The Evidence Basis Behind Sadlier Math[™] | Grades K-6

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Introduction

The instructional and programmatic features of *Sadlier Math* were built to develop mathematically proficient students by supporting the findings and recommendations of:

- The National Mathematics Advisory Panel (NMAP) in the areas of Curricular Content, Learning Process, Instructional Practices, and Assessment of Mathematics Learning
- The Shifts in Mathematics (focus, coherence, and rigor) as defined by the Student Achievement Partners (www.achievethecore.org), Common Core State Standards (CCSS), and the Publisher's Criteria
- The National Council of Teachers of Mathematics (NCTM) Principles and Standards

Curricular Content

NMAP Findings & Recommendations

Focused, coherent progression of mathematics learning, with an emphasis on proficiency with key topics, should become the norm in elementary and middle school mathematics curricula. (p. xvi)

The mathematics curriculum in Grades PreK-8 should be streamlined and should emphasize a well-defined set of the most critical topics in the early grades. (p. xiii)

How Addressed in Sadlier Math

The table of contents of each grade level is organized around a focused, coherent group of mathematical topics to help build students' understanding of key skills and concepts.

Lessons at each grade level focus on the Benchmarks for the Critical Foundations of the grade levels as defined by NMAP and the National Council of Teachers of Mathematics (NCTM) Curriculum Focal Points.

Learning Progression charts in **About the Chapter** in the Teacher's Editions describe how skills and concepts are developed within and across grade levels.

A Coherent Progression of Skills

Across the Grade Levels

٦.	GRADE 3 Chapter 9 Fraction Concepts	GRADE 4 Chapter 12 Fractions: Multiply by a Whole Number	GRADE 5 Chapter 8 Fractions: Multiplication
Within a Grade Lew	S1 Chapter Opener StAM Commetter 167 91 Understand Equal Parts. 188 92 Name Unit Fractions of a Whole. 190 93 Find Unit Fractions on a Number Line. 192 94 Name Fractions of a Whole. 196 95 Find Fractions of a Whole. 196 95 Find Fractions on a Number Line. 198 95 Use a Fraction to Find the Whole. 200 97 Problem Solving: Use a Model. 202 Chapter Review. 204 Performance Assessment StAM Commetor Fluency Practice. 208 208 208	Chapter Opener St&M Connection 249 I2-1 Add Unit Fractions to Multiply. 250 I2-2 Model Multiplying a Unit Fraction and a Whole Number. 252 I2-3 Multiply a Unit Fraction and a Whole Number. 254 Check Your Progress. 256 I2-3 Multiplying a Fraction and a Whole Number. 258 I2-5 Multiply a Fraction and a Whole Number. 260 I2-5 Represent Situations Involving Multiplying a Fraction and a Whole Number. 260 I2-6 Represent Situations Involving Multiplying a Fraction and a Whole Number. 264 Chapter Review. 266 Performance Assessment 312M Connector 288 Fluency Practice. 270 270	Chapter Opener STEAM Connection

CHAPTER

Curricular Content (continued)

Multiplication Concepts

About the Chapter

n this chapter, students extend their study of multiplication as they explore the Essential Question: How can place-value models help you multiply? They will learn about properties of multiplication, representing products with place-value models, and basic computations as they move towards multidigit multiplication in upcoming chapters.

The table shows the coherence and progression of growth in work with multiplication across the third- through fifth-grade span.

Learning Progression

Grade 3	Grade 4	Grade 5
Develop the concept of multiplication. Fluently multiply within 100. Multiply 1-digit numbers by tens.	Multiply a 1-digit number and a 2-, 3-, or 4-digit number or multiply two 2-digit numbers.	Fluently multiply multidigit numbers. Multiply decimals to hundredths.
Use place value to round whole numbers to the nearest 10 or 100.	Use place value to round numbers to different places and use these to estimate products.	Use place value to round decimals to different places and use these to estimate products.
Learn the Commutative, Associa- tive, and Distributive Properties of Multiplication.	Learn and apply properties of multiplication to extend multiplica- tion to multidigit numbers.	Write expressions with grouping symbols and perform order of operations.
Interpret products of whole numbers.	Write multiplicative comparisons as equations.	Interpret multiplication as scaling (resizing).

Teaching Tips and Practices

In the next two chapters, students will learn how to multiply multidigit numbers. It is critical that they understand the Distributive Property to do this, as well as multiplication by tens, hundreds, and thousands. It is a combination of these skills that leads to the general algorithm for multiplication.

Place-value models are used throughout the chapter. To support these, you can use a variety of visual models, such as base ten blocks and place-value charts, so that students will achieve the understanding of the concepts that underlie multidigit multiplication. Area models can be used to compare actual products to estimated products. Students will be able to see that the error in the approximation is the difference in the areas.

STEAM Connections

♦ Students will explore consumer packaging and apply multiplication concepts. Without computing volumes, they will compare rectangular prisms and determine how many smaller boxes can be packed in a shipping box. They will use place-value models, the Distributive Property, and estimation strategies to answer packing questions. (NGSS 5)

CHAPTER 4 = 67A

Learning Process

NMAP Findings & Recommendations

To prepare students for Algebra, the curriculum must simultaneously develop conceptual understanding, computational fluency, and problem-solving skills. (p. xix)

Use should be made of what is clearly known from rigorous research about how children learn, especially by recognizing the mutually reinforcing benefits of conceptual understanding, procedural fluency, and automatic (i.e., quick and effortless) recall of facts. (p. xiv)

How Addressed in Sadlier Math

Skills and concepts are taught through a consistent 3-step lesson design (**Develop Concepts**, **Use the Student Pages**, **Summarize**), which provides routine opportunities with fluency practice, concept development, application problems, and daily formative assessment opportunities. Skills and concepts are developed using Concrete-Pictorial-Abstract presentations to ensure students have a thorough understanding of mathematics.

Step 1, **Develop Concepts**, the concrete presentation, activates students' prior knowledge and builds foundational understanding of concepts that are new and more complex. Mathematical skills/ concepts are introduced through the use of models and virtual manipulatives to help students visualize math and make connections. Manipulatives help students become active learners, make connections, and develop conceptual understanding.

Step 2, **Use the Student Pages**, the pictorial and abstract presentations, provides guidance to support explicit step-by-step instruction for the teaching of the lesson.

This step employs the Gradual Release of Responsibility model to support student's development of the lesson's learning objective(s).

Teaching strategies and tips for Guided and Independent Practice help teachers guide students in applying and synthesizing their new knowledge.

Guided Practice offers students an opportunity to practice their newly-learned skills with teacher support and to collaborate with other students.

Learning Process (continued)



Learning Process (continued)

NMAP Findings & Recommendations

(continued)

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Use should be made of what is clearly known from rigorous research about how children learn, especially by recognizing the mutually reinforcing benefits of conceptual understanding, procedural fluency, and automatic (i.e., quick and effortless) recall of facts. (p. xiv)

How Addressed in Sadlier Math

(continued)

The **Independent Practice** section provides intentionally sequenced and scaffolded exercises so that students build knowledge to reach the expectation of the learning objective. Application problems require students to apply the four-step problem-solving model (Read-Plan-Solve-Check) to efficiently and accurately solve problems.

Exit Ticket (✓) allows you to efficiently assess students' basic understanding of each lesson's objective(s).

Mental Math, daily fluency practice, is identified at point of use in each lesson of the Teacher's Edition and is available online at www.SadlierConnect.com.

Step 3, **Summarize**, provides closure activities that act as a lesson wrap-up to check students' understanding of the lessons' skills and concepts and help inform subsequent instruction.

Each lesson provides **More Practice, Homework**, and **Differentiated Activities** to support lesson development and ensure all students achieve the lesson's learning objectives. All exercises are correlated to the Standards for Mathematical Practice (MP) and Webb's Depth of Knowledge (DOK) levels to help easily identify students' levels of proficiency. Instructional strategies are provided to modify each lesson in response to student differences in readiness and learning needs.

Problem Solving lessons in each Chapter provide students with rich opportunities to use various strategies and to apply math to cognitively demanding problems.

Learning Process (continued)

	_	_	
English	Language	learners	

Learners will benefit from focusing on using a model.

Read Exercise 13 on page 71 **Struggling Learners** Dra

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A multiplication model is shown below.

Early Finishers

Display the following multiplication model, and ask students to write a multiplication expression the model represents, determine the product, and explain how they used regrouping to find the product.

What Answer: $2 \times 96 = 192$

Wh Since each of the 2 groups contained 16 ones, I regrouped Ans 10 of those ones into 1 ten, making each group have 9 tens and 6 ones. 2 times 9 tens is 180, 2 times 6 ones is 12, and 180 + 12 = 192.



Exercise 2 requires a single regrouping of

model and do the regrouping. This requires regrouping ones and not tens.

INDEPENDENT PRACTICE

Exercise 10 requires regrouping ones and Exercise 11 requires regrouping both ones

Exercise 12 Students are required to determine which numbers are the factors of the product they will be modeling, as the problem involves 3 numbers. How is Exercise 12 different from the examples you have seen so far? Can you tell which numbers are the factors of the product you are modeling?

Exercise 14 Suggest to students that they use base ten blocks, or even pencil and paper, to help visualize the regrouping that must take place in this problem before

<u>Summarize</u>

LESSON 4-2 • 71

represent multiplication? (Model one of the factors with base ten blocks. Then use the other factor to see how many times to repeat the model. Regroup to simplify the

MORE PRACTICE SUMMARY (WB p. 51)									
ltem	MP	DOK							
1–3	4	2							

HOMEWORK SUMMARY (WB p. 52)									
ltem	MP	DOK							
1–3	7	2							
4	1	2							
5	2	2							
6	6	3							

Instructional Practice

NMAP Findings & Recommendations

High-quality research does not support the contention that instruction should be either entirely "student-centered" or "teacher-directed." Research indicates that some forms of particular instructional practices can have a positive impact under specified conditions. (p. xiv)

High-quality research does not support the exclusive use of either approach. (p. xxii)

How Addressed in Sadlier Math

Sadlier Math utilizes a balance approach to student-centered and teacher-directed instruction.

Step 1 of teaching the lesson, **Develop Concepts**, engages students in the exploration of the skills/ concepts introduced in the lesson.

Step 2, **Use the Student Pages**, incorporates all three steps of the Gradual Release of Responsibility model (Pearson and Gallagher, 1983) beginning with direct and guided instruction (*I do it.*), guided practice (*We do it.*), peer collaboration (*You do it together.*), and concludes with independent practice (*You do it independently.*).

Instructional Practice (continued)



Assessment

NMAP Findings & Recommendations

Teachers' regular use of formative assessments improves their students' learning, especially if teachers have additional guidance on using the assessment results to design and individualize instruction. (p. 47)

How Addressed in Sadlier Math

Sadlier Math's comprehensive diagnostic, formative, and summative assessments—in print and digital formats—help teachers monitor student progress toward mathematical proficiency, support differentiated instruction, and expose students to different item types. Varied and frequent assessments are essential for providing students with feedback to improve learning and build knowledge, keeping parents informed. Meaningful and timely feedback to students improves learning.

With Sadlier Math's comprehensive assessment system, teachers assess before each chapter to identify gaps and accelerate pacing when appropriate; assess during each chapter to adjust instruction, thus meeting students' immediate needs; and assess after each chapter to determine levels of concept mastery and determine the next step in the instructional process.

Each chapter concludes with **Before Leaving the Chapter**, which provides guided questions at the end of the chapter to promote discussion and reflection in order to bring closure to the chapter's learning objectives. Student and Teacher Reflections allow students to become aware of their progress and teachers to consider how their teaching can improve.

Sadlier Math's Comprehensive Assessment Plan

ASSESSMENT TYPE	ASSESSMENT	WHAT IS ASSESSED	FREQUENCY	WHERE FOUND*
Diagnostic	Beginning-of-Year Test	Previous grade-level learning objectives	Once per grade level	• Student Test Booklets • Online Assessments
Diagnostic	Pre-Chapter Diagnostic Test	Chapter prerequisite skills	Once per chapter	Online Assessments
Formative	Exit Ticket	Lesson objectives	In every lesson	Teacher's Edition
Formative	Check Your Progress	A cluster of lesson learning objectives	One to two times per chapter	Student Editions Online Assessments
Formative	Chapter Reviews	Chapter learning objectives	Once per chapter	Student Editions Online Assessments
Summative	Performance Assessments	Integration of multiple chapter learning objectives	Once per chapter	Student Editions Online Assessments
Summative	Chapter Tests	Chapter learning objectives	Once per chapter	Student Test Booklets Online Assessments
Summative	Cumulative Tests	Cumulative learning objectives in every three chapters	Every three chapters	Teacher's Edition of Student Test Booklets Online Assessments
Summative	End-of-Year Test	Grade-level learning objectives	Once per grade level	Student Test Booklets Online Assessments

Student Reflection Before Leaving the Chapter Ask students to write a few paragraphs about their learning expen Chapter 4, students extended their knowledge of multiplication by using place-value models. They learned the properties of multiplication; how to multiply by tens, hundreds, and thousands; and how to estimate products. riences with this chapter. Display the following questions on the board, and suggest that students use them to guide their writing: 1. Which multiplication concepts were easiest for you to learn? Students also represented multiplicative comparison with equations. Which were most difficult? 2. Do you understand why you are learning this material? 3. What ideas about multiplication are you still struggling with? Essential Question: How can place-Possible responses: 4. What questions do you have about the things you learned in help you multiply? Possible responses: Respond to the Essential Question When you have a multiplication expression, you can ble copies the model of one factor. Then you can ble copies of this to show the other factor. The you can ble copies of this to show the other factor. Display the Chapter 4 Essential Question, of the model is the value of the expression. this chapter? Reading your students' reflections may give you a better sense of their comfort level with the concepts in this chapter and indicate wheth **Teacher Reflection** and give students a minute or two to think about the answer. Ask volunteers to share When you have word problems, you can use a place-value model to represent the situation. You can regroup the model and find the answer. their responses. You might find it useful to reflect on your teaching of this chap-Critical Understandings Use these ideas of the chapter. Bulleted items suggest son of the important points to emphasize during the discussion. ter. This may give you insight into the methods and approaches How can you estimate a product of a one-digit number and a two- or three-digit number? that work best with your students. It might also suggest ideas for changes and adjustments you can make next time you teach You can use front-end estimation to replace the greater number by a number in the tens of hundreds and then multiply. this chapter Here are some questions to consider: How are the properties of multiplication similar and different from the properties of addition? Both operations have a Commutative and Associative Property. You can change the order or the grouping and get the same answer. You can round the greater number to the nearest ten or hundred and then multiply. 1. Which multiplication concepts were you most comfortable teaching? Which concepts were you least comfortable How can you compare numbers using multiplication? teaching? 2. Which multiplication concepts and skills did your students You can say that one number is several times as many as another. For example, 20 is 5 times as many as 4. struggle with most? Why do you think they struggled? Both operations have an Identity Property. For addition, you add 0 to get back the same number. For multiplication, you multiply by 1 to get back the same number. 3. Which multiplication concepts did your students find easy to You can write a multiplication sentence or equation, such as 20 = 5 × 4. understand? Why do you think so? 4. Is there a lesson or multiplication concept you wish you had How can you multiply a one-digit number by tens, hundreds, or thousands? When you use a place-value model to represent a product, how do you find its value? spent more time on? Is there a lesson or multiplication concept you feel you spent too much time on? First, you multiply the nonzero digits. Then you count the number of zeros in the factors and write that many on the end of the product. You have to regroup. You turn every group of 10 ones into 1 ten. The leftover ones is the digit in the ones place. You turn every group of 10 tens into 1 hundred. The leftover tens is the The leftover tens is the You can use the Associative Property to rewrite digit in the tens place. Then you write the number of hundreds in the hundreds place. the expression You might share the following information about what is ahead: Look Ahead In **Chapters 5 and 6**, students allead: study multiplication of one- and two-digit numbers by multidigit Explain to students that u standing multiplication is ing multiplication is many problems and will continue to study pcoming chapt In Grades 5 and 6, students will learn multiplication of decimals. 86A = CHAPTER 4

Feacher's Edition, , Grade

4

Vocabulary Recap eview these key vocabulary erms from **Chapter 4** with tudents:

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multiplication expression. multiply, product, estimate, rounding, front-end estimation, multiplication equation, factors, place-value model

Invite volunteers to define the terms in their own words and to give examples.

If students are making their own glossaries, have them add defini tions, illustrations, and examples for these terms.



In Chapter 9, students will study factors and multiples. In Grade 5, students will learn multiplication of multidigit

CHAPTER 4 = 86B

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Shifts in Mathematics Common Core Standards

Shift	Requirement	How Addressed in <i>Sadlier Math</i>
Focus	Class time and energy spent on a deeper focus on the key concepts as prioritized by the standards.	<i>Sadlier Math</i> is designed to focus on the major work of the grade per the CCSS.
Coherence	Learning within and across grade levels is carefully connected in order to build student understanding.	The Table of Contents exemplifies a focused curriculum that includes logically sequenced lessons within a grade level and across grade levels, ensuring students become fluent in mathematics as they progress through the program. Concepts that are tightly linked together help students build new understanding of the foundations they developed in prior lessons/years. Learning Progression charts that describe how the standards are developed within and across the grade levels are provided for each Chapter in the Teacher's Editions.
Rigor as Fluency	Students are expected to have speed and accuracy with simple calculations; teachers structure class or homework time for students to memorize through repetition.	Fluency practice is provided within each lesson as Mental Math warm ups, at the end of each chapter, and online at www.SadlierConnect.com .
Rigor as Deep Understanding	Students deeply understand and can operate easily within a math concept before moving on.	 Based on instructional best practices for concept and skill development, each lesson plan provides support for effective math instruction in three steps: STEP 1 Develop Concepts STEP 2 Use the Student Pages STEP 3 Summarize

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Shifts in Mathematics Common Core Standards (continued)

Shift	Requirement	How Addressed in <i>Sadlier Math</i>
Rigor as Application	Students use math and choose appropriate concept for application– not only when prompted.	Problem Solving lessons in each Chapter provide students with rich opportunities to use various strategies and apply math to cognitively demanding problems.
		A 4-step problem-solving process gives students a framework for problem solving and making sense of problems.
		<i>Source: George Polya,</i> How to Solve It: A New Aspect of Mathematical Method (<i>Princeton, NJ: Princeton University Press, 1945</i>).
		While working independently on the Independent Practice, More Practice, Homework, and the Performance Assessments, students must determine which skills, strategies, and practices best serve to solve the problems and tasks at hand.
Rigor as Dual Intensity	Students are practicing and understanding with intensity.	As students work through the scaffolded Practice, More Practice, and Homework exercises, teachers can gauge student understanding of the concepts. The Error Alert! provided in the Teacher's Edition guides teachers in addressing common misconceptions. Through both direct instruction and practice, students work toward a deep understanding of the concept.

References

http://www.ed.gov/about/bdscomm/list/mathpanel/index.html Foundations of Success: The Final Report of the National Mathematics Advisory Panel. March 2008.

Martin T. (2009). "A theory of physically distributed learning: How external environments and internal states interact in mathematics learning." *Child Development Perspectives*.

Chickering, A. & Gamson Z. 1987, "Seven principles for good practice in undergraduate education," Reprinted by University of Illinois, Springfield, viewed 24 May 2012, Isaacs, G. 2001, *Assessment for Learning*, The University of Queensland, Brisbane.

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