# New York Progress Mathematics 

Correlation to the New York State Next Generation Mathematics Learning Standards (2017) чрранео unе е 2019

## Grade 6



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## NY-6.RP

## RATIO AND PROPORTIONAL REASONING

Grade 6 Content Standards
New York Progress Mathematics, Grade 6

| Understand ratio concepts and use ratio reasoning to solve problems. |  |
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| NY-6.RP. 1 Understand the concept of a ratio and use ratio language to describe a ratio relationship between two quantities. <br> e.g., "The ratio of wings to beaks in the bird house at the zoo was $2: 1$, because for every 2 wings there was 1 beak." "For every vote candidate A received, candidate C received three votes." | Lesson 1 <br> Understand Ratios and Unit Rates-pp. 10-17 |
| NY-6.RP. 2 Understand the concept of a unit rate $a / b$ associated with a ratio $a: b$ with $b \neq 0$ ( $b$ not equal to zero), and use rate language in the context of a ratio relationship. <br> e.g., "This recipe has a ratio of 3 cups of flour to 4 cups of sugar, so there are $3 / 4$ cup of flour for each cup of sugar." "We paid $\$ 75$ for 15 hamburgers, which is a rate of $\$ 5$ per hamburger." <br> Note: Expectations for unit rates in this grade are limited to non-complex fractions. | Lesson 1 <br> Understand Ratios and Unit Rates-pp. 10-17 |
| NY-6.RP. 3 Use ratio and rate reasoning to solve real-world and mathematical problems. <br> Note: Strategies may include but are not limited to the following: tables of equivalent ratios, tape diagrams, double number lines, and equations. | Lesson 8 <br> Problem Solving: Ratios and Rates-pp. 66-73 |
| NY-6.RP.3a Make tables of equivalent ratios relating quantities with whole-number measurements, find missing values in the tables, and plot the pairs of values on the coordinate plane. Use tables to compare ratios. | Lesson 2 <br> Use Ratio Tables to Find Equivalent Ratios-pp. 18-25 <br> Lesson 3 <br> Use Ratio Tables to Compare Ratios-pp. 26-33 |
| NY-6.RP.3b Solve unit rate problems. <br> e.g., If it took 7 hours to mow 4 lawns, then at that rate, how many lawns could be mowed in 35 hours? At what rate were lawns being mowed? What is the unit rate? | Lesson 4 <br> Solve Unit Rate Problems-pp. 34-41 |

## NY-6.RP RATIO AND PROPORTIONAL REASONING

| Note: Problems may include unit pricing and constant speed. |  |
| :---: | :---: |
| NY-6.RP.3c Find a percent of a quantity as a rate per 100. Solve problems that involve finding the whole given a part and the percent, and finding a part of a whole given the percent. <br> e.g., $30 \%$ of a quantity means $\frac{30}{100}$ times the quantity. | Lesson 5 <br> Calculate a Percent of a Quantity—pp. 42-49 <br> Lesson 6 <br> Find the Whole Given a Part and the Percent-pp. $50-57$ |
| NY-6.RP.3d Use ratio reasoning to convert measurement units; manipulate and transform units appropriately when multiplying or dividing quantities. <br> Note: Conversion of units occur within a given measurement system, not across different measurement systems. | Lesson 7 <br> Convert Measurement Units—pp. 58-65 |

## NY-6.NS THE NUMBER SYSTEM

## Grade 6 Content Standards

New York Progress Mathematics, Grade 6

Apply and extend previous understandings of multiplication and division to divide fractions by fractions.

NY-6.NS. 1 Interpret and compute quotients of fractions, and solve word problems involving division of fractions by fractions.

Note: Strategies may include but are not limited to the following: using visual fraction models, a standard algorithm, and equations to represent the problem. e.g., Create a story context for $\left(\frac{2}{3}\right) \div\left(\frac{3}{4}\right)$ and use a visual fraction model to show the quotient; use the relationship between multiplication and division to explain that $\left(\frac{2}{3}\right) \div\left(\frac{3}{4}\right)=\frac{8}{9}$ because $\frac{3}{4}$ of $\frac{8}{9}$ is $\frac{2}{3}$. In general, $\left(\frac{a}{b}\right) \div\left(\frac{c}{d}\right)=\frac{a d}{b c}$.
continued

## Lesson 9

Divide a Fraction by a Fraction-pp. 80-87

## Lesson 10

Problem Solving: Fraction Division-pp. 88-95

## NY-6.NS

## THE NUMBER SYSTEM

Grade 6 Content Standards

## e.g.,

- How much chocolate will each person get if 3 people share $\frac{1}{2} \mathrm{lb}$ of chocolate equally?
- How many $\frac{3}{4}$ cup servings are in $\frac{2}{3}$ of a cup of yogurt?
- How wide is a rectangular strip of land with length $\frac{3}{4} \mathrm{mi}$. and area $\frac{1}{2}$ square mi.?

| Compute fluently with multi-digit numbers and find common factors and multiples. |  |
| :---: | :---: |
| NY-6.NS. 2 Fluently divide multi-digit numbers using a standard algorithm. | Lesson 11 <br> Divide Multi-digit Numbers-pp. 96-103 |
| NY-6.NS. 3 Fluently add, subtract, multiply, and divide multi-digit decimals using a standard algorithm for each operation. | Lesson 12 <br> Add and Subtract Multi-digit Decimals-pp. 104-111 <br> Lesson 13 <br> Multiply and Divide Multi-digit Decimals-pp. 112-119 |
| NY-6.NS. 4 Find the greatest common factor of two whole numbers less than or equal to 100. Use the distributive property to express a sum of two whole numbers 1-100 with a common factor as a multiple of a sum of two whole numbers with no common factor other than 1 . Find the least common multiple of two whole numbers less than or equal to 12. <br> e.g., Express $36+8$ as $4(9+2)$. | Lesson 14 <br> Find the Greatest Common Factor and Least Common Multiple-pp. 120-127 |

## Apply and extend previous understandings of numbers to the system of rational numbers.

NY-6.NS. 5 Understand that positive and negative numbers are used together to describe quantities having opposite directions or values. Use positive and negative numbers to represent quantities in real-world contexts, explaining the meaning of 0 in each situation.
continued

## Lesson 15

Understand Positive and Negative Numbers and Opposites-pp. 128-135

## NY-6.NS <br> THE NUMBER SYSTEM

Grade 6 Content Standards

| e.g., temperature above/below zero, elevation above/ <br> below sea level, debits/credits, positive/negative <br> electric charge. |  |
| :--- | :--- |
| NY-6.NS.6 Understand a rational number as a <br> point on the number line. Use number lines and <br> coordinate axes to represent points on a number <br> line and in the coordinate plane with negative <br> number coordinates. |  |
| NY-6.NS.6a Recognize opposite signs of <br> numbers as indicating locations on opposite <br> sides of O on the number line. Recognize that <br> the opposite of the opposite of a number <br> is the number itself, and that O is its own <br> opposite. | Understand Positive and Negative Numbers and <br> Opposites-pp. 128-135 |

## NY-6.NS <br> THE NUMBER SYSTEM

| NY-6.NS.7b Write, interpret, and explain statements of order for rational numbers in real-world contexts. <br> e.g., Write $-3^{\circ} \mathrm{C}>-7^{\circ} \mathrm{C}$ to express the fact that $-3^{\circ} \mathrm{C}$ is warmer than $-7^{\circ} \mathrm{C}$. | Lesson 17 <br> Compare and Order Rational Numbers-pp. 144-151 |
| :---: | :---: |
| NY-6.NS.7c Understand the absolute value of a rational number as its distance from O on the number line. Interpret absolute value as magnitude for a positive or negative quantity in a real-world situation. <br> e.g., For an account balance of -30 dollars, write $\|-30\|=30$ to describe the size of the debt in dollars. | Lesson 18 <br> Understand Absolute Value—pp. 152-159 |
| NY-6.NS.7d Distinguish comparisons of absolute value from statements about order. <br> e.g., Someone with a balance of $\$ 100$ in their bank account has more money than someone with a balance of $-\$ 1000$, because $100>-1000$. But, the second debt balance is much greater than the first person's credit balance because $\|-1000\|>\|100\|$. | Lesson 18 <br> Understand Absolute Value—pp. 152-159 |
| NY-6.NS. 8 Solve real-world and mathematical problems by graphing points on a coordinate plane. Include use of coordinates and absolute value to find distances between points with the same first coordinate or the same second coordinate. | Lesson 19 <br> Problem Solving: The Coordinate Plane—pp. 160-167 |

## NY-6.EE EQUATIONS AND EXPRESSIONS (INEQUALITIES)

Grade 6 Content Standards
New York Progress Mathematics, Grade 6

Apply and extend previous understandings of arithmetic to algebraic expressions.
NY-6.EE. 1 Write and evaluate numerical expressions involving whole-number exponents.

## Lesson 20

Write and Evaluate Numerical Expressions with
Exponents —pp. 174-181

## NY-6.EE EQUATIONS AND EXPRESSIONS (INEQUALITIES)

Grade 6 Content Standards

NY-6.EE. 2 Write, read, and evaluate expressions in which letters stand for numbers.

NY-6.EE.2a Write expressions that record operations with numbers and with letters standing for numbers.
e.g., Express the calculation "Subtract $y$ from 5" as $5-y$.

NY-6.EE.2b Identify parts of an expression using mathematical terms (term, coefficient, sum, difference, product, factor, and quotient); view one or more parts of an expression as a single entity.
e.g., Describe the expression $2(8+7)$ as a product of two factors; view $(8+7)$ as both a single entity and a sum of two terms.

NY-6.EE.2c Evaluate expressions given specific values for their variables. Include expressions that arise from formulas in real-world problems. Perform arithmetic operations, including those involving wholenumber exponents, in the conventional order (Order of Operations).
e.g., Use the formulas $V=s^{3}$ and $S A=6 s^{2}$ to find the volume and surface area of a cube with sides of length $s=1 / 2$.

Note: Expressions may or may not include parentheses. Nested grouping symbols are not included.

NY-6.EE. 3 Apply the properties of operations to generate equivalent expressions.
e.g., Apply the distributive property to the expression $3(2+x)$ to produce the equivalent expression $6+3 x$; apply the distributive property to the expression $24 x+18 y$ to produce the equivalent expression $6(4 x+3 y)$; apply properties of operations to $y+y+y$ to produce the equivalent expression $3 y$.

## Lesson 21

Write Algebraic Expressions to Record
Operations-pp. 182-189

## Lesson 22

Identify Parts of an Expression-pp. 190-197

## Lesson 23

Evaluate Algebraic Expressions—pp. 198-205

## Lesson 24

Generate and Identify Equivalent Expressionspp. 206-213

## NY-6.EE EQUATIONS AND EXPRESSIONS (INEQUALITIES)

Grade 6 Content Standards

NY-6.EE. 4 Identify when two expressions are equivalent.
e.g., The expressions $y+y+y$ and $3 y$ are equivalent because they name the same number regardless of which number $y$ represents.

New York Progress Mathematics, Grade 6

## Lesson 24

Generate and Identify Equivalent Expressionspp. 206-213

## Reason about and solve one-variable equations and inequalities.

NY-6.EE. 5 Understand solving an equation or inequality as a process of answering a question: which values from a specified set, if any, make the equation or inequality true? Use substitution to determine whether a given number in a specified set makes an equation or inequality true.

NY-6.EE. 6 Use variables to represent numbers and write expressions when solving a real-world or mathematical problem. Understand that a variable can represent an unknown number, or, depending on the purpose at hand, any number in a specified set.

NY-6.EE. 7 Solve real-world and mathematical problems by writing and solving equations of the form $x+p=q ; x-p=q ; p x=q ;$ and $\frac{x}{p}=q$ for cases in which $p, q$ and $x$ are all nonnegative rational.

Note: For the $\frac{x}{p}=q$ case, $p \neq 0$.
NY-6.EE. 8 Write an inequality of the form $x>c, x \geq c, x \leq c$ or $x<c$ to represent a constraint or condition in a real-world or mathematical problem. Recognize that inequalities of these forms have infinitely many solutions; represent solutions of such inequalities on a number line.

## Lesson 25

Identify Solutions to Equations and Inequalitiespp. 214-221

## Lesson 26

Write Algebraic Expressions to Represent Problems—pp. 222-229

## Lesson 27

Solve Equations of the Form $x+p=q-p p$. 230-237

## Lesson 28

Solve Equations of the Form px = q-pp. 238-245

## Lesson 29

Graph Solutions to Inequalities—pp. 246-253

## NY-6.EE EQUATIONS AND EXPRESSIONS (INEQUALITIES)

Represent and analyze quantitative relationships between dependent and independent variables.

NY-6.EE. 9 Use variables to represent two quantities in a real-world problem that change in relationship to one another.

Given a verbal context and an equation, identify the dependent variable, in terms of the other quantity, thought of as the independent variable. Analyze the relationship between the dependent and independent variables using graphs and tables, and relate these to the equation.
e.g., In a problem involving motion at constant speed, list and graph ordered pairs of distances and times.
e.g., Given the equation $d=65 t$ to represent the relationship between distance and time, identify $t$ as the independent variable and $d$ as the dependent variable.

## Lesson 30

Represent Relationships Between Variables-pp. 254-261

## NY-6.G

GEOMETRY
Grade 6 Content Standards
New York Progress Mathematics, Grade 6
Solve real-world and mathematical problems involving area, surface area and volume.

NY-6.G.1 Find area of triangles, trapezoids, and other polygons by composing into rectangles or decomposing into triangles and quadrilaterals. Apply these techniques in the context of solving real-world and mathematical problems.

Note: The inclusive definition of a trapezoid will be utilized, which defines a trapezoid as "A quadrilateral with at least one pair of parallel sides." (This definition includes parallelograms.)

NY-6.G. 2 Find volumes of right rectangular prisms with fractional edge lengths in the context of solving real-world and mathematical problems.

## Lesson 31

Find Areas of Parallelograms and Triangles-pp. 268-275

## Lesson 32

Find Areas of Polygons-pp. 276-283

## Lesson 33

Find Volumes of Rectangular Prisms—pp. 284291

## NY-6.G <br> GEOMETRY


#### Abstract

NY-6.G. 3 Draw polygons in the coordinate plane given coordinates for the vertices. Use coordinates to find the length of a side joining points with the same first coordinate or the same second coordinate. Apply these techniques in the context of solving real-world and mathematical problems.


NY-6.G. 4 Represent three-dimensional figures using nets made up of rectangles and triangles, and use the nets to find the surface area of these figures. Apply these techniques in the context of solving real-world and mathematical problems.

Note: Three-dimensional figures include only right rectangular prisms, right rectangular pyramids, and right triangular prisms. When finding surface areas, all necessary measurements will be given.

NY-6.G. 5 Use area and volume models to explain perfect squares and perfect cubes.

## Lesson 34

Plot and Analyze Polygons in the Coordinate Plane-pp. 292-299

## Lesson 35

Graph Solutions to Inequalities-pp. 246-253

## Related content

## Lesson 32

Find Areas of Polygons-pp. 276-283

## Lesson 33

Find Volumes of Rectangular Prisms—pp. 284291

See Grade 8

## Lesson 2

Use Rational Approximations of Irrational Numbers (perfect squares)-pp. 18-25

## Lesson 6

Evaluate Square Roots and Cube Roots (perfect cubes)-pp. 56-63

## NY-6.SP

STATISTICS AND PROBABILITY
Grade 6 Content Standards

| Develop an understanding of statistical variability. |  |
| :---: | :---: |
| NY-6.SP. 1 |  |
| NY-6.SP.1a Recognize that a statistical question is one that anticipates variability in the data related to the question and accounts for it in the answers. <br> e.g., "How old am I?" is not a statistical question, but "How old are the students in my school?" is a statistical question because one anticipates variability in students' ages. | Lesson 36 <br> Understand Statistical Questions and Describe Data-pp. 314-321 |
| NY-6.SP.1b Understand that statistics can be used to gain information about a population by examining a sample of the population; generalizations about a population from a sample are valid only if the sample is representative of that population. <br> Note: Students need to understand that data are generated with respect to particular contexts or situations and can be used to answer questions about those contexts or situations. | See Grade 7 <br> Lesson 30 <br> Understand Sampling (representative samples and populations)-pp. 266-273 |
| NY-6.SP.1c Understand that the method and sample size used to collect data for a particular question is intended to reduce the difference between a population and a sample taken from the population so valid inferences can be drawn about the population. Generate multiple samples (or simulated samples) of the same size to recognize the variation in estimates or predictions. <br> Note: Examples of acceptable methods to obtain a representative sample from a population include, but are not limited to, a simple random sample for a given population or a systematic random sample for an unknown population. Examples of unacceptable methods of sampling include, but are not limited to, online polls and convenience. | See Grade 7 <br> Lesson 30 <br> Understand Sampling (representative samples and populations)-pp. 266-273 |

## NY-6.SP

## STATISTICS AND PROBABILITY

NY-6.SP. 2 Understand that a set of quantitative data collected to answer a statistical question has a distribution which can be described by its center, spread, and overall shape.

Notes:

- Students need to determine and justify the most appropriate graph to display a given set of data (histogram, dot plot).
- Students extend their knowledge of symmetric shapes, to describe data displayed in dot plots and histograms in terms of symmetry. They identify clusters, peaks and gaps, recognizing common shapes and patterns in these displays of data distributions, and ask why a distribution takes on

NY-6.SP. 3 Recognize that a measure of center for a quantitative data set summarizes all of its values with a single number while a measure of variation describes how its values vary with a single number.

Note: Measures of center are mean, median, and mode. The measure of variation is the range.

## Lesson 36

Understand Statistical Questions and Describe
Data-pp. 314-321

## Lesson 37

Find the Median and Interquartile Range-pp. 322-329

## Summarize and describe distributions. <br> NY-6.SP. 4 Display quantitative data in plots on a number line, including dot plots and histograms.

## Lesson 36

Understand Statistical Questions and Describe Data-pp. 314-321

## Lesson 37

Find the Median and Interquartile Range-pp.
322-329
Lesson 38
Find the Mean and Mean Absolute Deviation-pp. 330-337

## Lesson 39

Display Numerical Data (dot plots, histograms, bar graphs)-pp. 338-345

## NY-6.SP

## STATISTICS AND PROBABILITY

Grade 6 Content Standards

|  | Lesson 40 <br> Summarize Numerical Data (dot plots)-pp. $346-353$ |
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| NY-6.SP. 5 Summarize quantitative data sets in relation to their context. |  |
| NY-6.SP.5a Report the number of observations. | Lesson 40 <br> Summarize Numerical Data-pp. 346-353 |
| NY-6.SP.5b Describe the nature of the attribute under investigation, including how it was measured and its units of measurement. | Lesson 40 <br> Summarize Numerical Data-pp. 346-353 |
| NY-6.SP.5c Calculate range and measures of center, as well as describe any overall pattern and any striking deviations from the overall pattern with reference to the context in which the data were gathered. <br> Note: Measures of center are mean, median, and mode. The measure of variation is the range. Role of outliers should be discussed, but no formula required. | Lesson 37 <br> Find the Median and Interquartile Range (range, measures of center)-pp. 322-329 <br> Lesson 38 <br> Find the Mean and Mean Absolute Deviation (measures of center)-pp. 330-337 <br> Lesson 39 <br> Display Numerical Data (range)—pp. 338-345 <br> Lesson 40 <br> Summarize Numerical Data (measures of center, outliers)-pp. 346-353 |
| NY-6.SP.5d Relate the range and the choice of measures of center to the shape of the data distribution and the context in which the data were gathered. <br> Note: Measures of center are mean, median, and mode. The measure of variation is the range. | Lesson 37 <br> Find the Median and Interquartile Range (measure of variation, measures of center)-pp. 322-329 <br> Lesson 38 <br> Find the Mean and Mean Absolute Deviation (measures of center)-pp. 330-337 <br> Lesson 39 <br> Display Numerical Data (range)-pp. 338-345 <br> Lesson 40 <br> Summarize Numerical Data (measures of center)-pp. 346-353 |

## NY-6.SP

STATISTICS AND PROBABILITY
Grade 6 Content Standards
New York Progress Mathematics, Grade 6

Investigate chance processes and develop, use and evaluate probability models.

NY-6.SP. 6 Understand that the probability of a chance event is a number between 0 and 1 inclusive, that expresses the likelihood of the event occurring. Larger numbers indicate greater likelihood. A probability near O indicates an unlikely event, a probability around $1 / 2$ indicates an event that is neither unlikely nor likely, and a probability near 1 indicates a likely event.

NY-6.SP. 7 Approximate the probability of a simple event by collecting data on the chance process that produces it and observing its long-run relative frequency, and predict the approximate relative frequency given the probability.
e.g., When rolling a number cube 600 times, predict that a 3 or 6 would be rolled roughly 200 times, but probably not exactly 200 times.

Note: Compound events are introduced in grade 7.
NY-6.SP. 8 Develop a probability model and use it to find probabilities of simple events. Compare probabilities from a model to observed frequencies; if the agreement is not good, explain possible sources of the discrepancy.

NY-6.SP.8a Develop a uniform probability model by assigning equal probability to all outcomes, and use the model to determine probabilities of simple events.
e.g., The probability of rolling a six-sided fair number cube and landing on a 2 is $\frac{1}{6}$. The probability of landing on an even number is $\frac{3}{6}$.

## See Grade 7

## Lesson 36

Develop a Uniform Probability Model—pp. 314-321

## NY-6.SP <br> STATISTICS AND PROBABILITY

Grade 6 Content Standards

NY-6.SP.8b Develop a probability model
(which may not be uniform) by observing frequencies in data generated from a chance process.
e.g., Find the approximate probability that a spinning penny will land heads up or that a tossed paper cup will land open-end down. Do the outcomes for the spinning penny appear to be equally likely based on the observed frequencies?

See Grade 7
Lesson 37
Use a Chance Process to Develop a Probability Model-pp. 322-329

