## Progress <br> Mathematics

Standards-Based Instruction \& Practice


Aligned to the

# Georgia Standards of Excellence 2015-2016: Mathematics 

## Grade 7

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## Ratios and Proportional Relationships

## Standards

Analyze proportional relationships and use them to solve real-world and mathematical problems.

| MGSE7.RP. 1 | Compute unit rates associated with ratios of fractions, including ratios of lengths, areas and other quantities measured in like or different units. For example, if a person walks $1 / 2$ mile in each $1 / 4$ hour, compute the unit rate as the complex fraction(1/2)/(1/4) miles per hour, equivalently 2 miles per hour. |
| :---: | :---: |
| MGSE7.RP. 2 | Recognize and represent proportional relationships between quantities. |
|  | MGSET.RP.2a Decide whether two quantities are in a proportional relationship, e.g., by testing for equivalent ratios in a table or graphing on a coordinate plane and observing whether the graph is a straight line through the origin. |
|  | MGSE7.RP.2b Identify the constant of proportionality (unit rate) in tables, graphs, equations, diagrams, and verbal descriptions of proportional relationships. |
|  | MGSET.RP.2c Represent proportional relationships by equations. For example, if total cost $t$ is proportional to the number $n$ of items purchased at a constant price $p$, the relationship between the total cost and the number of items can be expressed as $\mathrm{t}=\mathrm{pn}$. |
|  | MGSE7.RP.2d Explain what a point $(x$, ) on the graph of a proportional relationship means in terms of the situation, with special attention to the points $(0,0)$ and $(1, r)$ where $r$ is the unit rate. |
| MGSE7.RP. 3 | Use proportional relationships to solve multistep ratio and percent problems. Examples: simple interest, tax, markups and markdowns, gratuities and commissions, and fees. |

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## The Number System

Standards
Apply and extend previous understandings of
operations with fractions to add, subtract,
multiply, and divide rational numbers.
MGSET.NS. 1 Apply and extend previous understandings of addition and subtraction to add and subtract rational numbers; represent addition and subtraction on a horizontal or vertical number line diagram.

MGSET.NS. 1 a Show that a number and its opposite have a sum of 0 (are additive inverses). Describe situations in which opposite quantities combine to make 0 . For example, your bank account balance is $\$ 25.00$. You deposit $\$ 25.00$ into your account. The net balance is $\$ 0.00$.

MGSE7.NS.1b Understand $p+q$ as the number located a distance $|q|$ from $p$, in the positive or negative direction depending on whether $q$ is positive or negative. Interpret sums of rational numbers by describing real world contexts.

MGSE7.NS.1c Understand subtraction of rational numbers as adding the additive inverse, $p-q=p+(-q)$. Show that the distance between two rational numbers on the number line is the absolute value of their difference, and apply this principle in real-world contexts.

MGSE7.NS.1d Apply properties of operations as strategies to add and subtract rational numbers.

MGSE7.NS. 2 Apply and extend previous understandings of multiplication and division and of fractions to multiply and divide rational numbers.

MGSE7.NS.2a Understand that multiplication is extended from fractions to rational numbers by requiring that operations continue to satisfy the properties of operations, particularly the distributive property, leading to products such as $(-1)(-1)=1$ and the rules for multiplying signed numbers. Interpret products of rational numbers by describing real-world contexts.

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## Lesson $8 \quad$ Understand Addition of Integers—pp. 72-79

Lesson 9 Understand Subtraction of Integers—pp. 80-87

Lesson 10 Add and Subtract Rational Numbers-pp. 88-95

Lesson 11 Understand Multiplication of Integers-pp. 96-103

## The Number System

Standards

MGSE7.NS.2b Understand that integers can be divided, provided that the divisor is not zero, and every quotient of integers (with non-zero divisor) is a rational number. If $p$ and $q$ are integers, then $(p / q)=(-p) / q=p /(-q)$. Interpret quotients of rational numbers by describing realworld contexts.

MGSE7.NS.2c Apply properties of operations as strategies to multiply and divide rational numbers.

MGSE7.NS.2d Convert a rational number to a decimal using long division; know that the decimal form of a rational number terminates in Os or eventually repeats.

## MGSE7.NS. 3 Solve real-world and mathematical problems

 involving the four operations with rational numbers. (Computations with rational numbers extend the rules for manipulating fractions to complex fractions.)
## Expressions and Equations

## Standards

Use properties of operations to generate equivalent expressions.

| MGSE7.EE. 1 | Apply properties of operations as strategies <br> to add, subtract, factor, and expand linear <br> expressions with rational coefficients. |
| :--- | :--- |
| MGSE7.EE. 2 | Understand that rewriting an expression in <br> different forms in a problem context can <br> clarify the problem and how the quantities in <br> it are related. For example, $a+0.05 a=1.05 a$ <br> means that adding a $5 \%$ tax to $a$ total is the <br> same as multiplying the total by 1.05. |

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| Lesson 17 | Expand and Factor Linear Expressions-pp. <br> $150-157$ |

## Expressions and Equations

## Standards

## Solve real-life and mathematical problems using numerical and algebraic expressions and equations.

| MGSE7.EE. 3 | Solve multistep real-life and mathematical problems posed with positive and negative rational numbers in any form (whole numbers, fractions, and decimals) by applying properties of operations as strategies to calculate with numbers, converting between forms as appropriate, and assessing the reasonableness of answers using mental computation and estimation strategies. <br> For example: <br> - If a woman making \$25 an hour gets a 10\% raise, she will make an additional 1/10 of her salary an hour, or $\$ 2.50$, for a new salary of $\$ 27.50$. <br> - Ifyou want to place a towel bar 93/4 inches long in the center of a door that is 27 $1 / 2$ inches wide, you will need to place the bar about 9 inches from each edge; this estimate can be used as a check on the exact computation. |
| :---: | :---: |
| MGSE7.EE. 4 | Apply and extend previous understandings of multiplication and division and of fractions to multiply and divide rational numbers. |
|  | MGSE7.EE.4a Solve word problems leading to equations of the form $p x+q=r$ and $p(x+q)=r$, where $p, q$, and $r$ are specific rational numbers. Solve equations of these forms fluently. Compare an algebraic solution to an arithmetic solution, identifying the sequence of the operations used in each approach. For example, the perimeter of a rectangle is 54 cm . Its length is 6 cm . What is its width? |
|  | MGSE7.EE.4b Solve word problems leading to inequalities of the form $p x+q$ $>r$ or $p x+q<r$, where $p, q$, and $r$ are specific rational numbers. Graph the solution set of the inequality and interpret it in the context of the problem. For example: As a salesperson, you are paid $\$ 50$ per week plus $\$ 3$ per sale. This week you want your pay to be at least $\$ 100$. Write an inequality for the number of sales you need to make, and describe the solutions. |

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## Expressions and Equations

## Standards

MGSE7.EE.4c Solve real-world and mathematical problems by writing and solving equations of the form $x+p=q$ and $p x=q$ in which $p$ and $q$ are rational numbers.

## Geometry

Standards
Draw, construct, and describe geometrical figures and describe the relationships between them.

| MGSE7.G.1 | Solve problems involving scale drawings of <br> geometric figures, including computing <br> actual lengths and areas from a scale drawing <br> and reproducing a scale drawing at a different <br> scale. |
| :--- | :--- |
| MGSE7.G.2 | Explore various geometric shapes with given <br> conditions. Focus on creating triangles from <br> three measures of angles and/or sides, <br> noticing when the conditions determine a <br> unique triangle, more than one triangle, or no <br> triangle. |
| MGSE7.G.3 | Describe the two-dimensional figures (cross <br> sections) that result from slicing three- <br> dimensional figures, as in plane sections of <br> right rectangular prisms, right rectangular <br> pyramids, cones, cylinders, and spheres. |

Solve real-life and mathematical problems involving angle measure, area, surface area, and volume.

| MGSE7.G.4 | Given the formulas for the area and <br> circumference of a circle, use them to solve <br> problems; give an informal derivation of the <br> relationship between the circumference and <br> area of a circle. |
| :--- | :--- |
| MGSE7.G.5 | Use facts about supplementary, <br> complementary, vertical, and adjacent angles <br> in a multi-step problem to write and solve <br> simple equations for an unknown angle in a <br> figure. |

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| :--- |
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| :--- |
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## Geometry

## Statistics and Probability

## Standards <br> Use random sampling to draw inferences about a population.

| MGSE7.SP. 1 | Understand that statistics can be used to gain <br> information about a population by examining <br> a sample of the population; generalizations <br> about a population from a sample are valid <br> only if the sample is representative of that <br> population. Understand that random <br> sampling tends to produce representative <br> samples and support valid inferences. |
| :--- | :--- |
| MGSE7.SP.2 | Use data from a random sample to draw <br> inferences about a population with an <br> unknown characteristic of interest. Generate <br> multiple samples (or simulated samples) of <br> the same size to gauge the variation in <br> estimates or predictions. For example, <br> estimate the mean word length in a book by <br> randomly sampling words from the book; <br> predict the winner of a school election based on <br> randomly sampled survey data. Gauge how far <br> off the estimate or prediction might be. |
| Draw informal comparative inferences about |  |
| twO populations. |  |

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Lesson 32 Use Visual Overlap to Compare
Distributions-pp. 282-289

Lesson 33 Use Sample Statistics to Compare
Populations-pp. 290-297

## Statistics and Probability

## Standards

Investigate chance processes and develop, use, and evaluate probability models.

| MGSE7.SP.5 | Understand that the probability of a chance <br> event is a number between 0 and 1 that <br> expresses the likelihood of the event <br> occurring. Larger numbers indicate greater <br> likelihood. A probability near 0 indicates an <br> unlikely event, a probability around 1/2 <br> indicates an event that is neither unlikely nor <br> likely, and a probability near 1 indicates a <br> likely event. |
| :--- | :--- |
| MGSE7.SP.6 | Approximate the probability of a chance <br> event by collecting data on the chance <br> process that produces it and observing its <br> long-run relative frequency. Predict the <br> approximate relative frequency given the <br> probability. For example, when rolling a <br> number cube 600 times, predict that a 3 or 6 <br> would be rolled roughly 200 times, but probably <br> not exactly 200 times. |
| MGSE7.SP.7Develop a probability model and use it to find <br> probabilities of events. Compare <br> experimental and theoretical probabilities of <br> events. If the probabilities are not close, <br> explain possible sources of the discrepancy. |  |
| MGSE7.SP.7a Develop a uniform <br> probability model by assigning equal <br> probability to all outcomes, and use the <br> model to determine probabilities of <br> events. For example, if a student is selected <br> at random from a class, find the probability <br> that Jane will be selected and the <br> probability that a girl will be selected. |  |
|  | MGSE7.SP.7b Develop a probability <br> model (which may not be uniform) by <br> observing frequencies in data generated <br> from a chance process. For example, find <br> the approximate probability that a spinning <br> penny will land heads up or that a tossed <br> paper cup will land open-end down. Do the <br> outcomes for the spinning penny appear to <br> be equally likely based on the observed <br> frequencies? |

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Lesson 36 Develop a Uniform Probability Model—pp. 314-321

Lesson 37 Use a Chance Process to Develop a Probability Model—pp. 322-329

## Statistics and Probability

## Standards

MGSE7.SP. 8 Find probabilities of compound events using organized lists, tables, tree diagrams, and simulation.

MGSE7.SP.8a Understand that, just as with simple events, the probability of a compound event is the fraction of outcomes in the sample space for which the compound event occurs.

MGSE7.SP.8b Represent sample spaces for compound events using methods such as organized lists, tables and tree diagrams. For an event described in everyday language (e.g., "rolling double sixes"), identify the outcomes in the sample space which compose the event.

MGSE7.SP.8c Explain ways to set up a simulation and use the simulation to generate frequencies for compound events. For example, if $40 \%$ of donors have type A blood, create a simulation to predict the probability that it will take at least 4 donors to find one with type A blood.

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