## Progress <br> Mathematics

Standards-Based Instruction \& Practice


Aligned to the

## Colorado

Academic Standards for Mathematics

## Fourth Grade

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| Standard: 1. Number Sense, Properties, and Operations <br> Prepared Graduates: <br> Understand the structure and properties of our number system. At their most basic level numbers are abstract symbols that represent real-world quantities |  |  |
| :---: | :---: | :---: |
| Concepts and skills students master: |  |  |
| 1. The decimal number system to the hundredths place describes place value patterns and relationships that are repeated in large and small numbers and forms the foundation for efficient algorithms |  |  |
| Fourth Grade Evidence Outcomes | Sadlier Pr | ress Mathematics, Grade 4 |
| Students can: |  |  |
| a. Generalize place value understanding for multi-digit whole numbers (CCSS: 4.NBT) |  |  |
| i. Explain that in a multi-digit whole number, a digit in one place represents ten times what it represents in the place to its right. (CCSS: 4.NBT.1) | Lesson 6 | Understand Place Value of Whole Numberspp. 56-63 |
| ii. Read and write multi-digit whole numbers using base-ten numerals, number names, and expanded form. (CCSS: 4.NBT.2) | Lesson 7 | Read, Write, and Compare Whole Numberspp. 64-71 |
| iii. Compare two multi-digit numbers based on meanings of the digits in each place, using $>,=$, and < symbols to record the results of comparisons. (CCSS: 4.NBT.2) | Lesson 7 | Read, Write, and Compare Whole Numberspp. 64-71 |
| iv. Use place value understanding to round multi-digit whole numbers to any place. (CCSS: 4.NBT.3) | Lesson 8 | Apply Place Value to Round Whole Numbers-pp. 72-79 |
| b. Use decimal notation to express fractions, and compare decimal fractions (CCSS: 4.NF) |  |  |
| i. Express a fraction with denominator 10 as an equivalent fraction with denominator 100, and use this technique to add two fractions with respective denominators 10 and 100. (CCSS: 4.NF.5) | Lesson 24 | Add Fractions: Denominators of 10 and 100—pp. 206-213 |
| ii. Use decimal notation for fractions with denominators 10 or 100. (CCSS: 4.NF.6) | Lesson 25 | Write and Compare Decimal Fractions-pp. 214-221 |
| iii. Compare two decimals to hundredths by reasoning about their size. (CCSS: 4.NF.7) | Lesson 25 | Write and Compare Decimal Fractions-pp. 214-221 |

## Standard: 1. Number Sense, Properties, and Operations

Prepared Graduates:
> Understand that equivalence is a foundation of mathematics represented in numbers, shapes, measures, expressions, and equations

## Concepts and skills students master:

2. Different models and representations can be used to compare fractional parts

## Fourth Grade Evidence Outcomes

Students can:
a. Use ideas of fraction equivalence and ordering to: (CCSS:
4.NF)
i. Explain equivalence of fractions using drawings and models
ii. Use the principle of fraction equivalence to recognize and generate equivalent fractions. (CCSS: 4.NF.1)
iii. Compare two fractions with different numerators and different denominators, and justify the conclusions. (CCSS: 4.NF.2)
b. Build fractions from unit fractions by applying understandings of operations on whole numbers. (CCSS: 4.NF)
i. Apply previous understandings of addition and subtraction to add and subtract fractions.

1. Compose and decompose fractions as sums and differences of fractions with the same denominator in more than one way and justify with visual models.
2. Add and subtract mixed numbers with like denominators. (CCSS: 4.NF.3c)
3. Solve word problems involving addition and subtraction of fractions referring to the same whole and having like denominators. (CCSS: 4.NF.3d)
ii. Apply and extend previous understandings of multiplication to multiply a fraction by a whole number. (CCSS: 4.NF.4)
4. Express a fraction $a / b$ as a multiple of $1 / b$. (CCSS: 4.NF.4a)

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Lesson 21 Multiply Unit Fractions by Whole Numberspp. 182-189

## Fourth Grade Evidence Outcomes

2. Use a visual fraction model to express $\mathrm{a} / \mathrm{b}$ as a multiple of $1 / b$, and apply to multiplication of whole number by a fraction. (CCSS: 4.NF.4b)
3. Solve word problems involving multiplication of a fraction by a whole number. (CCSS: 4.NF.4c)

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## Lesson 22 Multiply Fractions by Whole Numbers-pp.

 190-197Lesson 23 Problem Solving: Multiply Fractions by Whole Numbers—pp. 198-205

## Standard: 1. Number Sense, Properties, and Operations

Prepared Graduates:
> Are fluent with basic numerical and symbolic facts and algorithms, and are able to select and use appropriate (mental math, paper and pencil, and technology) methods based on an understanding of their efficiency, precision, and transparency

Concepts and skills students master:
3. Formulate, represent, and use algorithms to compute with flexibility, accuracy, and efficiency

## Fourth Grade Evidence Outcomes

## Students can:

a. Use place value understanding and properties of operations to perform multi-digit arithmetic. (CCSS: 4.NBT)
i. Fluently add and subtract multi-digit whole numbers using standard algorithms. (CCSS: 4.NBT.4)
ii. Multiply a whole number of up to four digits by a one-digit whole number, and multiply two twodigit numbers, using strategies based on place value and the properties of operations. (CCSS: 4.NBT.5)
iii. Find whole-number quotients and remainders with up to four-digit dividends and one-digit divisors, using strategies based on place value, the properties of operations, and/or the relationship between multiplication and division. (CCSS: 4.NBT.6)
iv. Illustrate and explain multiplication and division calculation by using equations, rectangular arrays, and/or area models. (CCSS: 4.NBT.6)

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## Fourth Grade Evidence Outcomes

b. Use the four operations with whole numbers to solve problems. (CCSS: 4.OA)
i. Interpret a multiplication equation as a comparison. (CCSS: 4.OA.1)
ii. Represent verbal statements of multiplicative comparisons as multiplication equations. (CCSS: 4.OA.1)
iii. Multiply or divide to solve word problems involving multiplicative comparison. (CCSS: 4.OA.2)
iv. Solve multistep word problems posed with whole numbers and having whole-number answers using the four operations, including problems in which remainders must be interpreted. (CCSS: 4.OA.3)
v. Represent multistep word problems with equations using a variable to represent the unknown quantity. (CCSS: 4.OA.3)
vi. Assess the reasonableness of answers using mental computation and estimation strategies including rounding. (CCSS: 4.OA.3)
vii. Using the four operations analyze the relationship between choice and opportunity cost (PFL)

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| Lesson 1 | Interpret Multiplication Equations as <br> Comparisons-pp. 10-17 |
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## Lesson 3 Problem Solving: Multistep Problems—pp. 26-33

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Lesson 3 Problem Solving: Multistep Problems—pp. 26-33

## Standard: 2. Patterns, Functions, and Algebraic Structures <br> Prepared Graduates:

> Make sound predictions and generalizations based on patterns and relationships that arise from numbers, shapes, symbols, and data
> Make claims about relationships among numbers, shapes, symbols, and data and defend those claims by relying on the properties that are the structure of mathematics

## Concepts and skills students master:

1. Number patterns and relationships can be represented by symbols

## Fourth Grade Evidence Outcomes

Students can:
a. Generate and analyze patterns and identify apparent features of the pattern that were not explicit in the rule itself. (CCSS: 4.OA.5)
i. Use number relationships to find the missing number in a sequence
ii. Use a symbol to represent and find an unknown quantity in a problem situation

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## Lesson $5 \quad$ Generate and Analyze Number and Shape Patterns-pp. 42-49

Lesson 5 Generate and Analyze Number and Shape Patterns-pp. 42-49

| Sadlier Progress Mathematics, Grade 4, Aligned to ther Colorado Academic Standards in Mathematics Grade Level Expectation: Fourth Grade |  |  |
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| Fourth Grade Evidence Outcomes | Sadlier Progress Mathematics, Grade 4 |  |
| iii. Complete input/output tables | Lesson 5 | Generate and Analyze Number and Shape Patterns-pp. 42-49 |
| iv. Find the unknown in simple equations | Lesson 5 | Generate and Analyze Number and Shape Patterns-pp. 42-49 |
| b. Apply concepts of squares, primes, composites, factors, and multiples to solve problems |  |  |
| i. Find all factor pairs for a whole number in the range 1-100. (CCSS: 4.OA.4) | Lesson 4 | Find Factors and Multiples for Whole Numbers-pp. 34-41 |
| ii. Recognize that a whole number is a multiple of each of its factors. (CCSS: 4.OA.4) | Lesson 4 | Find Factors and Multiples for Whole Numbers-pp. 34-41 |
| iii. Determine whether a given whole number in the range $1-100$ is a multiple of a given one-digit number. (CCSS: 4.OA.4) | Lesson 4 | Find Factors and Multiples for Whole Numbers-pp. 34-41 |
| iv. Determine whether a given whole number in the range 1-100 is prime or composite. (CCSS: 4.OA.4) | Lesson 4 | Find Factors and Multiples for Whole Numbers-pp. 34-41 |
| Standard: 3. Data Analysis, Statistics, and Probability <br> Prepared Graduates: <br> Solve problems and make decisions that depend on understanding, explaining, and quantifying the variability in data |  |  |
| Fourth Grade Evidence Outcomes | Sadlier Progress Mathematics, Grade 4 |  |
| Students can: |  |  |
| a. Make a line plot to display a data set of measurements in fractions of a unit (1/2, 1/4, 1/8). (CCSS: 4.MD.4) | Lesson 30 | Problem Solving: Use Line Plots-pp. 266-273 |
| b. Solve problems involving addition and subtraction of fractions by using information presented in line plots. (CCSS: 4.MD.4) | Lesson 30 | Problem Solving: Use Line Plots-pp. 266-273 |

## Standard: 4. Shape, Dimension, and Geometric Relationships <br> \section*{Prepared Graduates:}

> Understand quantity through estimation, precision, order of magnitude, and comparison. The reasonableness of answers relies on the ability to judge appropriateness, compare, estimate, and analyze error

## Concepts and skills students master:

1. Appropriate measurement tools, units, and systems are used to measure different attributes of objects and time

## Fourth Grade Evidence Outcomes

Students can:
a. Solve problems involving measurement and conversion of measurements from a larger unit to a smaller unit. (CCSS: 4.MD)
i. Know relative sizes of measurement units within one system of units including km, m, cm; kg, g; lb, oz.; l, ml; hr, min, sec. (CCSS: 4.MD.1)
ii. Within a single system of measurement, express measurements in a larger unit in terms of a smaller unit. Record measurement equivalents in a twocolumn table. (CCSS: 4.MD.1)
iii. Use the four operations to solve word problems involving distances, intervals of time, liquid volumes, masses of objects, and money, including problems involving simple fractions or decimals, and problems that require expressing measurements given in a larger unit in terms of a smaller unit. (CCSS: 4.MD.2)
iv. Represent measurement quantities using diagrams such as number line diagrams that feature a measurement scale. (CCSS: 4.MD.2)
v. Apply the area and perimeter formulas for rectangles in real world and mathematical problems. (CCSS: 4.MD.3)
b. Use concepts of angle and measure angles. (CCSS: 4.MD)
i. Describe angles as geometric shapes that are formed wherever two rays share a common endpoint, and explain concepts of angle measurement. (CCSS: 4.MD.5)
ii. Measure angles in whole-number degrees using a protractor. Sketch angles of specified measure. (CCSS: 4.MD.6)

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| Lesson 26 | Convert Customary Measurement Units—pp. <br> $234-241$ |
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| Lesson 26 | Convert Customary Measurement Units—pp. <br> $234-241$ |
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Lesson 28 Problem Solving: Measurement—pp. 250-257

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| Sadlier Progress Mathematics, Grade 4, Aligned to the <br> Colorado Academic Standards in Mathematics <br> Grade Level Expectation: Fourth Grade |
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| Fourth Grade Evidence Outcomes |
| iii.Demonstrate that angle measure as additive. <br> (CCSS: 4.MD.7) Lesson 33 Problem Solving: Find Unknown Angle <br> Measures-pp. 290-297 <br> iv.Solve addition and subtraction problems to find <br> unknown angles on a diagram in real world and <br> mathematical problems. (CCSS: 4.MD.7)  Lesson 33Problem Solving: Find Unknown Angle <br> Measures-pp. 290-297 |

## Standard: 4. Shape, Dimension, and Geometric Relationships Prepared Graduates:

> Make claims about relationships among numbers, shapes, symbols, and data and defend those claims by relying on the properties that are the structure of mathematics

## Concepts and skills students master:

2. Geometric figures in the plane and in space are described and analyzed by their attributes

| Fourth Grade Evidence Outcomes |
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| Students can: |
| a. Draw points, lines, line segments, rays, angles (right, acute, <br> obtuse), and perpendicular and parallel lines. (CCSS: 4.G.1) |
| b. Identify points, line segments, angles, and perpendicular <br> and parallel lines in two-dimensional figures. (CCSS: 4.G.1) |
| c. Classify and identify two-dimensional figures according to <br> attributes of line relationships or angle size.6 (CCSS: 4.G.2) |
| d. Identify a line of symmetry for a two-dimensional figure.7 <br> (CCSS: 4.G.3) |

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| Lesson 34 | Draw and Identify Points, Lines, and <br> Angles-pp. 304-311 |
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| Lesson 34 | Draw and Identify Points, Lines, and <br> Angles—pp. 304-311 |
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