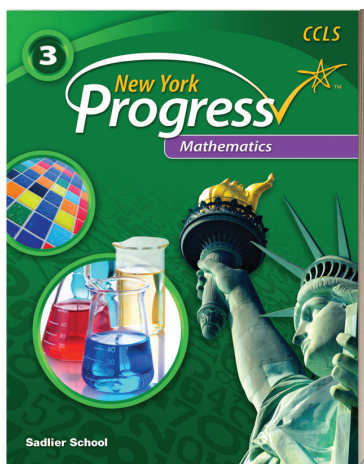


SADLIER

New York Progress Mathematics

Standards-Based Instruction & Practice



Aligned to the

New York State Learning Standards for Mathematics

(Revised 2017)

Grade 3

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Grade 3

Operations & Algebraic Thinking

GRADE 3 NYS LEARNING STANDARDS FOR MATHEMATICS

A. Represent and solve problems involving multiplication and division

3.OA.A.1

1. Interpret products of whole numbers.

ADDITIONAL CLARIFICATION/EXAMPLES

e.g., interpret 5×7 as the total number of objects in 5 groups of 7 objects each. Describe a context in which a total number of objects can be expressed as 5×7 .

3.OA.A.2

2. Interpret whole-number quotients of whole numbers.

ADDITIONAL CLARIFICATION/EXAMPLES

e.g., interpret $56 \div 8$ as the number of objects in each share when 56 objects are partitioned equally into 8 shares, or as a number of shares when 56 objects are partitioned into equal shares of 8 objects each. Describe a context in which a number of shares or a number of groups can be expressed as $56 \div 8$.

3.OA.A.3

3. Use multiplication and division within 100 to solve word problems in situations involving equal groups, arrays, and measurement quantities.

ADDITIONAL CLARIFICATION/EXAMPLES

e.g., using drawings and equations with a symbol for the unknown number to represent the problem.

	Unknown Product $a \times b = ?$	Group Size Unknown ("How many in each group?" Division) $a \div ? = p$ and $p \times a = ?$	Number of Groups Unknown ("How many groups?" Division) $? \times b = p$ and $p \div b = ?$
Equal Groups	There are a bags with b plums in each bag. How many plums are there in all? <i>Measurement example:</i> You need a lengths of string, each b inches long. How much string will you need altogether?	If p plums are shared equally into a bags, then how many plums will be in each bag? <i>Measurement example:</i> You have p inches of string, which you will cut into a equal pieces. How long will each piece of string be?	If p plums are to be packed b to a bag, then how many bags are needed? <i>Measurement example:</i> You have p inches of string, which you will cut into pieces that are b inches long. How many pieces of string will you have?
Arrays & Area	There are a rows of apples with b apples in each row. How many apples are there? <i>Area example:</i> What is the area of an a cm by b cm rectangle?	If p apples are arranged into equal rows, how many apples will be in each row? <i>Area example:</i> A rectangle has area p square centimeters. If it is a cm long, what is its width?	If p apples are arranged into equal rows of b apples, how many rows will there be? <i>Area example:</i> A rectangle has area p square centimeters. If it is b cm wide, what is its length?

Array problems can also be stated in terms of columns, exchanging the order of a and b , so that the same array is described. For example: There are b columns of apples with a apples in each column. How many apples are there?

3.OA.A.4

4. Determine the unknown whole number in a multiplication or division equation relating three whole numbers.

ADDITIONAL CLARIFICATION/EXAMPLES

e.g., determine the unknown number that makes the equation true in each of the equations $8 \times ? = 48$, $5 = \underline{\quad} \div 3$, $6 \times 6 = ?$.

SADLIER NEW YORK PROGRESS MATHEMATICS, GRADE 3

Lesson 1 Interpret Products of Whole Numbers—pp. 10–17

Lesson 2 Interpret Quotients of Whole Numbers—pp. 18–26

Lesson 3 Problem Solving: Multiplication/Division and Equal Groups—pp. 26–33

Lesson 4 Problem Solving: Multiplication/Division and Arrays—pp. 34–41

Lesson 32 Problem Solving: Measurement—pp. 288–295

Lesson 5 Find Unknown Numbers in Multiplication and Division Equations—pp. 42–49



Grade 3

Operations & Algebraic Thinking

GRADE 3 NYS LEARNING STANDARDS FOR MATHEMATICS

B. Understand properties of multiplication and the relationship between multiplication and division.

3.OA.B.5

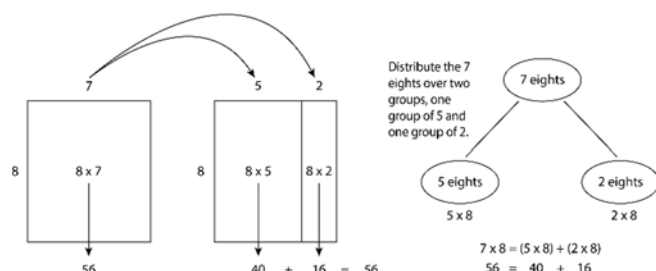
5. Apply properties of operations as strategies to multiply and divide.

ADDITIONAL CLARIFICATION/EXAMPLES

e.g.,

- If $6 \times 4 = 24$ is known, then $4 \times 6 = 24$ is also known. (Commutative property of multiplication.)
- $3 \times 5 \times 2$ can be found by $3 \times 5 = 15$, then $15 \times 2 = 30$, or by $5 \times 2 = 10$, then $3 \times 10 = 30$. (Associative property of multiplication.)
- Knowing that $8 \times 5 = 40$ and $8 \times 2 = 16$, one can find 8×7 as $8 \times (5 + 2) = (8 \times 5) + (8 \times 2) = 40 + 16 = 56$. (Distributive property.)

Note: A variety of representations can be used when applying the properties of operations, which may or may not include parentheses. The area model (3.MD.7c) is a multiplication/division strategy that applies the distributive property (3.OA.5), e.g.,



3.OA.B.6

6. Understand division as an unknown-factor problem.

ADDITIONAL CLARIFICATION/EXAMPLES

e.g., find $32 \div 8$ by finding the number that makes 32 when multiplied by 8.

C. Multiply and divide within 100.

3.OA.C.7

3.OA.C.7a

7a. Fluently solve single-digit multiplication and related divisions, using strategies such as the relationship between multiplication and division or properties of operations.

ADDITIONAL CLARIFICATION/EXAMPLES

e.g., knowing that $8 \times 5 = 40$, one knows $40 \div 5 = 8$

Note: Fluency involves a mixture of just knowing some answers, knowing some answers from patterns, and knowing some answers from the use of strategies.

SADLIER NEW YORK PROGRESS MATHEMATICS, GRADE 3

Lesson 6 Apply Commutative and Associative Properties to Multiply—pp. 50–57

Lesson 7 Apply the Distributive Property to Multiply—pp. 58–65

Lesson 8 Divide by Finding an Unknown Factor—pp. 66–73

Lesson 9 Multiply and Divide Fluently within 100—pp. 80–87



Grade 3

Operations & Algebraic Thinking

GRADE 3 NYS LEARNING STANDARDS FOR MATHEMATICS

3.OA.C.7b

- 7b. Know from memory all products of two one-digit numbers.

D. Solve problems involving the four operations, and identify and extend patterns in arithmetic.

3.OA.D.8

8. Solve two-step word problems posed with whole numbers and having whole-number answers using the four operations.

ADDITIONAL CLARIFICATION/EXAMPLES

Note: Two-step problems need not be represented by a single expression or equation.

3.OA.D.8a

- 8a. Represent these problems using equations or expressions with a letter standing for the unknown quantity.

3.OA.D.8b

- 8b. Assess the reasonableness of answers using mental computation and estimation strategies including rounding.

3.OA.D.9

9. Identify and extend arithmetic patterns (including patterns in the addition table or multiplication table).

SADLIER NEW YORK PROGRESS MATHEMATICS, GRADE 3

Lesson 9 Multiply and Divide Fluently within 100—pp. 80–87

Lesson 10 Problem Solving: Two-Step Problems—pp. 88–95

Lesson 11 Problem Solving: Use Equations—pp. 96–103

Lesson 10 Problem Solving: Two-Step Problems (check that an answer is reasonable, estimation)—pp. 88–95

Lesson 11 Problem Solving: Use Equations (check that an answer is reasonable)—pp. 96–103

Lesson 12 Identify and Explain Arithmetic Patterns—pp. 104–111

Number & Operations in Base Ten

GRADE 3 NYS LEARNING STANDARDS FOR MATHEMATICS

A. Use place value understanding and properties of operations to perform multi-digit arithmetic.

3.NBT.A.1

1. Use place value understanding to round whole numbers to the nearest 10 or 100.

3.NBT.A.2

2. Fluently add and subtract within 1,000 using strategies and algorithms based on place value, properties of operations, and/or the relationship between addition and subtraction.

ADDITIONAL CLARIFICATION/EXAMPLES

Note: A range of algorithms may be used.

SADLIER NEW YORK PROGRESS MATHEMATICS, GRADE 3

Lesson 13 Round Whole Numbers to the Nearest 10 or 100—pp. 112–119

Lesson 14 Add and Subtract Fluently within 1000—pp. 120–127



Grade 3

Number & Operations in Base Ten

GRADE 3 NYS LEARNING STANDARDS FOR MATHEMATICS

3.NBT.A.3

3. Multiply one-digit whole numbers by multiples of 10 in the range 10–90 using strategies based on place value and properties of operations.

ADDITIONAL CLARIFICATION/EXAMPLES

e.g., 9×80 , 5×60

3.NBT.A.4

3.NBT.A.4a

- 4a. Understand that the four digits of a four-digit number represent amounts of thousands, hundreds, tens and ones.

ADDITIONAL CLARIFICATION/EXAMPLES

e.g., 3,245 equals 3 thousands, 2 hundreds, 4 tens, and 5 ones.

3.NBT.A.4b

- 4b. Read and write four digit numbers using base-ten numerals, number names and expanded form.

ADDITIONAL CLARIFICATION/EXAMPLES

e.g., the number 3,245 in expanded form can be written as $3,245 = 3,000 + 200 + 40 + 5$.

SADLIER NEW YORK PROGRESS MATHEMATICS, GRADE 3

Lesson 15 Multiply One-Digit Whole Numbers by Multiples of 10—pp. 128–135

Related content—

Foundational Skills Handbook: C. Understand: Models can show that 10 tens is the same as 1 hundred— p. 338

*See also—

Grade 2 Lesson 8 Read and Write Numbers to 1,000—pp. 72–79

Grade 4 Lesson 6 Understand Place Value of Whole Numbers—pp. 56–63

Lesson 14 Add and Subtract Fluently within 1000 (expanded form)—pp. 120–127

*See also—

Grade 2 Lesson 6 Place Value: Hundreds, Tens, and Ones (expanded form)—pp. 56–6

Grade 2 Lesson 8 Read and Write Numbers to 1,000 (number, number name, expanded form)—pp. 72–79

Grade 4 Lesson 7 Read, Write, and Compare Whole Numbers—pp. 64–71

Number & Operations—Fractions

GRADE 3 NYS LEARNING STANDARDS FOR MATHEMATICS

A. Develop understanding of fractions as numbers.

3.NF.A.1

1. Understand a unit fraction, $\frac{1}{b}$, is the quantity formed by 1 part when a whole is partitioned into b equal parts.

Understand a fraction $\frac{a}{b}$ is the quantity formed by a parts of size $\frac{1}{b}$.

ADDITIONAL CLARIFICATION/EXAMPLES

Note: Fractions are limited to those with denominators 2, 3, 4, 6, and 8.

SADLIER NEW YORK PROGRESS MATHEMATICS, GRADE 3

Lesson 16 Understand Unit Fractions as Quantities—pp. 142–149

Lesson 17 Understand Fractions as Quantities—pp. 150–157



Grade 3

Number & Operations—Fractions

GRADE 3 NYS LEARNING STANDARDS FOR MATHEMATICS

3.NF.A.2

2. Understand a fraction as a number on the number line; represent fractions on a number line diagram.

ADDITIONAL CLARIFICATION/EXAMPLES

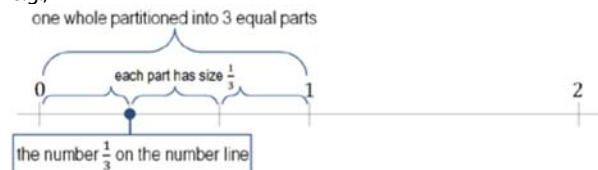
Note: Fractions are limited to those with denominators 2, 3, 4, 6, and 8.

3.NF.A.2a

- 2a. Represent a fraction $\frac{1}{b}$ on a number line diagram by defining the interval from 0 to 1 as the whole and partitioning it into b equal parts. Recognize that each part has size $\frac{1}{b}$ and that the endpoint of the part based at 0 locates the number $\frac{1}{b}$ on the number line.

ADDITIONAL CLARIFICATION/EXAMPLES

e.g.,



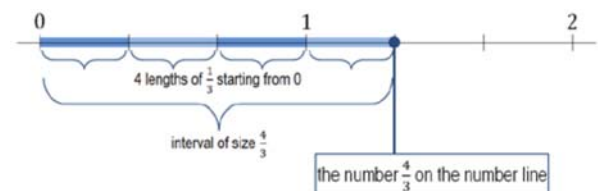
Note: Fractions are limited to those with denominators 2, 3, 4, 6, and 8.

3.NBT.A.2b

- 2b. Represent a fraction $\frac{a}{b}$ on a number line diagram by marking off a lengths $\frac{1}{b}$ from 0. Recognize that the resulting interval has size $\frac{a}{b}$ and that its endpoint locates the number $\frac{a}{b}$ on the number line.

ADDITIONAL CLARIFICATION/EXAMPLES

e.g.,



Note: Fractions are limited to those with denominators 2, 3, 4, 6, and 8.

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Lesson 18 Understand Fractions on the Number Line—
pp. 158–165

Lesson 18 Understand Fractions on the Number Line—
pp. 158–165



Grade 3

Number & Operations—Fractions

GRADE 3 NYS LEARNING STANDARDS FOR MATHEMATICS

3.NF.A.3

3. Explain equivalence of fractions in special cases, and compare fractions by reasoning about their size.

ADDITIONAL CLARIFICATION/EXAMPLES

Note: Grade 4 expectations are limited to fractions with denominators 2, 3, 4, 5, 6, 8, 10, 12, and 100.

3.NF.B.3a

- 3a. Understand two fractions as equivalent (equal) if they are the same size, or the same point on a number line.

ADDITIONAL CLARIFICATION/EXAMPLES

Note: Fractions are limited to those with denominators 2, 3, 4, 6, and 8.

3.NBT.A.3b

- 3b. Recognize and generate simple equivalent fractions.

Explain why the fractions are equivalent.

ADDITIONAL CLARIFICATION/EXAMPLES

e.g., $\frac{1}{2} = \frac{2}{4}$; $\frac{4}{6} = \frac{2}{3}$

e.g., using a visual fraction model.

Note: Fractions are limited to those with denominators 2, 3, 4, 6, and 8.

3.NF.B.3c

- 3c. Express whole numbers as fractions, and recognize fractions that are equivalent to whole numbers.

ADDITIONAL CLARIFICATION/EXAMPLES

e.g.,

- Express 3 in the form $3 = \frac{3}{1}$
- Recognize that $\frac{6}{3} = 2$
- Locate $\frac{4}{4}$ and 1 at the same point on a number line

Note: Fractions are limited to those with denominators 2, 3, 4, 6, and 8.

3.NBT.A.3d

- 3d. Compare two fractions with the same numerator or the same denominator by reasoning about their size. Recognize that comparisons rely on the two fractions referring to the same whole. Record the results of comparisons with the symbols $>$, $=$, or $<$, and justify the conclusions.

ADDITIONAL CLARIFICATION/EXAMPLES

e.g., using a visual fraction model.

Note: Fractions are limited to those with denominators 2, 3, 4, 6, and 8.

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Lesson 19 Understand Equivalent Fractions—pp. 166–173

Lesson 20 Write Equivalent Fractions—pp. 174–181

Lesson 21 Relate Whole Numbers and Fractions—pp. 182–189

Lesson 22 Compare Fractions: Same Denominator—pp. 190–197

Lesson 23 Compare Fractions: Same Numerator—pp. 198–205



Grade 3

Measurement & Data

GRADE 3 NYS LEARNING STANDARDS FOR MATHEMATICS

A. Solve problems involving measurement and estimation of intervals of time, liquid volumes, and masses of objects.

3.MD.A.1

1. Tell and write time to the nearest minute and measure time intervals in minutes. Solve one-step word problems involving addition and subtraction of time intervals in minutes.

ADDITIONAL CLARIFICATION/EXAMPLES

e.g., by representing the problem on a number line or other visual model.

Note: This includes one-step problems that cross into a new hour.

3.MD.A.2

3.MD.A.2a

- 2a. Measure and estimate liquid volumes and masses of objects using grams (g), kilograms (kg), and liters (l).

ADDITIONAL CLARIFICATION/EXAMPLES

Note: Does not include compound units such as cm^3 and finding the geometric volume of a container.

3.MD.A.3b

- 2b. Add, subtract, multiply, or divide to solve one-step word problems involving masses or liquid volumes that are given in the same units.

ADDITIONAL CLARIFICATION/EXAMPLES

e.g., using drawings (such as a beaker with a measurement scale) to represent the problem.

Note: Does not include multiplicative comparison problems involving notions of “times as much.”

B. Represent and interpret data.

3.MD.B.3

3. Draw a scaled picture graph and a scaled bar graph to represent a data set with several categories. Solve one- and two-step “how many more” and “how many less” problems using information presented in a scaled picture graph or a scaled bar graph.

ADDITIONAL CLARIFICATION/EXAMPLES

e.g., draw a bar graph in which each square in the bar graph might represent 5 pets.

3.MD.B.4

4. Generate measurement data by measuring lengths using rulers marked with halves and fourths of an inch. Show the data by making a line plot where the horizontal scale is marked off in appropriate units—whole numbers, halves, or quarters.

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Lesson 24 Problem Solving: Time—pp. 218–225

Lesson 25 Problem Solving: Volumes and Masses—pp. 226–233

Lesson 32 Problem Solving: Measurement—pp. 288–295

Lesson 25 Problem Solving: Volumes and Masses—pp. 226–233

Lesson 32 Problem Solving: Measurement—pp. 288–295

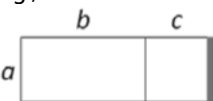
Lesson 26 Draw Graphs to Represent Categorical Data—pp. 234–241

Lesson 27 Generate and Graph Measurement Data—pp. 242–249



Grade 3

Measurement & Data

GRADE 3 NYS LEARNING STANDARDS FOR MATHEMATICS	SADLIER NEW YORK PROGRESS MATHEMATICS, GRADE 3
C. Geometric measurement: understand concepts of area and relate area to multiplication and to addition.	
3.MD.C.5 5. Recognize area as an attribute of plane figures and understand concepts of area measurement.	
3.MD.C.5a 5a. Recognize a square with side length 1 unit, called “a unit square,” is said to have “one square unit” of area, and can be used to measure area.	Lesson 28 Understand Concepts of Area Measurement— pp. 256–263
3.MD.C.5b 5b. Recognize a plane figure which can be covered without gaps or overlaps by n unit squares is said to have an area of n square units.	Lesson 28 Understand Concepts of Area Measurement— pp. 256–263
3.MD.C.6 6. Measure areas by counting unit squares. ADDITIONAL CLARIFICATION/EXAMPLES Note: Unit squares include square cm, square m, square in., square ft., and improvised units.	Lesson 28 Understand Concepts of Area Measurement— pp. 256–263
3.MD.C.7 7. Relate area to the operations of multiplication and addition.	
3.MD.C.7a 7a. Find the area of a rectangle with whole-number side lengths by tiling it, and show that the area is the same as would be found by multiplying the side lengths.	Lesson 29 Find Areas of Rectangles: Tile and Multiply— pp. 264–271
3.MD.C.7b 7b. Multiply side lengths to find areas of rectangles with whole-number side lengths in the context of solving real world and mathematical problems, and represent whole-number products as rectangular areas in mathematical reasoning.	Lesson 29 Find Areas of Rectangles: Tile and Multiply— pp. 264–271
3.MD.C.7c 7c. Use tiling to show in a concrete case that the area of a rectangle with whole-number side length a and side length $b + c$ is the sum of $a \times b$ and $a \times c$. Use area models to represent the distributive property in mathematical reasoning.	Lesson 30 Find Areas of Rectangles: Use the Distributive Property—pp. 272–279 Lesson 32 Problem Solving: Measurement—pp. 288–295
ADDITIONAL CLARIFICATION/EXAMPLES e.g., 	



Grade 3

Measurement & Data

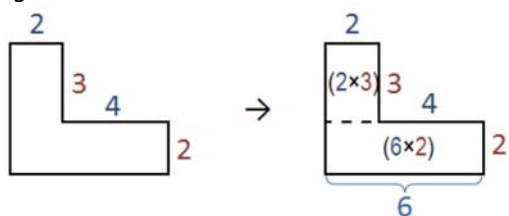
GRADE 3 NYS LEARNING STANDARDS FOR MATHEMATICS

3.MD.C.7d

- 7d. Recognize area as additive. Find areas of figures composed of non-overlapping rectangles, and apply this technique to solve real world problems.

ADDITIONAL CLARIFICATION/EXAMPLES

e.g.,



Note: Problems include one unknown side length.

D. Geometric measurement: recognize perimeter as an attribute of plane figures and distinguish between linear and area measures.

3.MD.D.8

3.MD.D.8a

- 8a. Solve real world and mathematical problems involving perimeters of polygons, including finding the perimeter given the side lengths or finding one unknown side length given the perimeter and other side lengths.

3.MD.D.8b

- 8b. Identify rectangles with the same perimeter and different areas or with the same area and different perimeters.

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Lesson 31 Find Areas: Decompose Figures into Rectangles—pp. 280–287

Lesson 32 Problem Solving: Measurement—pp. 288–295

Lesson 33 Problem Solving: Perimeter—pp. 296–303

Lesson 34 Problem Solving: Compare Perimeter and Area—pp. 304–311

Lesson 33 Problem Solving: Perimeter—pp. 296–303

Lesson 34 Problem Solving: Compare Perimeter and Area—pp. 304–311

Geometry

GRADE 3 NYS LEARNING STANDARDS FOR MATHEMATICS

A. Reason with shapes and their attributes.

3.G.A.1

1. Recognize and classify polygons based on the number of sides and vertices (triangles, quadrilaterals, pentagons, and hexagons). Identify shapes that do not belong to one of the given subcategories.

ADDITIONAL CLARIFICATION/EXAMPLES

e.g., Include both regular and irregular polygons, however, students need not use formal terms “regular” and “irregular,” e.g., students should be able to classify an irregular pentagon as “a pentagon,” but do not need to classify it as an “irregular pentagon.”

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Lesson 35 Understand Shapes and Attributes—pp. 312–319



Grade 3

Geometry

GRADE 3 NYS LEARNING STANDARDS FOR MATHEMATICS

3.G.A.2

2. Partition shapes into parts with equal areas. Express the area of each part as a unit fraction of the whole.

ADDITIONAL CLARIFICATION/EXAMPLES

e.g., partition a shape into 4 parts with equal area, and describe the area of each part as $\frac{1}{4}$ of the area of the shape.

SADLIER NEW YORK PROGRESS MATHEMATICS, GRADE 3

Lesson 36 **Partition Shapes to Make Equal Areas**—pp.
320–327