S-4}{S} \right) = 0.875$$

For $10 \leq S < 12$:

$$\text{One Lane} = \frac{16}{32} \left(1 + \frac{S-6}{S} \right) = 0.625$$

$$\text{Two Lanes} = \frac{16}{32} \left(1 + \frac{S-6}{S} + \frac{S-4}{S} + \frac{S-10}{S} \right) = 0.750$$

For $12 \leq S < 16$:

$$\text{One Lane} = \frac{16}{32} \left(1 + \frac{S-6}{S} \right) = 0.625$$

$$\text{Two Lanes} = \frac{16}{32} \left(1 + \frac{S-6}{S} + \frac{S-4}{S} + \frac{S-10}{S} \right) = 0.750$$

$$\text{Three Lanes} = \frac{16}{32} \left(1 + \frac{S-6}{S} + \frac{S-4}{S} + \frac{S-10}{S} + \frac{S-12}{S} \right) = 0.500$$

For $16 \leq S < 18$:

$$\text{One Lane} = \frac{16}{32} \left(1 + \frac{S-6}{S} \right) = 0.625$$

$$\text{Two Lanes} = \frac{16}{32} \left(1 + \frac{S-6}{S} + \frac{S-4}{S} + \frac{S-10}{S} \right) = 0.750$$

$$\text{Three Lanes} = \frac{16}{32} \left(1 + \frac{S-6}{S} + \frac{S-4}{S} + \frac{S-10}{S} + \frac{S-12}{S} \right) = 0.500$$

$$\text{Four Lanes} = \frac{16}{32} \left(1 + \frac{S-6}{S} + \frac{S-4}{S} + \frac{S-10}{S} + \frac{S-12}{S} + \frac{S-16}{S} \right) = 0.000$$

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LEVER RULE

$$S = 8.0 \text{ ft}$$

INTERIOR (con't)

For $18 \leq S < 22$:

$$\text{One Lane} = \frac{16}{32} \left(1 + \frac{S-6}{S} \right) = 0.625$$

$$\text{Two Lanes} = \frac{16}{32} \left(1 + \frac{S-6}{S} + \frac{S-4}{S} + \frac{S-10}{S} \right) = 0.750$$

$$\text{Three Lanes} = \frac{16}{32} \left(1 + \frac{S-6}{S} + \frac{S-4}{S} + \frac{S-10}{S} + \frac{S-12}{S} + \frac{S-18}{S} \right) = -0.125$$

$$\text{Four Lanes} = \frac{16}{32} \left(1 + \frac{S-6}{S} + \frac{S-4}{S} + \frac{S-10}{S} + \frac{S-12}{S} + \frac{S-18}{S} + \frac{S-16}{S} \right) = -0.625$$

For $22 \leq S \leq 24$:

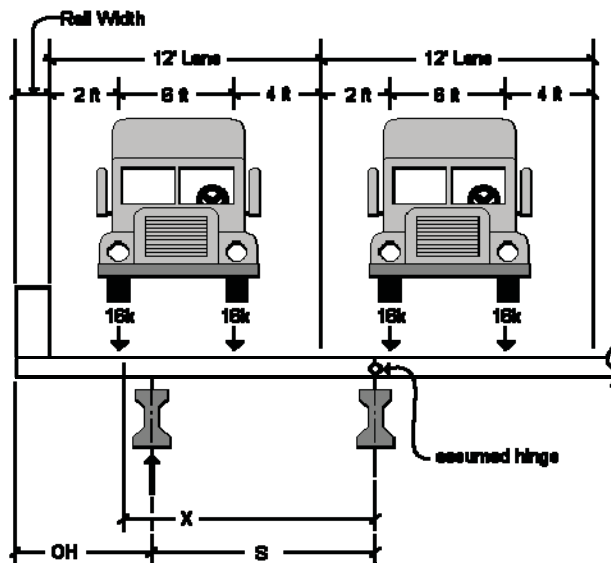
$$\text{One Lane} = \frac{16}{32} \left(1 + \frac{S-6}{S} \right) = 0.625$$

$$\text{Two Lanes} = \frac{16}{32} \left(1 + \frac{S-6}{S} + \frac{S-4}{S} + \frac{S-10}{S} \right) = 0.750$$

$$\text{Three Lanes} = \frac{16}{32} \left(1 + \frac{S-6}{S} + \frac{S-4}{S} + \frac{S-10}{S} + \frac{S-12}{S} + \frac{S-18}{S} \right) = -0.125$$

$$\text{Four Lanes} = \frac{16}{32} \left(1 + \frac{S-6}{S} + \frac{S-4}{S} + \frac{S-10}{S} + \frac{S-12}{S} + \frac{S-18}{S} + \frac{S-16}{S} + \frac{S-22}{S} \right) = -1.500$$

EXTERIOR



$$\begin{aligned}
 S &= 8.0 \text{ ft} \\
 OH &= 3.0 \text{ ft} \\
 \text{Rail Width} = RW &= 1.0 \text{ ft} \\
 X = S + OH - RW - 2\text{ft} &= 8.0 \text{ ft}
 \end{aligned}$$

For $X < 6$:

$$\text{One Lane} = \frac{16}{32} \left(\frac{X}{S} \right) = 0.500$$

>: For $6 \leq X < 12$:

$$\text{One Lane} = \frac{16}{32} \left(\frac{X}{S} + \frac{X-6}{S} \right) = 0.625$$

For $12 \leq X < 18$:

$$\text{One Lane} = \frac{16}{32} \left(\frac{X}{S} + \frac{X-6}{S} \right) = 0.625$$

$$\text{Two Lanes} = \frac{16}{32} \left(\frac{X}{S} + \frac{X-6}{S} + \frac{X-12}{S} \right) = 0.375$$

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LEVER RULE

EXTERIOR (con't)

$$S = 8.0 \text{ ft} \quad \text{OH} = 3.0 \text{ ft}$$

$$RW = 1.0 \text{ ft} \quad X = S + \text{OH} - RW - 2\text{ft} = 8.0 \text{ ft}$$

For $18 \leq X < 24$:

$$\text{One Lane} = \frac{16}{32} \left(\frac{X}{S} + \frac{X-6}{S} \right) = 0.625$$

$$\text{Two Lanes} = \frac{16}{32} \left(\frac{X}{S} + \frac{X-6}{S} + \frac{X-12}{S} + \frac{X-18}{S} \right) = -0.250$$

For $24 \leq X < 30$:

$$\text{One Lane} = \frac{16}{32} \left(\frac{X}{S} + \frac{X-6}{S} \right) = 0.625$$

$$\text{Two Lanes} = \frac{16}{32} \left(\frac{X}{S} + \frac{X-6}{S} + \frac{X-12}{S} + \frac{X-18}{S} \right) = -0.250$$

$$\text{Three Lanes} = \frac{16}{32} \left(\frac{X}{S} + \frac{X-6}{S} + \frac{X-12}{S} + \frac{X-18}{S} + \frac{X-24}{S} \right) = -1.250$$

For $30 \leq X < 36$:

$$\text{One Lane} = \frac{16}{32} \left(\frac{X}{S} + \frac{X-6}{S} \right) = 0.625$$

$$\text{Two Lanes} = \frac{16}{32} \left(\frac{X}{S} + \frac{X-6}{S} + \frac{X-12}{S} + \frac{X-18}{S} \right) = -0.250$$

$$\text{Three Lanes} = \frac{16}{32} \left(\frac{X}{S} + \frac{X-6}{S} + \frac{X-12}{S} + \frac{X-18}{S} + \frac{X-24}{S} + \frac{X-30}{S} \right) = -2.625$$

For $36 \leq X < 42$:

$$\text{One Lane} = \frac{16}{32} \left(\frac{X}{S} + \frac{X-6}{S} \right) = 0.625$$

$$\text{Two Lanes} = \frac{16}{32} \left(\frac{X}{S} + \frac{X-6}{S} + \frac{X-12}{S} + \frac{X-18}{S} \right) = -0.250$$

$$\text{Three Lanes} = \frac{16}{32} \left(\frac{X}{S} + \frac{X-6}{S} + \frac{X-12}{S} + \frac{X-18}{S} + \frac{X-24}{S} + \frac{X-30}{S} \right) = -2.625$$

$$\text{Four Lanes} = \frac{16}{32} \left(\frac{X}{S} + \frac{X-6}{S} + \frac{X-12}{S} + \frac{X-18}{S} + \frac{X-24}{S} + \frac{X-30}{S} + \frac{X-36}{S} \right) = -4.375$$

For $42 \leq X \leq 48$:

$$\text{One Lane} = \frac{16}{32} \left(\frac{X}{S} + \frac{X-6}{S} \right) = 0.625$$

$$\text{Two Lanes} = \frac{16}{32} \left(\frac{X}{S} + \frac{X-6}{S} + \frac{X-12}{S} + \frac{X-18}{S} \right) = -0.250$$

$$\text{Three Lanes} = \frac{16}{32} \left(\frac{X}{S} + \frac{X-6}{S} + \frac{X-12}{S} + \frac{X-18}{S} + \frac{X-24}{S} + \frac{X-30}{S} \right) = -2.625$$

$$\text{Four Lanes} = \frac{16}{32} \left(\frac{X}{S} + \frac{X-6}{S} + \frac{X-12}{S} + \frac{X-18}{S} + \frac{X-24}{S} + \frac{X-30}{S} + \frac{X-36}{S} + \frac{X-42}{S} \right) = -6.500$$

INTERIOR

One Lane Loaded = 0.625

Two Lanes Loaded = 0.875

Three Lanes Loaded = 0.875

Four Lanes Loaded = 0.875

EXTERIOR

One Lane Loaded = 0.625

Two Lanes Loaded = 0.625

Three Lanes Loaded = 0.625

Four Lanes Loaded = 0.625

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LRFD Live Load Distribution Factors*

Live Load Distribution Factors are calculated according to AASHTO LRFD Bridge Design Specifications, 4th Edition (2007 with no interim revisions) as prescribed by TxDOT policies (LRFD Design Manual July 2008) and practices. The Lever Rule is used when outside the Range of Applicability. The Range of Applicability for the Skew Correction Factors is ignored.

INPUT:

Beam Type = Tx54
 No. Beams, N_b = 6
 CL_{brg} to CL_{brg} , L = 106.75 ft
 Beam Spacing, S = 8.00 ft
 Avg. Skew Angle, θ = 0.00 deg
 Slab Thickness, t_s = 8 in
 Slab Overhang, OH = 3 ft
 Rail Width, RW = 1 ft
 Roadway Width, W = 44 ft
 Number of Lanes, N_L = 3

Deck Slab		Beam	
Conc wt =	0.145 k/ft ³	weight =	0.145 k/ft ³
f'_c =	4.0 ksi	f'_c =	8.5 ksi
E_{slab} =	3644 ksi	E_{beam} =	5312 ksi
		y_t =	30.49 in
		A =	817.0 in ²
		I =	299740 in ⁴

Longitudinal Stiffness Parameter: (4.6.2.2.1-1)

e_g (in) = 34.49 (dist. b/w cog of bm & deck)
 n = 1.000
 $K_g = n(I + Ae_g^2) = 1271611 \text{ in}^4$

**For typical cross sections (a,e,i,j & k). Table 4.6.2.2.1-1*

RESULTS:

	Final LLDF
Interior Shear LLDF, $gV_{interior}$	0.814
Interior Moment LLDF, $gM_{interior}$	0.649
Exterior Shear LLDF, $gV_{exterior}$	0.814
Exterior Moment LLDF, $gM_{exterior}$	0.649

The Final LLDF may be modified according to the following TxDOT policies:

- ◆ Exterior beams use the interior LLDF when $OH \leq S/2$.
- ◆ When $OH > S/2$ the exterior beam LLDF is determined by the lever rule for a single lane with a multiple presence factor of 1.0.
- ◆ In no case shall the LLDF for the exterior beams be less than the LLDFs for the interior beams.
- ◆ When the Roadway width is less than 20ft, all beams are designed for one lane loaded only.
- ◆ In no case shall the LLDF be less than $m \cdot N_L \cdot N_b$.

CALCULATIONS:

Shear LLDF Correction for Skew (Table 4.6.2.2.3c-1)

$$\text{Corr.} = 1.0 + 0.20 \left(\frac{12.0 L t_s^3}{K_g} \right)^{0.3} \tan \theta$$

$$= 1.0 + 0.20 * [(12.0 * 106.8 * 8^3) / (1,271,611)]^{0.3} * \tan(0)$$

$$\text{Corr.} = 1.000$$

Check θ : $0^\circ \leq 0^\circ \leq 60^\circ$ OK

Check S: $3.5' \leq 8.0' \leq 16.0'$ OK

Check L: $20' \leq 106.8' \leq 240'$ OK

Check N_b : $6 \geq 4$ OK

Moment LLDF Correction for Skew (Table 4.6.2.2.2e-1)

$$\text{Corr.} = 1 - c_1 (\tan \theta)^{1.5}$$

$$= 1 - 0 (\tan 0)^{1.5}$$

$$\text{Corr.} = 1.000$$

Check θ : $0^\circ < 30^\circ$

Set $\theta = 0^\circ$

where: $c_1 = 0.25 \left(\frac{K_g}{12.0 L t_s^3} \right)^{0.25} \left(\frac{S}{L} \right)^{0.5}$

$c_1 = 0.000$ because $\theta < 30^\circ$

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INTERIOR BEAM:

Shear LL Distribution Per Lane (Table 4.6.2.2.3a-1):

One Lane Loaded

Lever Rule (Table 3.6.1.1.2)

$$mg = 0.625 * 1.2 = 0.750$$

Modify for Skew:

$$\text{skew correction} = 1.000$$

$$mg = 0.750 * 1.000 = 0.750$$

Equation

$$g = 0.36 + \left(\frac{S}{25} \right)$$

$$g = 0.36 + (8 / 25) = 0.680$$

Modify for Skew:

$$\text{skew correction} = 1.000$$

$$g = 0.680 * 1.000 = 0.680$$

Range of Applicability (ROA) Checks

$$\text{Check S: } 3.5' \leq 8.0' \leq 16.0' \quad \text{OK}$$

$$\text{Check } t_s: 4.5" \leq 8.0" \leq 12.0" \quad \text{OK}$$

$$\text{Check L: } 20' \leq 106.8' \leq 240' \quad \text{OK}$$

$$\text{Check } N_b: 6 \geq 4 \quad \text{OK}$$

Use Equation from Table 4.6.2.2.3a-1 because all criteria is OK.

$$gV_{\text{int1}} = 0.680$$

Two or More Lanes Loaded

Lever Rule (Table 3.6.1.1.2)

$$mg = \text{Max}(0.875 * 1.0, 0.875 * 0.85, 0.875 * 0.65) = 0.875$$

Modify for Skew:

$$\text{skew correction} = 1.000$$

$$mg = 0.875 * 1.000 = 0.875$$

Equation

$$g = 0.2 + \left(\frac{S}{12} \right) - \left(\frac{S}{35} \right)^{2.0}$$

$$g = 0.2 + (8 / 12) - (8 / 35)^{2.0} = 0.814$$

Modify for Skew:

$$\text{skew correction} = 1.000$$

$$g = 0.814 * 1.000 = 0.814$$

Range of Applicability (ROA) Checks (same as for one lane loaded)

Use Equation from Table 4.6.2.2.3a-1 because all criteria is OK.

$$gV_{\text{int2+}} = 0.814$$

TxDOT Policy states gV_{Interior} must be $\geq m \cdot N_L + N_b$

$$m \cdot N_L + N_b = 0.85 * 3 / 6 = 0.425$$

Is $W \geq 20\text{ft}$? **Yes**

TxDOT Policy states that if $W < 20\text{ft}$, gV_{Interior} is the Maximum of: gV_{int1} and $m \cdot N_L + N_b$.

>> TxDOT Policy states that if $W \geq 20\text{ft}$, gV_{Interior} is the Maximum of: gV_{int1} , $gV_{\text{int2+}}$, $m \cdot N_L + N_b$.

$gV_{\text{Interior}} = 0.814$

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INTERIOR BEAM:

Moment LL Distribution Per Lane (Table 4.6.2.2.2b-1):

One Lane Loaded

Lever Rule (Table 3.6.1.1.2)

$$mg = 0.625 * 1.2 = 0.750$$

Modify for Skew:

$$\text{skew correction} = 1.000$$

$$mg = 0.750 * 1.000 = 0.750$$

Equation

$$g = 0.06 + \left(\frac{S}{14}\right)^{0.4} \left(\frac{S}{L}\right)^{0.3} \left(\frac{K_g}{12Lt_s^3}\right)^{0.1}$$

$$g = 0.06 + (8/14)^{0.4} * (8/106.8)^{0.3} * (1,271,611/(12*106.8*8^3))^{0.1} = 0.453$$

Modify for Skew:

$$\text{skew correction} = 1.000$$

$$g = 0.453 * 1.000 = 0.453$$

Range of Applicability (ROA) Checks

$$\text{Check } S: 3.5' \leq 8.0' \leq 16.0' \quad \text{OK}$$

$$\text{Check } t_s: 4.5" \leq 8.0" \leq 12.0" \quad \text{OK}$$

$$\text{Check } L: 20' \leq 106.8' \leq 240' \quad \text{OK}$$

$$\text{Check } N_b: 6 \geq 4 \quad \text{OK}$$

$$\text{Check } K_g: 10,000 \leq 1,271,611 \leq 7,000,000 \quad \text{OK}$$

Use Equation from Table 4.6.2.2.2b-1 because all criteria is OK.

$$gM_{int1} = 0.453$$

Two or More Lanes Loaded

Lever Rule (Table 3.6.1.1.2)

$$mg = \text{Max}(0.875 * 1.0, 0.875 * 0.85, 0.875 * 0.65) = 0.875$$

Modify for Skew:

$$\text{skew correction} = 1.000$$

$$mg = 0.875 * 1.000 = 0.875$$

Equation

$$g = 0.075 + \left(\frac{S}{9.5}\right)^{0.6} \left(\frac{S}{L}\right)^{0.2} \left(\frac{K_g}{12Lt_s^3}\right)^{0.1}$$

$$g = 0.075 + (8/9.5)^{0.6} * (8/106.8)^{0.2} * (1,271,611/(12*106.8*8^3))^{0.1} = 0.649$$

Modify for Skew:

$$\text{skew correction} = 1.000$$

$$g = 0.649 * 1.000 = 0.649$$

Range of Applicability (ROA) Checks (same as for one lane loaded)

Use Equation from Table 4.6.2.2.2b-1 because all criteria is OK.

$$gM_{int2+} = 0.649$$

TxDOT Policy states $gM_{Interior}$ must be $\geq m \cdot N_L \div N_b$

$$m \cdot N_L \div N_b = 0.85 * 3 / 6 = 0.425$$

Is $W \geq 20\text{ft}$? **Yes**

TxDOT Policy states that if $W < 20\text{ft}$, $gM_{Interior}$ is the Maximum of: gM_{int1} and $m \cdot N_L \div N_b$.

>> TxDOT Policy states that if $W \geq 20\text{ft}$, $gM_{Interior}$ is the Maximum of: gM_{int1} , gM_{int2+} , $m \cdot N_L \div N_b$.

$$gM_{interior} = 0.649$$

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EXTERIOR BEAM:

Shear LL Distribution Per Lane (Table 4.6.2.2.3b-1):

One Lane Loaded

Lever Rule (Table 3.6.1.1.2)

$$mg = 0.625 * 1.0 = 0.625$$

TxDOT uses a multiple presence factor of 1.0 for one lane loaded on the exterior beam.

Modify for Skew:

$$\text{skew correction} = 1.000$$

$$mg = 0.625 * 1.000 = 0.625$$

Use Lever Rule, as per AASHTO LRFD Table 4.6.2.2.3b-1.

$$gV_{\text{ext1}} = 0.625$$

Two or More Lanes Loaded

Lever Rule (Table 3.6.1.1.2)

$$mg = \text{Max}(0.625 * 1.0, 0.625 * 0.85, 0.625 * 0.65) = 0.625$$

Modify for Skew:

$$\text{skew correction} = 1.000$$

$$mg = 0.625 * 1.000 = 0.625$$

Equation

d_e = dist. b/w CL web to curb

d_e = OH - Rail Width

$$d_e = 3\text{ft} - 1\text{ft} = 2.0\text{ft}$$

$$e = 0.6 + \left(\frac{d_e}{10}\right)$$

$$e = 0.6 + (2.0/10) = 0.800$$

$g = e * gV_{\text{int2+Eq}}$

$$g = 0.800 * 0.814 = 0.651$$

Skew Correction is included in $gV_{\text{(interior)}}$.

Range of Applicability (ROA) Checks

Interior ROA is implicitly applied to the exterior beam.

Check Interior Beam ROA: OK

Check d_e : $-1.0' \leq 2.0' \leq 5.5'$ OK

Check N_b : $6 \neq 3$ OK

Use Equation from Table 4.6.2.2.3b-1 because all criteria is OK.

$$gV_{\text{ext2+}} = 0.651$$

TxDOT Policy states gV_{Exterior} must be $\geq gV_{\text{interior}}$

$$gV_{\text{interior}} = 0.814$$

TxDOT Policy states gV_{Exterior} must be $\geq m \cdot N_L + N_b$

$$m \cdot N_L + N_b = 0.85 * 3 / 6 = 0.425$$

Is $OH \leq S/2$? Yes

Is $W \geq 20\text{ft}$? Yes

>> TxDOT Policy states that if $OH \leq S/2$, gV_{Exterior} is gV_{interior} .

TxDOT Policy states that if $OH > S/2$ and $W < 20\text{ft}$, gV_{Exterior} is the Maximum of: gV_{ext1} , gV_{interior} , and $m \cdot N_L + N_b$.

TxDOT Policy states that if $OH > S/2$ and $W \geq 20\text{ft}$, gV_{Exterior} is the Maximum of: gV_{ext1} , $gV_{\text{ext2+}}$, gV_{interior} , and $m \cdot N_L + N_b$.

$gV_{\text{exterior}} = 0.814$

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EXTERIOR BEAM:

Moment LL Distribution Per Lane (Table 4.6.2.2d-1):

One Lane Loaded

Lever Rule

$mg = 0.625 * 1.0 = 0.625$ TxDOT uses a multiple presence factor of 1.0 for one lane loaded on the exterior beam.

Modify for Skew:

skew correction = 1.000

$mg = 0.625 * 1.000 = 0.625$

Use Lever Rule as per AASHTO LRFD Table 4.6.2.2d-1.

$gM_{ext1} = 0.625$

Two or More Lanes Loaded

Lever Rule (Table 3.6.1.1.2)

$mg = \text{Max}(0.625 * 1.0, 0.625 * 0.85, 0.625 * 0.65) = 0.625$

Modify for Skew:

skew correction = 1.000

$mg = 0.625 * 1.000 = 0.625$

Equation

$$e = 0.77 + \left(\frac{d_e}{9.1} \right)$$

$e = 0.77 + (2.0/9.1) = 0.990$

$g = e * gM_{int2+Eq}$

$g = 0.99 * 0.649 = 0.643$

Skew Correction included in $gM_{interior}$.

Range of Applicability (ROA) Checks

Interior ROA is implicitly applied to the exterior beam.

Check Interior Beam ROA: OK

Check d_e : $-1.0' \leq 2.0' \leq 5.5'$ OK

Check N_b : $6 \neq 3$ OK

Use Equation from Table 4.6.2.2d-1 because all criteria is OK.

$gM_{ext2+} = 0.643$

TxDOT Policy states $gM_{Exterior}$ must be $\geq gM_{interior}$

$gM_{interior} = 0.649$

TxDOT Policy states $gM_{Exterior}$ must be $\geq m \cdot N_L \div N_b$

$m \cdot N_L \div N_b = 0.85 * 3 / 6 = 0.425$

Is $OH \leq S/2$? Yes

Is $W \geq 20ft$? Yes

>> TxDOT Policy states that if $OH \leq S/2$, $gM_{Exterior}$ is $gM_{interior}$.

TxDOT Policy states that if $OH > S/2$ and $W < 20ft$, $gM_{Exterior}$ is the Maximum of: gM_{ext1} , $gM_{interior}$, and $m \cdot N_L \div N_b$.

TxDOT Policy states that if $OH > S/2$ and $W \geq 20ft$, $gM_{Exterior}$ is the Maximum of: gM_{ext1} , gM_{ext2+} , $gM_{interior}$, and $m \cdot N_L \div N_b$.

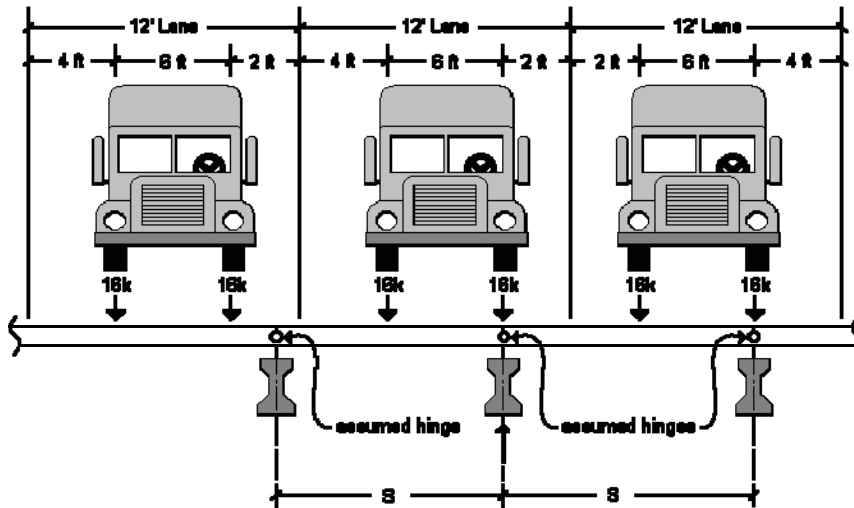
$gM_{exterior} = 0.649$

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LEVER RULE

$$S = 8.0 \text{ ft}$$

INTERIOR



For $S < 4$:

$$\text{One Lane} = \frac{16}{32} = 0.500$$

For $4 \leq S < 6$:

$$\text{One Lane} = \frac{16}{32} = 0.500$$

$$\text{Two Lanes} = \frac{16}{32} \left(1 + \frac{S-4}{S} \right) = 0.750$$

>: For $6 \leq S < 10$:

$$\text{One Lane} = \frac{16}{32} \left(1 + \frac{S-6}{S} \right) = 0.625$$

$$\text{Two Lanes} = \frac{16}{32} \left(1 + \frac{S-6}{S} + \frac{S-4}{S} \right) = 0.875$$

For $10 \leq S < 12$:

$$\text{One Lane} = \frac{16}{32} \left(1 + \frac{S-6}{S} \right) = 0.625$$

$$\text{Two Lanes} = \frac{16}{32} \left(1 + \frac{S-6}{S} + \frac{S-4}{S} + \frac{S-10}{S} \right) = 0.750$$

For $12 \leq S < 16$:

$$\text{One Lane} = \frac{16}{32} \left(1 + \frac{S-6}{S} \right) = 0.625$$

$$\text{Two Lanes} = \frac{16}{32} \left(1 + \frac{S-6}{S} + \frac{S-4}{S} + \frac{S-10}{S} \right) = 0.750$$

$$\text{Three Lanes} = \frac{16}{32} \left(1 + \frac{S-6}{S} + \frac{S-4}{S} + \frac{S-10}{S} + \frac{S-12}{S} \right) = 0.500$$

For $16 \leq S < 18$:

$$\text{One Lane} = \frac{16}{32} \left(1 + \frac{S-6}{S} \right) = 0.625$$

$$\text{Two Lanes} = \frac{16}{32} \left(1 + \frac{S-6}{S} + \frac{S-4}{S} + \frac{S-10}{S} \right) = 0.750$$

$$\text{Three Lanes} = \frac{16}{32} \left(1 + \frac{S-6}{S} + \frac{S-4}{S} + \frac{S-10}{S} + \frac{S-12}{S} \right) = 0.500$$

$$\text{Four Lanes} = \frac{16}{32} \left(1 + \frac{S-6}{S} + \frac{S-4}{S} + \frac{S-10}{S} + \frac{S-12}{S} + \frac{S-16}{S} \right) = 0.000$$

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LEVER RULE

$$S = 8.0 \text{ ft}$$

INTERIOR (con't)

For $18 \leq S < 22$:

$$\text{One Lane} = \frac{16}{32} \left(1 + \frac{S-6}{S} \right) = 0.625$$

$$\text{Two Lanes} = \frac{16}{32} \left(1 + \frac{S-6}{S} + \frac{S-4}{S} + \frac{S-10}{S} \right) = 0.750$$

$$\text{Three Lanes} = \frac{16}{32} \left(1 + \frac{S-6}{S} + \frac{S-4}{S} + \frac{S-10}{S} + \frac{S-12}{S} + \frac{S-18}{S} \right) = -0.125$$

$$\text{Four Lanes} = \frac{16}{32} \left(1 + \frac{S-6}{S} + \frac{S-4}{S} + \frac{S-10}{S} + \frac{S-12}{S} + \frac{S-18}{S} + \frac{S-16}{S} \right) = -0.625$$

For $22 \leq S \leq 24$:

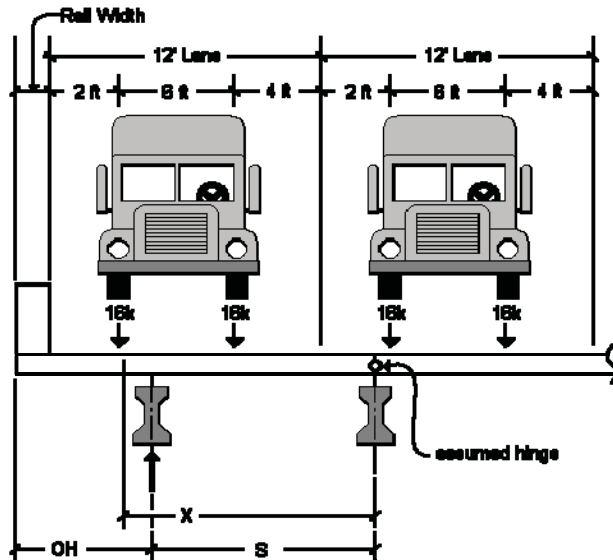
$$\text{One Lane} = \frac{16}{32} \left(1 + \frac{S-6}{S} \right) = 0.625$$

$$\text{Two Lanes} = \frac{16}{32} \left(1 + \frac{S-6}{S} + \frac{S-4}{S} + \frac{S-10}{S} \right) = 0.750$$

$$\text{Three Lanes} = \frac{16}{32} \left(1 + \frac{S-6}{S} + \frac{S-4}{S} + \frac{S-10}{S} + \frac{S-12}{S} + \frac{S-18}{S} \right) = -0.125$$

$$\text{Four Lanes} = \frac{16}{32} \left(1 + \frac{S-6}{S} + \frac{S-4}{S} + \frac{S-10}{S} + \frac{S-12}{S} + \frac{S-18}{S} + \frac{S-16}{S} + \frac{S-22}{S} \right) = -1.500$$

EXTERIOR



$$\begin{aligned} S &= 8.0 \text{ ft} \\ OH &= 3.0 \text{ ft} \\ \text{Rail Width} = RW &= 1.0 \text{ ft} \\ X = S + OH - RW - 2\text{ft} &= 8.0 \text{ ft} \end{aligned}$$

For $X < 6$:

$$\text{One Lane} = \frac{16}{32} \left(\frac{X}{S} \right) = 0.500$$

>: For $6 \leq X < 12$:

$$\text{One Lane} = \frac{16}{32} \left(\frac{X}{S} + \frac{X-6}{S} \right) = 0.625$$

For $12 \leq X < 18$:

$$\text{One Lane} = \frac{16}{32} \left(\frac{X}{S} + \frac{X-6}{S} \right) = 0.625$$

$$\text{Two Lanes} = \frac{16}{32} \left(\frac{X}{S} + \frac{X-6}{S} + \frac{X-12}{S} \right) = 0.375$$

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LEVER RULE

EXTERIOR (con't)

$$S = 8.0 \text{ ft} \quad \text{OH} = 3.0 \text{ ft}$$

$$RW = 1.0 \text{ ft} \quad X = S + \text{OH} - RW - 2\text{ft} = 8.0 \text{ ft}$$

For $18 \leq X < 24$:

$$\text{One Lane} = \frac{16}{32} \left(\frac{X}{S} + \frac{X-6}{S} \right) = 0.625$$

$$\text{Two Lanes} = \frac{16}{32} \left(\frac{X}{S} + \frac{X-6}{S} + \frac{X-12}{S} + \frac{X-18}{S} \right) = -0.250$$

For $24 \leq X < 30$:

$$\text{One Lane} = \frac{16}{32} \left(\frac{X}{S} + \frac{X-6}{S} \right) = 0.625$$

$$\text{Two Lanes} = \frac{16}{32} \left(\frac{X}{S} + \frac{X-6}{S} + \frac{X-12}{S} + \frac{X-18}{S} \right) = -0.250$$

$$\text{Three Lanes} = \frac{16}{32} \left(\frac{X}{S} + \frac{X-6}{S} + \frac{X-12}{S} + \frac{X-18}{S} + \frac{X-24}{S} \right) = -1.250$$

For $30 \leq X < 36$:

$$\text{One Lane} = \frac{16}{32} \left(\frac{X}{S} + \frac{X-6}{S} \right) = 0.625$$

$$\text{Two Lanes} = \frac{16}{32} \left(\frac{X}{S} + \frac{X-6}{S} + \frac{X-12}{S} + \frac{X-18}{S} \right) = -0.250$$

$$\text{Three Lanes} = \frac{16}{32} \left(\frac{X}{S} + \frac{X-6}{S} + \frac{X-12}{S} + \frac{X-18}{S} + \frac{X-24}{S} + \frac{X-30}{S} \right) = -2.625$$

For $36 \leq X < 42$:

$$\text{One Lane} = \frac{16}{32} \left(\frac{X}{S} + \frac{X-6}{S} \right) = 0.625$$

$$\text{Two Lanes} = \frac{16}{32} \left(\frac{X}{S} + \frac{X-6}{S} + \frac{X-12}{S} + \frac{X-18}{S} \right) = -0.250$$

$$\text{Three Lanes} = \frac{16}{32} \left(\frac{X}{S} + \frac{X-6}{S} + \frac{X-12}{S} + \frac{X-18}{S} + \frac{X-24}{S} + \frac{X-30}{S} \right) = -2.625$$

$$\text{Four Lanes} = \frac{16}{32} \left(\frac{X}{S} + \frac{X-6}{S} + \frac{X-12}{S} + \frac{X-18}{S} + \frac{X-24}{S} + \frac{X-30}{S} + \frac{X-36}{S} \right) = -4.375$$

For $42 \leq X \leq 48$:

$$\text{One Lane} = \frac{16}{32} \left(\frac{X}{S} + \frac{X-6}{S} \right) = 0.625$$

$$\text{Two Lanes} = \frac{16}{32} \left(\frac{X}{S} + \frac{X-6}{S} + \frac{X-12}{S} + \frac{X-18}{S} \right) = -0.250$$

$$\text{Three Lanes} = \frac{16}{32} \left(\frac{X}{S} + \frac{X-6}{S} + \frac{X-12}{S} + \frac{X-18}{S} + \frac{X-24}{S} + \frac{X-30}{S} \right) = -2.625$$

$$\text{Four Lanes} = \frac{16}{32} \left(\frac{X}{S} + \frac{X-6}{S} + \frac{X-12}{S} + \frac{X-18}{S} + \frac{X-24}{S} + \frac{X-30}{S} + \frac{X-36}{S} + \frac{X-42}{S} \right) = -6.500$$

INTERIOR

$$\text{One Lane Loaded} = 0.625$$

$$\text{Two Lanes Loaded} = 0.875$$

$$\text{Three Lanes Loaded} = 0.875$$

$$\text{Four Lanes Loaded} = 0.875$$

EXTERIOR

$$\text{One Lane Loaded} = 0.625$$

$$\text{Two Lanes Loaded} = 0.625$$

$$\text{Three Lanes Loaded} = 0.625$$

$$\text{Four Lanes Loaded} = 0.625$$



County: Any
 Highway: Any
 C-S-J: XXXX-XX-XXX
Bridge Division Rev: 09/26/08

Descrip: LRFD Inverted Tee Cap Design Example - Bent 2
 Design: BRG Ck Dsn: BRG
 Date: Apr-10

CONCRETE SECTION SHEAR CAPACITY BY AASHTO LRFD BRIDGE DESIGN SPECIFICATIONS, FOURTH EDITION, 2007

Resistance Factors:

$\phi_V =$	0.9
$\phi_M =$	0.9
$\phi_N =$	0.75

Units: **US**

Concrete:	$f'_c =$ 3.6 ksi	$E_c =$ 3453 ksi	Mild Steel:	$f_y =$ 60 ksi	$E_s =$ 29000 ksi	Prestressed Steel:	$f_{pu} =$ 270 ksi	$E_p =$ 28500 ksi
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		SECTIONS							
Units		8	12	32	36	56	60	80	84

Input Data

Bending moment, Mu	kip-ft	429.2	619.9	507.9	335.6	335.6	507.9	619.9	429
Shear force, Vu	kip	419.8	239.8	247.3	448.1	448.1	247.3	239.8	419.8
Axial force, Nu (+ if tensile)	kip	0	0	0	0	0	0	0	0
Web width, bv	in	39.00	39.00	39.00	39.00	39.00	39.00	39.00	39.00
Shear depth, dv	in	80.58	80.58	80.58	80.58	80.58	80.58	80.58	80.58
Mild steel reinf. area, As	in ²	7.8	7.8	7.8	7.8	7.8	7.8	7.8	7.8
Conc area on tension side, Ac	in ²	1657.5	1657.5	1657.5	1657.5	1657.5	1657.5	1657.5	1657.5
Area of stirrups, Av	in ²	1.76	1.76	1.76	1.76	1.76	1.76	1.76	1.76
Stirrup spacing, s	in	8.5	8.5	8.5	8.5	8.5	8.5	8.5	8.5
Prestressed steel area, Aps	in ²								
Prestress shear, Vp	kip								
Average prestress, fps	ksi								
Torsional moment, Tu	kip-ft	660	330	330	660	660	330	330	660
Shear flow area, Ao	in ²	3329	3329	3329	3329	3329	3329	3329	3329
Area of one leg of stirrup, At	in ²	0.44	0.44	0.44	0.44	0.44	0.44	0.44	0.44
Perimeter of stirrup, Ph	in	332	332	332	332	332	332	332	332

Calculated Values

Vc	kip	420.2	431.5	427.7	420.2	420.2	427.7	431.5	420.2
Vs	kip	1251.3	1355.4	1345.1	1251.3	1251.3	1345.1	1355.4	1251.3
ϕV_n	kip	1504	1608	1595	1504	1504	1595	1608	1504
ϵ_x		1.00E-03	9.03E-04	9.28E-04	1.00E-03	1.00E-03	9.28E-04	9.03E-04	1.00E-03
θ	deg	36.40	35.40	35.60	36.40	36.40	35.60	35.40	36.40
β		2.230	2.290	2.270	2.230	2.230	2.270	2.290	2.230
Req'd Shear reinf. Av/S	in ² /in	0.007	0.000	0.000	0.012	0.012	0.000	0.000	0.007
Req'd Torsion reinf. At/S	in ² /in	0.016	0.008	0.008	0.016	0.016	0.008	0.008	0.016
Maximum stirrup spacing, Smax	in	24.0	24.0	24.0	22.9	22.9	24.0	24.0	24.0

Conclusion

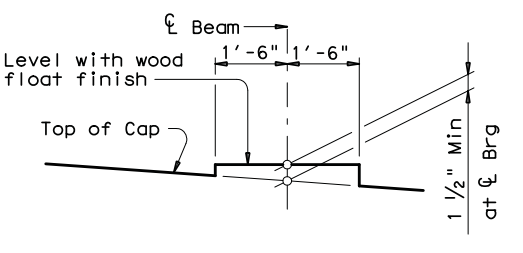
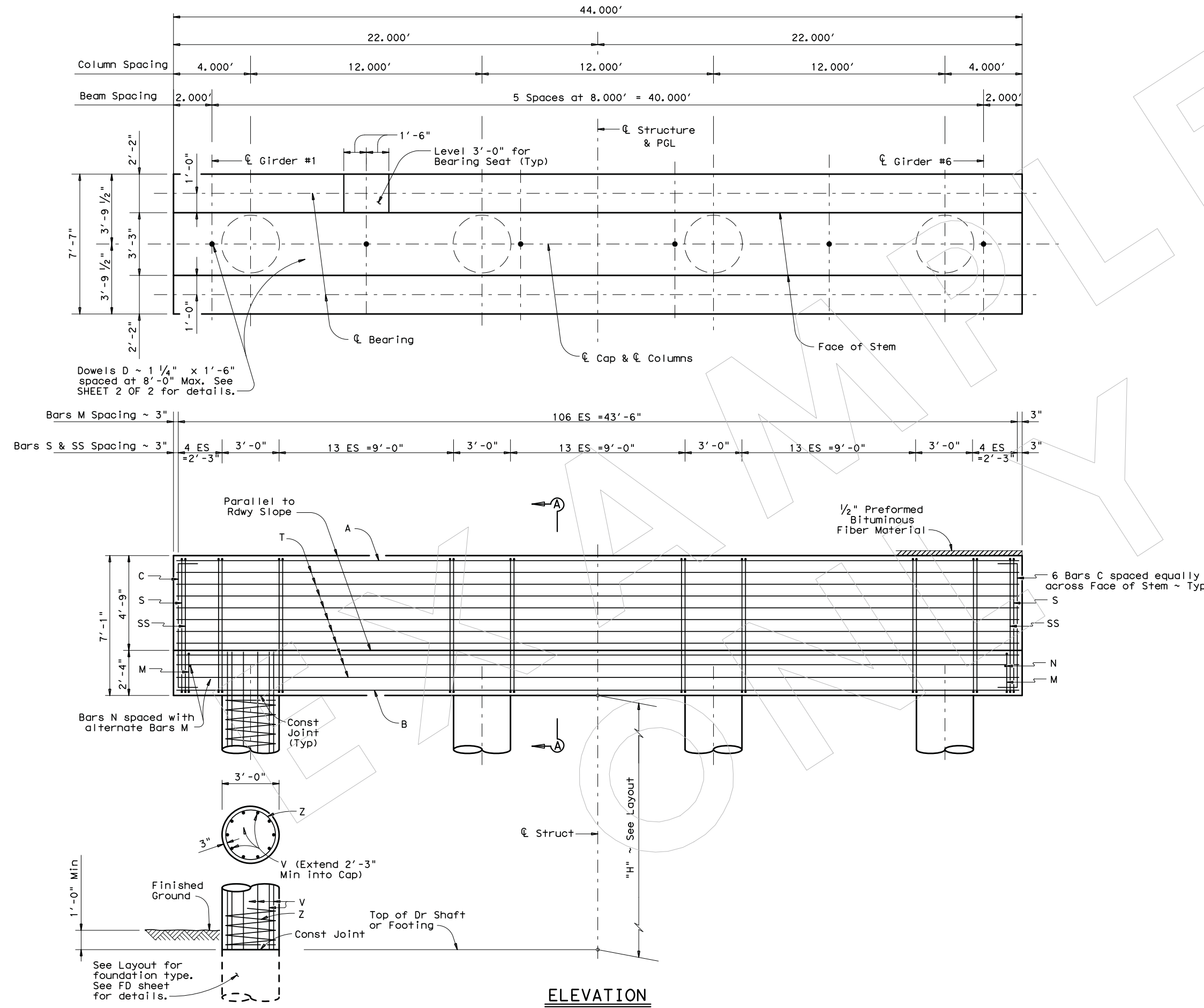
Shear Reinforcing	OK	OK	OK	OK	OK	OK	OK	OK	OK
Longitudinal Reinforcing	FAILED	OK	OK	FAILED	FAILED	OK	OK	OK	FAILED

Note: Longitudinal Reinforcing check can be ignored for typical multi-column bent caps. For straddle bents with no overhangs, this check must be considered. Refer to LRFD 5.8.3.5 for further information.
 If torsion is not being considered, leave last five rows of input data blank.

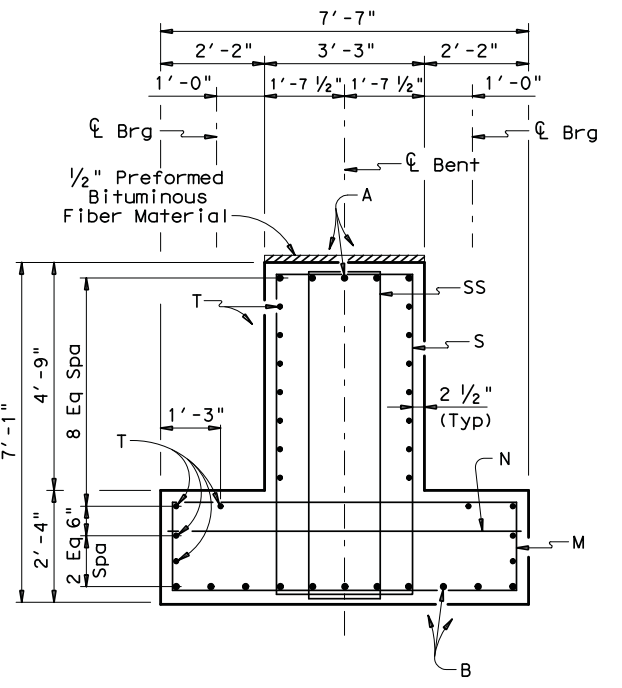
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LEVELS DISPLAYED

1	ACC:
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BEARING SEAT DETAIL
 (Bearing surface shall be clean and free of all loose material before placing bearing pad.)



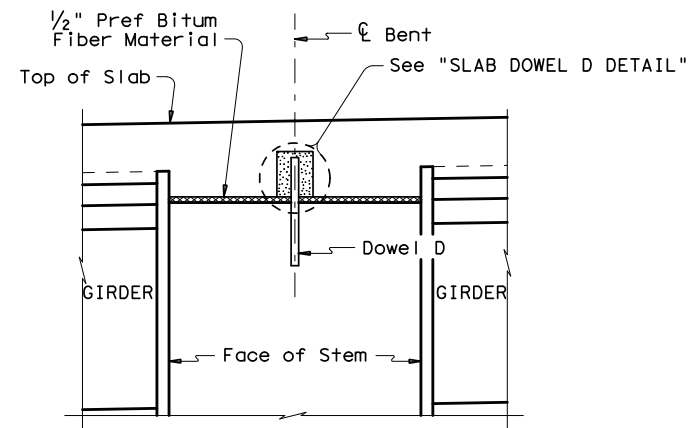
SECTION A-A

ELEVATION

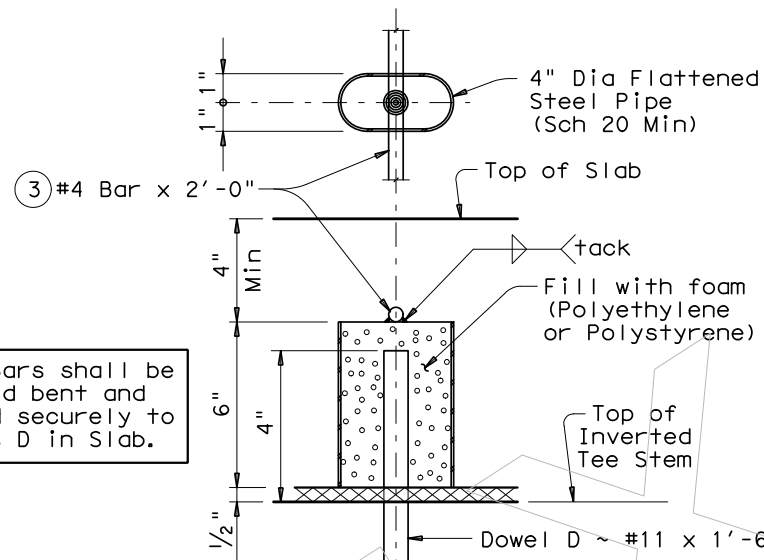
HL-93 LOADING	SHEET 1 OF 2
<p>Texas Department of Transportation Design Division (Bridge)</p>	
INTERIOR BENT	
INVERTED TEE BENT CAP	
DESIGN EXAMPLE	
FILE: XXXX1+01.dgn	DN: BRG CK: BRG DW: BRG CK: BRG
© TxDOT April 2010	DISTRICT FEDERAL AID PROJECT SHEET
REVISIONS	ANY XX XXXX (XXX) XXX
COUNTY	CONTROL SECT JOB HIGHWAY
ANY	XXXX XX XXX ANY
June 2010	

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LEVELS DISPLAYED	ACC:
1	

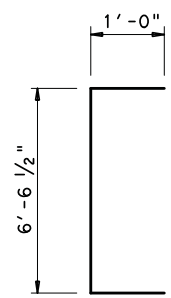


LONGITUDINAL SECT THRU SLAB AT INVERTED-TEE BENT

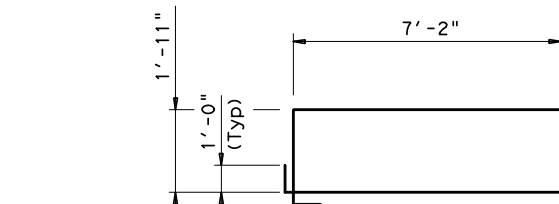


SLAB DOWEL D DETAIL

③ #4 Bars shall be field bent and tied securely to Bars D in Slab.

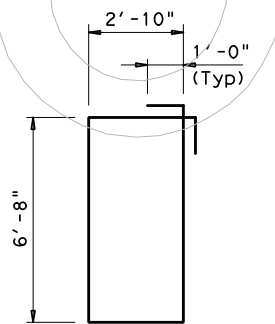


BARS C

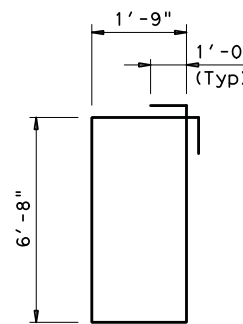


Lap shall be located at bottom of StIRRup. Alternate lap location.

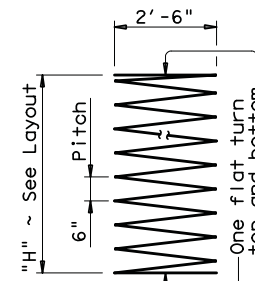
BARS M



BARS S



BARS SS



BARS Z

TABLES OF CONSTANT QUANTITIES

Bar	No.	Size	Length	Weight
A	5	#11	43'-8"	1160
B	11	#11	43'-8"	2552
C	12	# 5	8'-7"	107
D	6	#11	1'-6"	48
M	107	#6	20'-2"	3241
N	54	#6	7'-3"	588
S	52	#6	21'-0"	1640
SS	55	#6	18'-10"	1471
T	20	#6	43'-8"	1443
Reinforcing Steel				Lb 12,250
Class "C" Concrete				CY 54.4

① TABLE OF VARIABLE QUANTITIES FOR 4 COLUMNS						② TOTAL ESTIMATED QUANTITIES	
"H"	Class "C" Conc (Cols)	Bars V 40 ~ #9	Bars Z 4 ~ #3 Spiral	Reinf Steel	Class "C" Conc		
Ft	CY	Length	Weight	Length	Weight	Lb	CY
22	23.0	24'-3"	3,298	362'	544	15,962	77.4
12	12.6	14'-3"	1,938	205'	308	14,366	67.0

- ① Adjust Bars V length by 1 Ft and Bars Z length by 15.740 Ft for each linear foot of variation in "H" value.
- ② Adjust Reinforcing Steel Total by 160 Lbs and Class "C" Conc by 1.047 CY for each linear foot of variation in "H" value.

GENERAL NOTES:
 Designed according to AASHTO LRFD Bridge Design Specifications, 5th Edition (2010).
 Class "C" concrete strength $f'_c = 3,600$ psi.
 All Cap reinforcing shall be Grade 60.
 Column and Drilled Shaft reinforcing may be Grade 40.
 See Foundation Detail Standard Sheet, FD, for all foundation details and notes.
 Calculated Foundation Load = 210 Tons/Or Short

HL-93 LOADING SHEET 2 OF 2

Texas Department of Transportation
 Design Division (Bridge)

**INTERIOR BENT
 INVERTED TEE BENT CAP
 DESIGN EXAMPLE**

FILE: XXXX1+01.dgn	DN: BRG	CK: BRG	DW: BRG	CK: BRG
© TxDOT June 2010	DISTRICT	FEDERAL AID PROJECT		SHEET
REVISIONS	ANY	XX XXXX (XXX)		XXX
	COUNTY	CONTROL	SECT	JOB HIGHWAY
	ANY	XXXX	XX	XXX ANY